# THE SCALING OF TEACHERS' MARKS AND ESTIMATES

#### By

#### DOUGLAS M. McINTOSH

M.A., B.Sc., B.Ed., Ph.D. Director of Education, Fife.

#### DAVID A. WALKER

M.A., B.Ed., Ph.D. Depute Director of Education, Fife.

#### DONALD MACKAY

M.B.E., M.C., M.A. Headmaster, Viewforth Secondary School, Kirkcaldy.

OLIVER AND BOYD

EDINBURGH: TWEEDDALE COURT LONDON: 98 GREAT RUSSELL STREET, W.C.

#### OLIVER AND BOYD LTD.

EDINBURGH AND LONDON

Sole Agents outside the British Isles (Except in Canada and the U.S.A.)

MACMILLAN & CO. LIMITED LONDON ROMBAY CALCUTTA MADRAS MELBOURNE

Sole Agents for Canada

CLARK, IRWIN & CO. LIMITED TORONTO

1949

PRINTED IN GREAT BRITAIN BY
A. WALKER & SON, LTD., GALASHIELS
FOR OLIVER & BOYD LTD., EDINBURGH

#### **FOREWORD**

THE publication of this book reflects a belief, which I share with Dr McIntosh, that the scaling of teachers' marks will have an established and permanent place not merely in educational research but in many departments of everyday educational practice. We used the technique on a large scale in our Dundee investigation on Selection for Secondary Education, and our experience left us both with a conviction of its practical possibilities—a conviction that has been greatly strengthened by the results of later researches by Dr McIntosh, Dr Walker and Mr Mackay.

Estimates of pupils' attainments in school subjects are needed for a multitude of practical educational purposes; and it is part of my educational faith that the assessments of the teachers provide the best guide that is, or ever will be, available as to the order of merit of their pupils in these attain-But, unfortunately, the standard and scatter of marks vary from teacher to teacher and from school to school; and while teachers' assessments may be improved in this respect, it is extremely doubtful whether they could ever be steadied to such an extent that they could be used with assurance as a basis for the serious decisions involved in selection for secondary education or the award of Leaving Certificates. If these premises are sound, there is no escape from the conclusion that teachers' marks should be used for such purposes, but only if they have been scaled in such a way that the estimates of different teachers are comparable.

Scaling has already been employed in practice to a considerable extent, particularly in selection for secondary education, but one suspects that it would have been more widely used but for two relatively groundless fears. The first is that this is a tool that can be handled only by the expert mathematical statistician: the second is that a prohibitive amount of laborious calculation is involved. The present volume should do much to dispel these fears. It gives a simple explanation

of the basis of scaling, and clear and definite instructions as to the best ways of making the calculations. Now that such a work is available there should be little difficulty in the use of the technique by the staff of an Education Office, the headmaster or the class teacher.

The book is, however, much more than a statistical primer giving instructions for the use of methods that are already well known: it is an important contribution to educational research. In the hands of Dr McIntosh and his colleagues, new and improved scaling procedures have been evolved—procedures that have passed the acid test of extensive use in actual practice. New fields for the application of scaling methods are opened up; and headmasters and class teachers who study the authors' suggestions will find their reward in increased interest in their work and fuller satisfaction that they are carrying out their important task of adjusting the education they provide to the varying talents and needs of their pupils.

WILLIAM McCLELLAND

#### **PREFACE**

THE ideas developed in this book have their origin in McClelland's "Selection for Secondary Education." In that book a clear case was presented against the use of teachers' estimates for the purpose of selection unless they were made comparable from school to school.

These ideas were further developed in the Report of the Scottish Advisory Council on Secondary Education. Here the scaling procedure was suggested for use in an examination scheme for the award of the Leaving Certificate and, again, on the discussion of marks and terminal reports, it was suggested that school examination marks should be made comparable by some method not aiming at "statistical impeccability, but rather something reasonably valid yet easily workable by the busy teacher in the school."

We have attempted to attain the Advisory Council's objective. No deep knowledge of statistics is required for the understanding of our methods. Chapter III on "A Little Statistics" will, we hope, give all that is necessary for the understanding of the techniques we have devised: it is an attempt at statistics without tears.

We should like to emphasise also that our methods are not merely theoretical but have been adopted in practice both in education offices and in a large junior secondary school. The needs of the administrator and "the busy teacher in school" have been in the forefront of our minds all the time.

We wish to acknowledge our indebtedness to Mr McClelland for writing the foreword, for the keen interest he showed in our work and for the many helpful suggestions which he made. Mr W. F. Lindsay, Assistant Director of Education for Fife, read the manuscript in its various stages and offered many constructive criticisms. We also received much help regarding the layout of the book from Mr S. Stewart, Educational Editor of Messrs Oliver & Boyd. For illustrative materials in Chapters VII and VIII we are indebted to Midlothian Education Committee.

#### CONTENTS

	Foreword		•	•			•	v
	Preface .	•		•		•	•	vii
Chapter								
I.	Examination	s.	•					1
II.	The Need for	r Scal	ling				•	5
III.	A Little Stat	istics		•				12
IV.	From Physic	al to	Menta	al Scal	ling			29
V.	The Scaling l	Proce	dure			•		35
VI.	Scaling Teac	hers'	Estim	ates—	-Some	Furt	her	
	Points .	•	•	•	•	•	•	46
VII.	The Standard							49
	in Practice							49
VIII.	Promotion Education		Prin	•				57
IX.	The Leaving							62
X.	Classroom S	Scalin	g—As	signin	g Cla	ss M	ean	
	Marks		•	•	•	•	•	72
XI.	Scaling in th	e Cla	ssroor	n.		•	•	80
	Postscript							93

### **APPENDICES**

Appendi	ix	
I.	Examples of Objective Tests in English, Latin and Mathematics	9:
II.	Calculation of the Mean with Grouped Data	98
III.	Calculation of the Standard Deviation with Grouped Data	99
IV.	Table of Standard Deviations and Percentiles	100
V.	Table of Percentiles and Standard Deviations	10
VI.	Arithmetical Method of Scaling	102
VII.	Adjusting Table	106
VIII.	Percentiles and Corresponding Class Ranks	107
IX.		108
X.	Key Points for Classes	109

# LIST OF FIGURES

Figure		
I.	Distribution of Marks in Test A	8
II.	Distribution of Marks in Test B	. 8
III.	Distribution of Marks in Test C	9
IV.	Illustration of Difference in Mean and Scatter of School Marks	11
V.	Diagrammatic Representation of Frequency Distribution A	14
VI.	Histogram of Normal Distribution of IQs	20
VII.	Area under Normal Curve	22
VIII.	Percentile Curve or Ogive	25
IX.	Percentile Curve on Permille Paper	26
Χ.	Graph of Percentile Distribution of IQs on Permille Paper	27
XI.	Converting Centigrade to Fahrenheit by Graphical Method	31
XII.	Conversion Chart for Fahrenheit, Centigrade and Réaumur Temperatures	32
XIII.	Graph for Scaling Teachers' Estimates .	39
XIV.	Graphs for Scaling Teachers' Estimates in English in School E	43
XV.	Permille graphs for Scaling Teachers' Estimates in English in School E	44
XVI.	Percentile Curve of 1379 Arithmetic Marks and Normal Percentile Curve	52
XVII.	Percentile line of 1379 Arithmetic Marks and Normal Percentile Line	56
XVIII.	Record of Qualifying Data	60

# xii

## **CONTENTS**

Figure	•	
XIX.	Results of Scaling Leaving Certificate Estimates from Schools A and B	64
XX.	Graphs for Scaling Leaving Certificate Teachers' Estimates	68
XXI.	Rubber Stamp Imprint for Scaling Calculation	84
XXII.	Horizontal Axis of Sigma Chart	88
XXIII.	Sigma Chart for Scaling 14 Class Marks .	90
XXIV.	Graphical Method of Scaling History Marks for 27 Pupils	92

# LIST OF TABLES

Tab	le	
1.	Frequency Distribution of Marks for Examinations A, B and C	13
2.	Calculation of Percentiles in a Frequency Distribution	18
3.	Normal Distribution of IQs	20
4.	Estimates and Marks in English for 20 Pupils	3′
5.	Estimates for English Scaled by Calculation and by Graphical Method	4(
6.	Frequency Distribution of Scores and Estimates in English in School E	4
7.	Calculation of Percentiles for Upper Limit of class Intervals. Scores and Estimates in English in School E	42
8.	Extract from Conversion Table	4:
9.	Distribution of Arithmetic Marks of 1379 Pupils	5
10.	Percentiles for Normal Distribution with Mean 65 and Standard Deviation 15	5.
11.	Converting Raw Marks in Arithmetic into Standardised Marks	54
12.	Raw and Scaled Estimates of 13 Pupils selected from Schools A and B	6.
13.	Typical Distribution of Scaled Marks	78
14.	History Examination Marks for 27 Pupils .	8:
15.	Benchwork Marks for a class of 15 Boys .	8:
16.	Raw and Scaled Marks for a class of 14 Pupils	89
17.	Calculation of the Mean from Grouped Data.	9
18.	Calculation of Standard Deviation from Grouped	9

## xiv

## CONTENTS

Tab	le			
19.	Percentiles for Given Standard Deviations .	100		
20.	Standard Deviations for Given Percentiles .			
21.	Calculation of Scaling Equation—First Method	102		
22.	Scaling Table	103		
23.	Calculation of Scaling Equation from Grouped Data	105		
24.	Adjusting Table	106		
25.	Percentiles and Corresponding Class Ranks .	107		
26.	Number of Marks for $P_{84}$ and $P_{16}$	108		
27.	Key Points for Small Classes	109		
28.	Key Points for Larger Classes	110		