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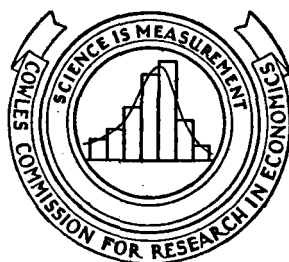
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# GENERAL-EQUILIBRIUM THEORY IN INTERNATIONAL TRADE

By  
JACOB L. MOSAK



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## PREFACE

This book is an attempt to bridge the gap that has existed thus far between the general theory of value for a closed economy and the theory of international trade. It stems primarily from the work of the mathematical school of economists to which I was first introduced by the late Professor Henry Schultz. Although he died before I began this study, I am heavily indebted to him for instruction and inspiration. His friendship and warm personal interest in me will always be a treasured memory.

This study was presented as a doctoral dissertation at the University of Chicago in the summer of 1941. The members of my dissertation committee were Professor Jacob Viner, chairman, and Professors Oscar Lange and Theodore O. Yntema. I am indeed indebted to all three, not only for general intellectual stimulation, but also for their constant encouragement and friendly help. They each read the manuscript carefully and made many helpful suggestions. I need hardly add, however, that the responsibility for any errors is mine alone.

I also wish to express my sincere appreciation to Mr. Dickson H. Leavens, the editor of the Cowles Commission Monographs, for his invaluable aid in preparing the book for the printers.

JACOB L. MOSAK

*Washington, D.C.*

*July, 1944*

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