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Foundations of Logic and Mathematics

dolf Carnap

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Foundations of the Unity of Science

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**Foundations
of the Unity of Science**

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