

Major Gen Sir G. Holman K.C.B.  
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R E P O R T  
ON A  
**SCHEME FOR GRANTING PENSIONS**  
TO THE  
**WIDOWS AND ORPHANS**  
OF  
**OFFICERS ENTERING THE STAFF CORPS,**  
AND OF  
**CHAPLAINS AND MEDICAL OFFICERS**  
ON THE  
**INDIAN ESTABLISHMENT.**

---

BY MAJOR-GENERAL HANNYNGTON, F.S.S.,  
ASSOCIATE MEMBER OF THE INSTITUTE OF ACTUARIES.

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1870.

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To

Major General Pears, C.B.,  
Military Secretary.

Sir,

In pursuance of the instructions conveyed in your Letter, No. 1,105, dated 25th February 1869, I have the honour to submit a Report on the probable financial operation of Colonel Norman's proposal to establish a system of pensions for the benefit of widows and children of Officers of the several Staff Corps.

2. The proposal is thus stated by Colonel Norman :—“ Looking to the rates of pension formerly given, and striking somewhere about the average of the three Presidencies, I think the following would be a fair scale of pension for widows and orphans—

	£
“ Widow of a Colonel	240 a year.
“ “ Lieutenant-Colonel	200 ”
“ “ Major	160 ”
“ “ Captain	120 ”
“ “ Lieutenant	70 ”
“ Orphan, male or female, under five years of age	24 ”
“ Male orphan from 5 to 19, or any earlier age at which provided for	40 ”
“ Female orphan from 5 until married	40 ”

“ As I do not think Government need be put to more expense than a payment equivalent to the scale of pensions given in the British Army to widows and orphans, I would suggest that the donations and subscriptions should be limited to such amount as might fairly meet the cost of the increase of pensions.”

3. The scheme, thus briefly but sufficiently indicated, differs from the plan of the several funds now existing for like purposes in India, to an extent that requires the preparation of a new set of tables, and to this is owing the seeming delay in the submission of this Report.

4. As a basis for calculation the following elements are necessary :—

I. The rates of mortality for,—

Officers	-	-	-	-	(a)
Wives	-	-	-	-	(b)
Widows	-	-	-	-	(c)
Sons	-	-	-	-	(d)
Daughters	-	-	-	-	(e)

II. The rates of marriage for,—

Widows	-	-	-	-	(a)
Daughters	-	-	-	-	(b)

III. The rate of interest.

IV. The rate of exchange.

5. On these heads I have to offer some remarks.

I. (a). *The mortality among Officers.* The most complete analysis hitherto made is that by Mr. Neison from the records of the India Office for the Bengal Army. The Table XI. of his Report (1849) on the Bengal Military Fund,

exhibits a rate of mortality much lower than had previously been assigned. This table I have now used. Mr. Neison's remarks on it, page 18 of the Report, are as follows,—

"In connexion with this table, it may be stated that the rate of mortality resulting from the data given in Table IX., and as set forth in the combined form for quinquennial periods of life in Table X. was adopted as the basis of calculation up to 60; but from that age upwards, the rate of mortality prevailing among the male sex in England and Wales, advanced two years, was taken as the datum for interpolation at every interval of five years. It will be found that the rate of mortality, shown by Mr. Christie's table for retired Officers beyond the age of 60 approximates very closely to that for the male sex in England and Wales so advanced, that is, for age 65, taking the rate of mortality for age 67, and for age 70, the rate for age 72. The mortality of the more recent retirements is more favourable than that of Mr. Christie's table, but those of the earlier retirements, less so. This, then, is sufficient to explain the formation of Table XI., from which it will be seen that one half of the cadets appointed to the service at the age of 17 will be alive between the ages of 46 and 47, while of the general population of England and Wales one half of those entering on their 17th year would live to attain their 63d year, showing a difference of 17 years. Of those Officers of the Bengal Army who live to attain their 30th year, one half would pass their 56th year, while in England and Wales one half would pass their 66th year. Again, of those Officers attaining their 60th year, one half would survive their 64th year, but in England and Wales one half would survive their 68th year of life; and of those Officers living to the age of 50, one half would still live till the age of 69, but in England and Wales one half would live till the age of 73. Thus showing that the deterioration of life among Officers of the Bengal military service is greater at the younger age, when compared with the male sex generally of this country, than at the older ages; and as life advances the difference in the duration of life in the two classes, gradually becomes less and less."

I have cited this explanation, not only because it is interesting in itself, but also to show that as the table includes the retired Officers, it must be regarded as giving a full value to the subscriptions of Officers serving in India, and is therefore favourable to those Officers.

I. (b). *Mortality of Wives.*—I have used Mr. G. Davies's table as modified by him for the Bengal Military Fund. Another table, based on a larger experience, has been prepared by Mr. S. Brown, and is published in his able Report on the Madras Military Fund. But as the marginal table shows, the expectation of life deduced from Mr. Brown's table exceeds that of the female population of England as computed by Dr. Farr from his English Life Table No. 3. I have, therefore, hesitated to adopt Mr. Brown's table. Without making question as to the fact, it is yet not easily credible that ladies resident in India are more healthy than the general population of England. Mr. Brown's data include both wives and widows, and in respect of the former, he says (Report 1863, page 57),—"By far the largest proportion of lives exposed to risk was found in the former list, but the mortality as might

Age.	Expectation of Life.		
	English.		Officers Wives.
	Dr. Farr.	S. Brown.	G. Davies.
15	43.90	41.20	39.09
20	40.29	39.95	35.97
25	37.04	38.07	32.78
30	33.81	35.68	29.57
35	30.59	32.88	26.58
40	27.34	29.91	23.73
45	24.06	26.78	21.04
50	20.75	23.42	18.41
55	17.43	19.93	16.00
60	14.34	16.45	13.57

"be supposed, was excessive at the earlier ages." In the same Report, page 19, Mr. Brown says, "the results deduced will greatly modify the conclusions hitherto prevailing, though they must be used with caution till the observations of a few years longer, collected with greater care and accuracy, either confirm or correct them." I cite these passages, not by way of impugning Mr. Brown's conclusions, but only to explain the hesitation above expressed.

I. (c). *Mortality of Widows.*—I have used this as determined by Mr. Neison, on the experience of the Bengal Military Fund. It nearly agrees with that of the Madras Fund, as deduced by Mr. S. Brown,\* and is for the present purpose quite sufficient.

I. (d). *Mortality of Sons.*—Some years ago it was ascertained, from returns furnished by the Officers of the Bengal Army,

	Indian (unadjusted).	Farr, No. 3, Males.	Milne Carlisle.
0	10,000	10,000	10,000
5	7,359	7,237	6,797
10	7,136	6,899	6,460
15	6,921	6,728	6,300
20	—	6,504	6,090

that in infancy and early childhood children born and brought up in India are quite as healthy as those born in England. Such children are usually sent home at about the age of five, and are thenceforth subject to the same risks as those born in England. I have, therefore, adopted Dr. Farr's English

Life Table No. 3, which is even more favourable to life than the well known Carlisle Table, as is shown in the margin.

I. (e). *Mortality of Daughters.*—In like manner, and for the same reasons, I have adopted Dr. Farr's English Life Table No. 3, Females.

II. (a). *Rate of remarriage of Widows.*—For this I have used the rate deduced by Mr. Neison from the experience of the Bengal Military Fund. The pensions of widows are suspended during remarriage, and it is probable that this rule has a tendency to check remarriage. Mr. Neison, in a report on the Madras Medical Fund (1856), expresses an opinion that "the effect of a regulation permitting widows on remarriage to continue in receipt of one half of the amount of pension payable during widowhood, will be to accelerate remarriage 50 per cent. beyond the ratio entering into the construction" of the Bengal Table. On this view it might seem advisable to adopt the principle of granting half pensions during remarriage, as is now done in the Bombay Fund. But even admitting that under such a rule, the remarriage rate would be increased one half, this would not balance the cost of the half pensions; and, if adopted, the rates of contribution would have to be considerably raised. For this reason, I have thought it right to follow the example of the existing Bengal and Madras Funds, and, consequently, the pensions of widows, as herein set forth, are valued on the supposition that they are not payable during remarriage. There is a risk of second incumbency, perhaps two in a hundred of the widows may be expected to come on again, but they re-enter at more advanced ages, and against this risk there is a compensation, arising from the fact that many widows remarry into the service. For these the usual subscriptions and donations are paid, but they do not on second widowhood receive two pensions from the same fund. One or other of the pensions, the least of course, is forfeited, and in such cases the risk will usually have been more than repaid. I have therefore not attempted to estimate the second widowhood risk, being satisfied that it is not large.

II. (b). *The rate of marriage of Daughters.*—There is no part of the subject that has so anxiously engaged my attention as this. It appears, as above shown,

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\* Report on the Madras Military Fund, page 26, art. 46.

that the Indian widows' rate of remarriage can be no sufficient index to that of the marriage of spinsters whose fathers are living. The widow forfeits a pension in possession, and is thereby restrained from remarriage; but the daughter forfeits only a reversionary pension of small value. Her position as to marriage is free, and must be nearly the same as that of English spinsters in like circumstances. What is that position? On putting this question to Dr. Farr, he kindly placed in my hands the Fourteenth Annual Report of the Registrar General, wherein, page viii., is given a table (V. c.) showing, for each fifth year of age, the proportion married to 100 living, as deduced from the census of 1851. In this table, it will be observed that the spinsters' marriage rate is very much below the widows' marriage rate. The table is given in full, and the interpolated rate for each year of age is shown in the Appendix. Considering, however, that this general rate includes all classes of the population, and that among special classes there may be special rates, I have, with a view to safety, reduced the rate by one fifth. On this subject a letter to Dr. Farr, and his reply, are entered in the Appendix. The departure from the Indian widows' rate is wide, but the data on which it rests are unquestionable.

III. The rate of interest used is four and a half per cent. per annum; and,

IV. The rate of exchange is one shilling and elevenpence for one rupee.

6. Owing to the various conditions and contingencies that enter into such calculations as those in hand, the formulæ are more intricate than in the ordinary cases of life assurance. But they have been so fully explained by Mr. Griffith Davies, by Mr. S. Brown, by Mr. Neison, and others, that any exposition of them here is unnecessary. A summary of the formulæ is given in the Appendix, as they may be useful for future reference.

7. As to the amount of widows' pensions, the average of the existing funds gives,—

Colonel.	Lieutenant-Colonel.	Major.	Captain.	Lieutenant.
£	£	£	£	£
241	203	165	123	96

Colonel Norman has proposed,—

Colonel.	Lieutenant-Colonel.	Major.	Captain.	Lieutenant.
£	£	£	£	£
240	200	160	120	70

The widows' pensions granted in the British Army are, under ordinary conditions,—

Colonel.	Lieutenant-Colonel.	Major.	Captain.	Lieutenant.
£	£	£	£	£
100	80	70	50	40

And similar rates, under like conditions, will be granted to the widows of the Staff Corps Officers. It is therefore only necessary to supplement these to something near the extent proposed by Colonel Norman. The following rates, having a common difference of 30*l.*, will be convenient,—

Colonel.	Lieutenant-Colonel.	Major.	Captain.	Lieutenant.
£	£	£	£	£
160	130	100	70	40

and to these the contributions have been adapted.

8. The subscriptions of married Officers depend on rank, age, difference of ages of husband and wife, and the amounts of widows' pensions for the several

grades. The combinations of these elements are manifold, and, though it would be possible to fix a special rate for each particular case, such a course would be very inconvenient. Taking the differences of age between husband and wife in

Lieutenant - 5 years. the several ranks as noted in the margin,\* it will be safe to assume that the differences of age Major - 7 " advance with the rank, and that the subscriptions Lieutenant-Colonel - 8 " necessary to cover the increments of pension are General Officer - 10 " to be adjusted accordingly.

9. It is, however, to be observed that the rates of subscription payable in India could not possibly be maintained by retired Officers, and provision must therefore be made for unavoidable reduction of rate at the more advanced ages. To this end I have supposed that retirement occurs at the age of 49, and that the subscriptions are then reduced to one half. To compensate for these inadequate rates, donations on promotion and on marriage must be imposed. These have been strictly computed, and, in accordance with the results, a gradually increasing scale has been assigned, sufficient to supply the defect of the subscriptions, and to afford a margin for safety. The details of the calculation are shown in the Appendix, and the scale of subscriptions and donations is as follows, for married Officers only:—

Rank.	Donations.		Monthly Subscriptions.		Widows' Pensions.	
	On Marriage.	On Promotion.	India.	Europe.	India, monthly.	Europe, yearly.
	Rs.	Rs.	Rs.	£ s. d.	Rs.	£
General Officers -	4,000	700	50	2 10 0	140	160
Lieutenant-Colonels -	2,000	400	40	2 0 0	113	130
Majors -	1,000	200	30	1 10 0	87	100
Captains -	500	100	20	1 0 0	60	70
Lieutenants -	250	—	10	0 10 0	35	40

N.B.—The Europe rates of subscription are payable after retirement, and during furlough, and whenever full Indian pay is not received.

The pensions do not in any way interfere with the pensions ordinarily granted by the Government to the widows of Officers.

10. As regards the annuities for orphans, there have been some differences of rule in the several Presidencies. In Madras and Bombay, orphans with mothers living receive one-third less than those who have lost both parents. Such a plan introduces questions involving three lives, and specially for this reason is undesirable. In Bengal a similar end, reduction of charge, is effected by the simpler method of giving smaller pensions without distinction of case. In all the Funds the pensions during infancy and childhood are smaller than at more advanced ages. For males they cease at or under the age of 21, and for females they continue till death or marriage. The actual rates may be represented thus:—

Males - 20*l.* till six, 30*l.* till twelve, 45*l.* till twenty-one.

Females - 20*l.* , 30*l.* , 45*l.* till death or marriage.

11. The compassionate allowances granted by the British Government to the children of deceased Officers are, yearly.—

Colonel.	Lieutenant-Colonel.	Major.	Captain.	Lieutenant.
£	£	£	£	£
16	16	14	12	10

and these ordinarily cease at the age of 21 years.

12. Taking these allowances into consideration, the supplementary rates to be provided by the subscriptions of Officers, without distinction of rank, may be as follows:—

Age, under 6	-	-	-	-	-	£
" from 6 till 12	-	-	-	-	-	20
" " 12 till 21	-	-	-	-	-	30
" " 21 till death or marriage	-	-	-	-	-	45

13. Before assigning the rates of contribution for children, it is needful to consider how far these may be aided by the income to be derived from the subscriptions of unmarried Officers.

14. The Orphan Funds established in the several Presidencies did not originally grant any personal benefits to Officers, but subscription to them was an absolute condition of service. The present scheme supposes the like arrangement. Colonel Norman says, “As no Officer who is not married could benefit by the fund, I would require no donation from a bachelor joining the Staff Corps or from a bachelor on promotion from one rank to another, and his subscription I think should not exceed half that of married Officers without children.”

	Rs.	2 per cent. Rate.	
		Rs.	Rs.
General Officer	1,295	-	25
Lieutenant-Colonel	827	-	16
Major	640	-	12
Captain	374	-	7
Lieutenant	225	-	4

15. The marginal table shows the Staff Corps pay of the several grades, and also the amount, omitting fractions, of a two per cent. rate thereon. This (as will be seen) is considerably below the half of the the married rates now imposed. It is not excessive, and, being on a clearly intelligible principle, I would suggest that it be adopted. The scale of unmarried subscription will then be as follows:—

		Monthly.		
		In India.		In Europe, Half Rates.
		Rs.	£ s. d.	
General Officer	-	25	1 4 0	
Lieutenant-Colonel	-	16	0 15 4	
Major	-	12	0 11 6	
Captain	-	7	0 6 8	
Lieutenant	-	4	0 3 10	

16. The contributions of unmarried Officers, though they do not in the present scheme bring immediate personal advantage, are by no means to be regarded as unproductive, even to them. For, as will be seen, the final probability of marriage is large, and whenever marriage occurs then a substantial repayment follows. The loss, if it can ever be called a loss, affects comparatively few.

17. The proportions of married and unmarried Officers, existing together, as obtained from the records of

the Bengal Fund, are entered in the margin. In the early years of the Fund the unmarried class was about two-thirds of the whole, and, perhaps, at last the proportions would become nearly equal. But when it is

Year.	Married.	Single.	Proportion in 100.	
			Married.	Single.
1825	513	846	38	62
1835	822	1,227	40	60
1845	1,141	1,922	37	63
1855	1,601	1,824	47	53

considered, that of the single class, which includes most of the younger Officers, numbers will certainly marry, then it becomes evident that the *final* chance of marriage is large.

18. For the purpose here in view, namely, the distribution of income, as now to be explained, it will suffice to assume that the numbers of married and single are equal. And though it is not intended to make any distinction in the application of income to charge, it will yet be very convenient (as indicated in para. 13) to suppose that the contributions of unmarried Officers go to supply a rate in aid of the payments required to make provision for orphans.

19. The records of the Indian Funds show, as noted in the margin, the proportions of children *living*

Year.	Presidency.	Fathers.	Sons.	Daughters.
1856	Bengal -	1,664	1,430	1,590
1858	Madras -	1,133	1,389	1,471
		2,797	2,819	3,061

with fathers, and it hence appears that each married Officer will have two children for whom subscriptions will be constantly payable. With a view to safety, it will

be prudent to assume an average of two and a half children to each father.

20. The *average* amount of subscription to be derived from each unmarried Officer cannot be exactly computed, for the proportion of Officers in each grade of the Staff Corps is indeterminate. I had occasion to consider this subject in a memorandum on the Staff Corps Pension List, and I then submitted the following remarks :—

“The normal distribution of the Staff Corps, deduced from the Life Table,

“without regard to retirements is here shown. The  
 General Officers - 403 “effect of retirements would be to reduce the higher and  
 Lieutenant-Colonels - 423 Majors - 284 “to increase the lower ranks. For the purpose in  
 Captains - 469 Lieutenants - 921 Captains - 469  
 —————— 2,500 “view this distribution is therefore safe.” Here also  
 this distribution may serve, and it may be noted that, retirements, coupled with increase in the junior grades,  
 would have the effect of *reducing* the amount obtainable

from unmarried members. The full rates of subscription applied to the numbers above exhibited would yield an average of Rs. 10.88, say, Rs. 10, monthly for each unmarried Officer; but looking to the circumstances, it would be unwise to reckon on more than three-fourths of this amount. Accepting this as a fair conclusion, taking the married and single as numerically equal, and assigning  $2\frac{1}{2}$  children to each married Officer, the “rate in aid” will be Rs. 3, three rupees for each child, without distinction of sex. Allowing, however, that the claims of daughters will always exceed those of sons, because the latter go off at 21, while the former remain till marriage or death, the distribution may with sufficient caution, be made  $3\frac{1}{2}$  rupees for daughters and  $2\frac{1}{2}$  rupees for sons. These rates may, accordingly, be applied in relief of the family contributions.

21. In order that the monthly subscriptions for children may be kept within convenient bounds, it is further necessary to impose a small donation on the birth of each child. The amount may be fixed at will, under the sole condition that the donation and monthly subscription together shall be sufficient to provide the benefits promised to the child. As it is not intended that the family contributions shall be lowered during residence in Europe, I have supposed that donations of

Rs. 156 on the birth of a son, and of Rs. 250 on the birth of a daughter, will not be deemed excessive. To make them smaller than this would necessarily increase the monthly subscription, a result which I desire to avoid.

22. The scale of contributions for children may now be stated:—

	In India.		In Europe.	
	Birth Donation.	Monthly Subscription.	Birth Donation.	Monthly Subscription.
For Sons - - -	R. A. 156 0	R. A. 1 0	f s. d. 15 0 0	f s. d. 0 2 0
For Daughters - -	250 0	2 8	24 0 0	0 5 0

The details of the calculation are shown in the Appendix.. There is a small risk for posthumous children, which I have not overlooked, but it cannot be strictly estimated, and it does not seem to require any special provision.

23. Having thus far considered the adaptation of means to ends, with much fuller information than was available when the old Indian Service Funds were instituted ; guided, indeed, by the experience of those Funds, and warned by their

\* See para. 2. errors,—having also had careful regard to the important condition\* that, by the system of pensions herein set forth,

Government of India should not be put to any expense beyond that of the scale of pensions given in the British Army, I am enabled to express a reasonably confident opinion that the scheme proposed by Colonel Norman, from which I have not essentially deviated, may safely be carried out. I observe that it is very strongly recommended by the Government of India.

24. There are many matters of detail with which I am unwilling to burden this Report. They will be found in the Draft of Rules hereto appended.

25. The scheme includes the Medical and Clerical branches of the service. I have not found it needful to insist on any special scale of contributions for members of these classes, the scale being so graduated that it will meet all ordinary cases. Provision for exceptional cases should be made by requiring extra donations, rather than by special rates of subscription, whereby the accounts of Paymasters or other disbursing officers might be embarrassed.

26. It must here be noticed that the scheme, as proposed, does not include a grant of passage money to widows and orphans coming from India to England. In some cases it is probable that aid of this kind may be required, and I may mention two methods by which it could be provided. One way is, that an Officer might be permitted to effect a life assurance, the payment for which to be made at once or in a few instalments, the sum to be assured not exceeding Rs. 1,500, and the amount to be payable to his widow or his children on his decease. The other way is, that the Government should make the requisite advance, to be repaid by deductions from the pensions. The former is, I think, the preferable mode, and I have therefore supplied a Table, by which the value of an assurance may be calculated. The sum being small, the payment should be made in full within two years from the date of the policy ; the instalments in arrear bearing interest at  $4\frac{1}{2}$  per cent. As an instance, suppose an Officer, aged 35, wishes to secure Rs. 1,200, payable at his decease, he could effect this by an immediate payment of Rs. 486, or by instalments of about Rs. 21 monthly for

'two years. It is obvious that this provision can be most economically made at the earliest period, and it is further to be remarked that the values in the Table are not dependent on survivorship; the sum assured will, therefore, belong to the Officer's estate, under all circumstances.

27. I have, in para. 6, noticed the peculiar complexity of the calculations required in this case, and here, as due to the late Mr. Griffith Davies, I beg leave to offer some extracts from his last, and hitherto unpublished, letter on the Indian Funds.

" All of them were originally founded without much regard to calculations as " to the sufficiency of the contributions to provide for the claims that would " ultimately come upon them. \* \* \*

" I have had to investigate and report on the state of nearly all of " them. \* \* \*

" In making such investigations, I had but loose, indirect, and imperfect data, " and was obliged to devise modes of calculation that, to the best of my knowledge " and belief, had not been previously introduced into the calculation of life con- " tingencies, such as to embody the fraternal principle into the value of the " future contributions; to consider the members, their wives and children, " subject to different rates of mortality, and the females as subject to one rate of " mortality while residing in India, and to another rate after retirement to this " country as pensioners, and as subject to leave the Funds by marriage as well " as by death, and I had therefore to introduce all these elements into my " calculations."

28. The way thus cleared by Mr. Davies has been comparatively easy to his successors, and the data, though still incomplete, are greatly improved. I have been very anxious to establish the present scheme on a safe pecuniary basis, and to this end I have introduced a principle of some importance. The reduction of subscriptions paid in Europe is necessary, and the financial effect is considerable. Hitherto it has been assumed that the improvement of life by a change from tropical residence affords a sufficient compensation. I would, however, observe that the life table includes the home residents, and that consequently the apparent value of subscriptions payable in India is enhanced by this circumstance. I deem it very needful to provide against the foreseen reduction of subscriptions, and accordingly I have adjusted the payments to the supposition that from the age of 50 Officers will reside in Europe and contribute half rates only. The effect of this on the payments at the earlier ages is, as regards the individual Officer, inconsiderable, and to marriages at advanced ages it sets no real bar, for the required donations do not go beyond the probable means of the Officer. The pensions are on a moderate scale, and being only intended as safeguards from poverty, they should not, in extreme cases, become profitable investments, affording a cheap provision for young widows.

29. The stability of the scheme will depend on the adequacy of its resources. If it be self-supporting it will flourish, and will, to coming generations, prove a blessing. But how shall its condition at any time be known, for under a fair appearance there may be a worm at the root? I answer, by valuations to be made from time to time, and although it will not be at all needful that any special reserve or investment of money, as for the purposes of the institution, should be maintained, it will nevertheless be convenient and proper to have a

book account that will show the state of affairs. I do not, in fact, see how this could be omitted, for without it there could never be shown indisputable grounds for action in relation to the contributions on the one hand or to the benefits granted on the other, while it is desirable that the Government should exercise an absolute and clear-sighted control, having power to modify the scheme from time to time in accordance with the results of experience.

30. To effect a valuation certain data must be had. To procure and preserve such data, attention must be given, constant attention, not costly, not burdensome, the result useful always, and when for years patiently gathered, then of extreme value. Believing that if the scheme be carried out, so small a part of it as the keeping of necessary records will not be neglected, or rather that it will be, as I most earnestly recommend it may be, insisted on, I have given in the Appendix a Form of Register to be kept in some central office, either in India or in London. Similar subordinate registers should be kept in each Presidency, and a certified copy be sent periodically to the central office. To preserve uniformity, and as a material saving of time and labour, registers with printed headings might be prepared and supplied.

31. The extensive series of Tables hereto annexed will afford the solution of all technical questions that may arise, and I have only to express a hope that the calculations on which I have bestowed all the care in my power are such as may be trusted.

I have the honour to be,  
Sir,  
Your most obedient Servant,  
J. C. HANNYNGTON,  
Major General.

London, 7th June 1870.

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**APPENDIX.**

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"    for children ( <i>see Report, para. 22.</i> )	10
"    of unmarried officers ( <i>see Report, para. 15.</i> )	8
Symbols and formulæ	21

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## A P P E N D I X.

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No. 479 of 1868.

Separate.

Military Department.

To the Right Honourable the Secretary of State for India.

SIR,

We have the honour to forward Minutes by the Right Honourable the Governor General and the Honourable Colonel Norman on the subject of pensions to widows and orphans of officers entering the staff corps from the British Army, as well as of chaplains and medical officers under the new conditions of service.

2. We consider the necessity to secure a provision for the widows and orphans of the above officers to be most urgent, and we very earnestly recommend the proposals contained in the Minute of Colonel Norman to the favourable consideration of Her Majesty's Government.

We have, &c.,

(Signed) JOHN LAWRENCE.  
W. R. MANSFIELD.  
HENRY S. MAINE.  
J. STRACHEY.  
R. TEMPLE.  
H. W. NORMAN.

Fort William,  
The 14th December 1868.

Exd. M. Joseph.

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MINUTE by the Honourable Colonel H. W. NORMAN, C.B., on the subject of Pensions to Widows and Orphans of Officers entering the Staff Corps from the British Army, as well as of Chaplains and Medical Officers under the new conditions of service.

ONE of the measures resolved on in connexion with the abolition of a local army for India was the transfer of the several Military and Orphan Funds in the three presidencies to the Government, and their gradual winding up.

By these funds, which were maintained by donations and subscriptions from the officers of the army, aided by not very large subscriptions from Government, pensions were provided for widows and for orphans, and some other advantages given, such as passage money on certain occasions, an income allowance of £50 a year to subalterns on furlough, and an outfit allowance to a sick officer going home.

The advantages, and the rates of subscription, and the rules, differed in all the presidencies, but in all a fair provision was secured for widows and orphans, mainly from the proceeds of the subscription of the officers themselves.

When the Government took over the funds, all advantages were guaranteed to the existing subscribers, who continued, subject to the previous rules as to rates of subscription and donation; but as no new subscribers were to be admitted, the funds would gradually expire.

The Staff Corps is now recruited from the British army, and it has been laid down that in the case of all officers so appointed, their widows and families will be granted a pension "not less than that to which they would be entitled under the provisions of the Royal Warrant of June 15th, 1855."

In communicating this decision, the Secretary of State remarked that it remained "to be decided from what funds those pensions will be provided."

It seems pretty clear, however, that this new pension list will be a charge on the State, while the pensions to widows and orphans formerly given, though far more adequate than the new scale, cost the State only a comparatively small sum in the shape of an annual subscription to each fund.

Annexed are the statements showing the amount of donations and subscriptions paid by officers, under the old system, to the funds of the three presidencies, and of the pensions given to widows and orphans.

There is also attached a copy of the pension scale of the British army, which now will be applicable to the families of officers entering the Staff Corps.

These pensions are manifestly inadequate to the support of the widows and children of gentlemen, and in the case of the Royal army, to avoid the scandal of widows having to be privately aided, to enable them to return home, a Queen's Widows' Fund has been in existence for many years, formed from subscriptions of officers, from which fund grants of money are given to widows to enable them to defray all their expenses till they leave India, and to pay their passage home.

It seems most desirable that some fund should be re-constituted by which the widows and legitimate orphans of officers now entering the Staff Corps should be secured from poverty, as is now the case with the families of officers who belonged to the late Indian army, and of the Civil Service; and in any scheme of the kind medical officers and chaplains might be appropriately included, as they were under the former system, subscribing and receiving advantages, according to their relative rank, with combatant officers.

But, as an improvement on the old system, I think the fund should be entirely a Government institution, with a uniform scale of donations, subscriptions, and pensions for the three presidencies. No advantages beyond pensions to widows and orphans are now needed, as the present system of Furlough Regulations should render it unnecessary for officers to require the aid previously given by funds when they proceeded home.

Looking to the rates of pensions formerly given, and striking somewhere about the average of the three presidencies, I think the following would be a fair scale of pension for widows and orphans :—

	£
Widow of a colonel	240 a year.
"    " lieutenant-colonel	200 "
"    " major	160 "
"    " captain	120 "
"    " lieutenant	70 "
Orphan (male or female) under 5 years of age	24 "
Male orphan from 5 to 19 or any earlier age at which provided for	40 "
Female orphan from 5 until married	40 "

Under the old system a small marriage dower for girls, or apprentice fee for boys, was authorized, but this I think need not form a part of the new system.

I think if some such scale of pensions could be secured to the families of officers of the Staff Corps the respectability of the service would be increased, and the advantage of belonging to it more highly prized.

As I do not think Government need be put to more expense than a payment equivalent to the scale of pensions given in the British army to widows and orphans, I would suggest that the donations and subscriptions should be limited to such amount as might fairly meet the cost of the increase of pensions.

For those officers now in the Staff Corps who came from British regiments I would allow subscription or not to be optional, but I think it should be compulsory on all hereafter joining, as it used to be in the Indian army, and is now in the Civil Service.

As no officer who is not married could benefit by the fund I would require no donation from a bachelor joining the Staff Corps, or from a bachelor on promotion from one rank to another, and his subscription I think should not exceed half that of a married officer without children. From the married officer on joining the Staff Corps, or from a Staff Corps officer marrying, or a married officer on promotion, a donation might be exacted ; and besides double the subscription of the bachelor in each grade, I think a monthly subscription for each child eligible to the benefits of pension might be exacted, as is now the case with subscribers to the late Bengal Orphan Fund.

What should be the scale of pensions and donations is a matter for an actuary, and probably could only be soundly reported on at home, and anything I could devise on the subject would probably be incorrect ; but I think there would be no difficulty in doing this on the principles above proposed.

I would solicit the support of the Viceroy and of his Excellency's Council to the scheme I propose, or to some modification of it. The case of a chaplain's widow has already excited public attention, and necessitated a subscription on her behalf, and in a few years such cases will become numerous, and constant appeals come for charitable aid for widows and orphans left in a strange land with means utterly inadequate to support them. It was greatly to remedy this state of things that the old funds were established ; and as I do not ask for an expenditure of public money, but merely for an organized system under government control, by which officers shall subscribe the equivalent between the government rate of pensions and those on a higher, but still moderate scale, I should hope that Her Majesty's Government would view the proposal with favour.

Calcutta,  
The 4th December 1868.

H. W. NORMAN.

## I.

## STATEMENT of Donations paid by Subscribers to the Military Funds of the Three Presidencies.

	BENGAL.					MADRAS.					BOMBAY.						
	Married.		Unmarried.			Married.		Unmarried.			Married.		Widows with Offspring.		Unmarried.		
	On joining.	On promotion.	On joining.	On promotion.	On marriage.	On joining.	On promotion.	On joining.	On promotion.	On marriage.	On joining.	On promotion.	On joining.	On promotion.	On joining.	On promotion.	On marriage.
Colonels -	Rs. As. P. 4,550 0 0	Rs. As. P. 723 12 0	Rs. As. P. 787 8 0	Rs. As. P. 157 8 0	Rs. As. P. 3,912 8 0	Rs. As. P. 3,700 0 0	Rs. As. P. 1,100 0 0	Rs. As. P. 2,000 0 0	Rs. As. P. 550 0 0	Rs. As. P. *4,000 0 0	Rs. As. P. 6,000 0 0	Rs. As. P. 2,400 0 0	Rs. As. P. 2,250 0 0	Rs. As. P. 900 0 0	Rs. As. P. 1,500 0 0	Rs. As. P. 600 0 0	Rs. As. P. 4,500 0 0
Lieut.-Cols. -	2,501 0 0	642 8 0	630 0 0	157 8 0	2,151 4 0	2,600 0 0	800 0 0	1,450 0 0	400 0 0	2,900 0 0	3,600 0 0	800 0 0	1,350 0 0	300 0 0	900 0 0	200 0 0	2,700 0 0
Majors -	1,452 0 0	517 8 0	472 8 0	135 0 0	1,190 0 0	1,800 0 0	600 0 0	1,050 0 0	300 0 0	2,100 0 0	2,800 0 0	1,000 0 0	1,050 0 0	380 0 0	700 0 0	250 0 0	2,100 0 0
Captains -	695 0 0	455 0 0	837 8 0	135 0 0	507 9 0	1,200 0 0	500 0 0	750 0 0	250 0 0	1,500 0 0	1,800 0 0	600 0 0	670 0 0	320 0 0	450 0 0	150 0 0	1,850 0 0
Lieutenants -	450 0 0	150 0 0	202 8 0	67 8 0	225 0 0	700 0 0	400 0 0	500 0 0	200 0 0	1,000 0 0	1,200 0 0	400 0 0	450 0 0	150 0 0	300 0 0	100 0 0	900 0 0
Ensigns -	300 0 0	—	135 8 0	—	150 0 0	800 0 0	—	800 0 0	—	600 0 0	800 0 0	—	300 0 0	—	200 0 0	—	600 0 0

\* Marriage donations when the husband's age exceeds that of his wife by more than 8 years will be regulated by a disparity scale which became a rule in 1844.

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## II.

## STATEMENT of Monthly Subscriptions to the Military Fund at the Three Presidencies for Widows.

	BENGAL.				MADRAS.				BOMBAY.			
	Married.		Unmarried.		Married.		Unmarried.		Married.		Unmarried.	
	In India.	In Europe.	In India.	In Europe.	In India.	In Europe.	In India.	In Europe.	In India.	In Europe.	In India.	In Europe.
Colonels -	Rs. As. P. 62 8 0	£ s. d. 8 15 0	Rs. As. P. 28 2 0	£ s. d. 1 13 9	Rs. As. P. 63 13 3	£ s. d. 1 17 6	Rs. As. P. 42 8 10	£ s. d. 1 5 0	Rs. As. P. 64 8 0	£ s. d. 1 17 6	Rs. As. P. 43 0 0	£ s. d. 1 5 0
Lieut.-Colonels -	45 0 0	2 10 0	20 4 0	1 2 6	40 12 9	1 10 0	27 3 2	1 0 0	34 8 0	1 10 0	23 0 0	1 0 0
Majors -	35 0 0	2 0 0	15 12 0	0 18 0	31 9 3	1 4 0	21 0 10	0 16 0	27 12 0	1 4 0	18 8 0	0 16 0
Captains -	20 0 0	1 6 3	9 0 0	0 11 10	18 6 11	0 15 9	12 4 7	0 10 6	17 0 0	0 15 9	11 4 0	0 10 6
Lieutenants -	12 8 0	0 16 3	5 10 0	0 7 4	11 2 0	0 9 9	7 6 8	0 6 6	9 12 0	0 9 9	6 8 0	0 6 6
Ensigns -	10 0 0	0 13 2	4 8 0	0 5 11	8 14 11	0 7 11	5 15 3	0 5 3	7 8 0	0 7 10 1	5 0 0	0 5 3

## III.

## STATEMENT of Monthly Subscriptions to the Bengal Military Orphan Fund.

	Rs. As. P.	In addition.	Monthly. Ra. As. P.
Colonel	25 0 0	For each male child until he attains the age of 19 years.	
Lieutenant-Colonel	20 0 0		1 0 0
Major	15 0 0		
Captain	10 0 0	For each female child until marriage or death	
Lieutenant	6 4 0		3 0 0
Ensign	5 0 0		

MADRAS.—There is no separate subscription in Madras, but one rupee is payable for each child, whether son or daughter until 21 years, with a donation of rupees 282 for each daughter, if a claim to pension after 21 years of age be desired, to be secured.

BOMBAY.—No monthly subscription nor any payment for children, but a donation of rupees 200 for daughters, 100 for sons.

## IV.

## STATEMENT of the Annuities to widows of deceased Subscribers of the Military Fund of the three Presidencies.

	BENGAL.		MADRAS.		BOMBAY.	
	In India.	In England.	In India.	In England.	In India.	In England.
Colonel's widow	Rs. As. P.	£ s. d.	Rs. As. P.	£ s. d.	Rs. As. P.	£ s. d.
Colonel's widow	2,574 12 0	281 12 3	2,064 7 3	235 18 9	1,822 3 6	205 0 0
Lieutenant-Colonel's widow	2,059 13 0	225 5 9	1,826 9 0	208 15 0	1,555 8 10	175 0 0
Major's widow	1,546 13 0	168 19 3	1,588 10 9	181 11 3	1,288 14 2	145 0 0
Captain's widow	1,029 15 0	112 12 11	1,197 10 6	136 17 6	1,066 10 8	120 0 0
Lieutenant's widow	768 15 0	84 1 11	894 2 3	102 3 9	908 5 4	102 3 9
Ensign's widow	611 5 0	66 17 3	715 5 0	81 15 0	726 10 8	81 15 0

## V.

## STATEMENT of Annuities to children of Subscribers of the Military Orphan Fund of the Bengal Presidency.

	MALE.				FEMALE.				
	Under 5 years of Age.	From 5 to 19 years of age, or in a position to gain his own livelihood before them.	Under 6 years of age.	From 6 to 19 years of age.	Under 5 years of age.	From 5 till marriage or death.	Under 6 years of age.	From 6 to 18 years of age.	After 18 years of age.
In India	Rs. As. P.	Rs. As. P.	£ s. d.	£ s. d.	Rs. As. P.	Rs. As. P.	£ s. d.	£ s. d.	£ s. d.
In India	20 0 0	35 0 0	—	—	20 0 0	35 0 0	—	—	—
In England	—	—	30 0 0	40 0 0	—	—	30 0 0	45 0 0	35 0 0

MALE.—Apprentice fee or final grant in India rupees 500, if sanctioned by the general management.

FEMALE.—Marriage portion 150/- if in England, and rupees 1,500 if in India, if sanctioned by the general management.

## VI.

## STATEMENT of Annuities to children of deceased Subscribers of the Military Funds of the Madras and Bombay Presidencies.

	MADRAS.				BOMBAY.			
	Bereft of Father only.		Bereft of both Parents.		Bereft of Father only.		Bereft of both Parents.	
	In India.	In England.	In India.	In England.	In India.	In England.	In India.	In England.
Under { (Madras) 6 years of age - } (Bombay) 7 "	175 0 0	20 0 0	262 8 0	30 0 0	200 0 0	22 10 0	266 10 8	30 0 0
From { (Madras) 6 to 12 years of age } (Bombay) 7 to 10 "	262 8 0	30 0 0	393 12 0	45 0 0	266 10 8	30 0 0	400 0 0	45 0 0
From { (Madras) 12 to 21 } (Bombay) 10 to 18 "	350 0 0	40 0 0	525 0 0	60 0 0	333 5 4	37 10 0	533 5 4	60 0 0

SCALE referred to in the preceding Regulation.

RANK OF THE OFFICERS.	Widows ordinary pension.	Special pension in lieu of ordinary pension.		Allowance to the mother or sister of an officer killed in action.	Compassionate allowance to legitimate children.			Aggregate amount of allowances to the family of any one officer not to exceed.	
		To widows of officers dying from illness contracted in the field.	To widows of officers killed in action.		If the officer was killed in action.	If the officer died from illness contracted in the field.	If the officer was not killed in action, or did not die from illness contracted in the field.	If killed in action.	If not killed in action.
General Officer	£ 120	According to circumstances.	£ 120	25 to 40	£ 20 to 30	£ 16 to 20	£ 500	£ 300	
<b>REGIMENTAL OFFICERS.</b>									
Colonels not being also General Officers	100	£ 150	£ 200	100	18 to 25	16 to 20	14 to 16		
Lieutenant-Colonels } of the Foot Guards	90	145	200	90	18 to 25	16 to 20	14 to 16	350	
Majors	80	140	200	80	18 to 25	16 to 20	14 to 16		
Lieutenant-Colonels	70	100	130	70	16 to 20	14 to 17	12 to 14	250	
Majors	50	65	80	50	12 to 16	10 to 14	9 to 12	150	
Captains	40	50	60	40	8 to 14	6 to 12	5 to 10	100	
Paymasters									
Lieutenants									
Adjutants									
Second Lieutenants									
Cornets	36	40	46	36	8 to 14	6 to 12	5 to 10	80	
Ensigns									
Quarter Masters { under 10 years' service	36	40	46	36	8 to 14	6 to 12	5 to 10	80	
Quarter Masters { after 10 "	40	50	60	40	8 to 14	6 to 12	5 to 10	100	
Quarter Masters { after 20 "	50	65	80	50	12 to 16	10 to 14	9 to 12	150	
Veterinary Surgeons { under 10 years' service	40	50	60	40	8 to 14	6 to 12	5 to 10	80	
Veterinary Surgeons { after 10 "	45	55	70	45	8 to 14	6 to 12	5 to 10	100	
Veterinary Surgeons { after 20 "	55	70	80	55	12 to 16	10 to 14	9 to 12	150	
<b>MEDICAL OFFICERS.*</b>									
Inspectors General of Hospitals	100	150	200	100	18 to 25	16 to 20	14 to 16	350	
Deputy	80	140	200	80	18 to 25	16 to 20	14 to 16	350	
Staff Surgeons, 1st class "	70	100	130	70	16 to 20	14 to 17	12 to 14	250	
Surgeon Majors of the Regiments of Foot Guards									
Ditto, 2nd class, and Regimental Surgeon	50	65	80	50	12 to 16	10 to 14	9 to 12	150	
Purveyors, under 10 years	36	40	46	36	8 to 14	6 to 12	5 to 10	80	
Ditto after 10 "	40	50	60	40	8 to 14	6 to 12	5 to 10	100	
Ditto after 15 "	50	65	80	50	12 to 16	10 to 14	9 to 12	150	
Assistant Surgeons	40	50	60	40	8 to 14	6 to 12	5 to 10	100	
Chaplains to the Forces									
District Paymasters									
Provost Marshals, commissioned as such	50	65	80	50	12 to 16	10 to 14	9 to 12	150	
Other Staff or Garrison Officers		According to the Regimental Commissions which they held when placed on half-pay.							

C 2  
19  
Not exceeding the annual amount of the half-pay attached to the rank of the officer.

\* The widows of half-pay Medical Officers holding any commission giving a rank not included in the above scale may, if eligible, have the rates of pension specified in the scale annexed to the warrant of 13th June 1826.

## MINUTE by His Excellency the Right Honourable the Governor General.

I AM most strongly in favour of this proposal, and would urge it very strongly on the Secretary of State for India. It appears to me to be the duty of the Government to establish such funds, and insist on officers subscribing to them on entering the local service. Unless officers are compelled to subscribe for the future maintenance of their widows and children, this sacred duty will in many cases be neglected, and we shall constantly have instances of these relatives of officers, who have held honourable positions under the Government of India, seeking, and seeking even in vain, for assistance from the public. Such a state of things would, I submit, be derogatory to the service at large, and a grave scandal in the eyes of the natives of the country. On public grounds, therefore, as well as to prevent much misery and degradation hereafter to many helpless ladies and children, tenderly brought up, I strongly recommend the proposal for the support of my colleagues and the Secretary of State.

The 5th December 1868.

JOHN LAWRENCE.

I quite agree.

The 6th December 1868.

J. STRACHEY.

And I.

The 7th December 1868.

H. S. MAINE.

And I.

The 7th December 1868.

G. N. TAYLOR.

## MINUTE by the Honourable Sir R. TEMPLE, K.C.S.I.

I UNDERSTAND that a limited amount of widows' pension, according to the analogy of the British Service, is to be paid by the State; and that the remainder required to make up the amount to the old Indian scale is to be obtained by enforced subscriptions from the officers themselves. In the general principle, I cordially concur, as being essential to the efficiency and character of the future Staff Corps.

The 5th December 1868.

R. TEMPLE.

Exd. M. Joseph.

India Office, S.W.,  
25th February 1869.

Sir,  
I AM directed by the Secretary of State for India in Council to forward for your information, copy of a despatch from the Government of India, relating to a proposal to establish a system of Pensions for the benefit of Widows and Children of Officers of the several Staff Corps, and I am to request that, as soon as the work upon which you are now engaged shall have been completed, you will prepare and submit a full report upon the probable financial operation of Colonel Norman's proposal.

I have, &amp;c.

T. T. PEARS,

Major-General, Military Secretary.

Major-General Hannington.

London, 5th April 1869.

BEFORE entering on the money calculations respecting a system of Pensions for the benefit of Widows and Orphans of Officers in the Staff Corps, it is necessary to define the rates of interest and exchange that may be used without disadvantage to the Government or its officers.

I would respectfully suggest four and a half per cent. interest per annum, and one shilling and elevenpence for the rupee, as equitable rates, and I will adopt these if not otherwise instructed.

To Major-General Pears, C.B.,  
Military Secretary.

I have, &amp;c.

J. HANNINGTON.

India Office, S.W.,  
23d April 1869.

Sir,  
I AM directed by the Secretary of State for India in Council to acknowledge the receipt of your letter of the 5th instant, and to acquaint you in reply that you are authorised to adopt the rates therein proposed for interest and exchange in your calculations on the subject of the scheme for Pensions to Widows and Orphans of Officers entering the Staff Corps from the British Army, and of Chaplains and Medical Officers under the new conditions of service.

I have, &amp;c.,

T. T. PEARS,

Major-General, Military Secretary.

Major-General Hannington.

### Symbols and Formulae.

Person.		Age.		Number living at that Age.
Officer	-	$x$	-	$l_x$
Wife	-	$y$	-	$l_y$
Widow	-	$w$	-	$l_w$
Son	-	$-$	-	$l_s$
Daughter, unmarried	-	$u$	-	$l_u$

1.  $l_x - l_{x+1} = d_x$ ; the number of officers now aged  $x$ , who die in the next, or  $(x + 1)^{\text{th}}$  year.
2.  $\frac{l_y + l_{y+1}}{2} = l_{y+\frac{1}{2}}$ ; the number of wives now aged  $y$ , who live till the middle of the next, or  $(y + 1)^{\text{th}}$  year.
3.  $r$  = the rate of interest per cent. per annum.  
(In the calculations,  $r = .045$ .)
4.  $v^x = \frac{1}{(1+r)^x}$ ; the present value of a monetary unit to be received at the end of  $x$  years hence.
5.  $l_x v^x = D_x$
6.  $\sum (D_{x+1}) = N_x$ ; the sum of  $D_{x+1} + D_{x+2}$ , &c. to the end of life.
7.  $\frac{N_x}{D_x} = a_x$ ; the present value of a monetary unit, to be received at the end of each year of age during the existence of a life now aged  $x$ . This is called a life annuity.
8.  $l_x l_y v^y = D_{x,y}$ . Note. In the joint life formulae,  $v^y$  is used for convenience in the arithmetical operations.
9.  $\sum (D_{x,y+1}) = N_{x,y}$ ; the sum of  $D_{x,y+1} + D_{x,y+2}$ , &c., to the end of coexistent life.
10.  $\frac{N_{x,y}}{D_{x,y}} = a_{x,y}$ ; the present value of a monetary unit to be received at the end of each year during the coexistence of the lives now aged  $x$  and  $y$ . This is called a joint life annuity. It ceases on the failure of either life.
11.  $d_x l_{y+\frac{1}{2}} v^{y+\frac{1}{2}} a_{w+\frac{1}{2}} = D_{x,y}^{\frac{1}{2}}$ . Note.  $l_{y+\frac{1}{2}} v^{y+\frac{1}{2}} a_{w+\frac{1}{2}} = B_y$
12.  $\sum (D_{x,y}^{\frac{1}{2}}) = N_{x,y}^{\frac{1}{2}}$ ; the sum of  $D_{x,y}^{\frac{1}{2}} + D_{x,y+1}^{\frac{1}{2}} +$  &c., to the end of life.
13.  $\frac{N_{x,y}^{\frac{1}{2}}}{D_{x,y}^{\frac{1}{2}}} = a_{x,y}^{\frac{1}{2}}$ ; the present value of a monetary unit, to be received in the middle of each year, after the decease of a male, now aged  $x$ , and to continue during the widowhood of his wife now aged  $y$ . Payment ceases on re-marriage or death.
14.  $ma_{x,y}^{\frac{1}{2}}$  = the present value of a reversionary widowhood annuity of  $m$  units of money.
15.  $S(a_{x,y} + .458)$  = the present value of an annuity of  $S$  units of money payable in 12 equal portions during the year.
16. Equating the expressions 14 and 15, we have—  

$$m = \frac{S(a_{x,y} + .458)}{a_{x,y}^{\frac{1}{2}}}, \text{ and } S = \frac{ma_{x,y}^{\frac{1}{2}}}{a_{x,y} + .458}$$

17. If a donation or fine  $f$  be paid in reduction of  $S$ , then—

$$S = \frac{ma_{x,y}^2 - f}{a_{x,y} + .458}$$

18. When  $m$  and  $S$  are fixed, the fine  $f$  for disparity of age is,—

$$ma_{x,y}^2 - S(a_{x,y} + .458) = f.$$

19.  $a_u - a_{x+u}$  = the present value of an annuity, payable so long as a daughter now aged  $u$ , may live *unmarried* after the decease of her father now aged  $x$ .

20.  $S = \frac{m(a_u - a_{x+u})}{a_{x+u}}$ ; the amount of yearly subscription to be paid during the co-existence of the lives now aged  $x$  and  $u$  to provide a reversionary annuity  $m$ , payable to  $u$  while *unmarried* after the death of  $x$ .

21.  $S = \frac{m(a_u - a_{x+u}) - f}{a_{x+u}}$  = the same, supposing a fine  $f$ , to be paid at the beginning.

22. In the case of sons, let it be understood that the annuities are temporary,  $D_{21}$  being the limit of  $D_s$ , and  $D_{55+21}$  the limit of  $D_{x,s}$ ; then, putting  $s$  for  $u$ , the formulæ 20 and 21 will serve to determine the subscriptions to be paid for sons.

23. The addition to be made to a joint life annuity for monthly payments is in all cases  $0.458$ .

24. The present value at age  $x$  of an annuity to begin at a future age  $x+n$  is  $\frac{D_{x+n}a_{x+n}}{D_x} = {}^{ln}a_x$ , and the form holds when  $x \cdot y$  or  $\frac{2}{x \cdot y}$  is put for  $x$ .

25. The present value at age  $x$ , of an annuity which will be reduced to one half at the age  $x+n$ , is  $a_x - \frac{{}^{ln}a_x}{2}$ .

26. The present value of an annuity to begin at age  $x$  and continue till age  $x+n$  is  $\frac{N_x - N_{x+n}}{D_x} = {}^n a_x$ . This holds when  $x \cdot y$  or  $\frac{2}{x \cdot y}$  is put for  $x$ .

27. The present value of a monetary unit to be received on the death of a person now aged  $x$  is,  $v - (1-v)a_x = A_x$ .

Note on the Construction of the Tables.

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1. Nearly all of the calculations in this report have been effected on the "arithmometre" or calculating machine invented by M. Thomas de Colmar. As this machine is not yet known and appreciated as it deserves to be, and as it is necessary to explain some of the processes that I have used, the following details will not be deemed out of place.

2. Let it be understood that the machine will add or subtract numbers up to 1,000 millions; that it will multiply eight figures by eight figures, giving products up to sixteen figures; that it will divide sixteen figures by eight figures, giving the quotient to any extent; and all this without risk of error.

3. I had first occasion to compute a table of  $v^x$  from  $v^0$  to  $v^{100}$  at  $4\frac{1}{2}$  per cent. To effect this I had to compute by hand  $v^{10}$ ,  $v^{20}$ ,  $v^{30}$ , &c., each tenth value, to a large number of decimal places.

4. The machine gives  $v = \frac{1}{1.045} = 0.9569377990430622$ , and by tabulating the first nine multiples of this, it becomes easy to form  $v^2$ . Again tabulating we can form  $v^4$ ; from  $v^4$  we get  $v^8$ , and then  $v^8 \times v^2$  gives  $v^{10}$ . In precisely the same way we can obtain successively  $v^{20}$ ,  $v^{30}$ ,  $v^{40}$ , and so on. The values are in fact as follows:—

$$\begin{aligned}v^2 &= 0.91572995124 \\v^4 &= 0.83856134359 \\v^8 &= 0.70318512697 \\v^{10} &= 0.64392768203 \\v^{20} &= 0.41464285968 \\v^{30} &= 0.26700001551 \\v^{40} &= 0.17192870109 \\v^{50} &= 0.11070964997 \\v^{60} &= 0.07128900828 \\v^{70} &= 0.04590496586 \\v^{80} &= 0.02955947826 \\v^{90} &= 0.01903416316 \\v^{100} &= 0.01225662660\end{aligned}$$

5. The required table may now be completed in reverse order on the machine, by the formula—

$$v^{n-1} = v^n (1 \times r)$$

an extremely simple process.

6. This done, the next step is to form  $D_x = l_x v^x$ , to which end  $v^x$  is put on the machine, and is multiplied by  $l_x$ . The details pass off on the machine, and the values of  $D_x$  have only to be transcribed as they arise. The summation on the machine gives  $N_x$ , and then  $\frac{N_x}{D_x}$  gives  $a_x$ , the present value of an annuity on the life  $x$ .

7. It is here to be remarked that the last step is one of division, an operation that even on the machine is not nearly so facile as multiplication. I have therefore found it convenient to record  $D_x^{-1}$  from the table published by Lieut.-Col. W. H. Oakes, a work of great value, and to which, as will be seen, I am much indebted. Thus we have  $N_x D_x^{-1} = a_x$ , the product of two factors.

8. By a similar method any of the single life annuity tables may be formed.

9. The joint life tables might be formed in the same way, but although the machine does not err, the computer might in a multitude of *detached* operations commit errors that would elude notice. To prevent this it is always proper to devise continuous processes in which a single error induces a series of errors that cannot escape detection. For, at fixed points, independent values may be interposed, and when the continuous values agree with these, the work must be right, or a disagreement will disclose error to be then corrected.

10. It would be tedious further to explain the various arithmetical details. Suffice it to say that the values of  $D_{x,y}$  and  $D_{x,y}^{-\frac{1}{2}}$  for each 10th difference of age from -10 to +40 were independently computed on the machine to many places of figures. The intermediate values were constructed by continuous operations, and are certainly free from any material errors. However, to afford a means of verifying them by ordinary methods the logarithms of  $l_x$ ,  $D_y$ ,  $d_x$  and  $B_y$  are given.

11. I may observe that the symbol  $D_{x,y}$  is the product of three factors, and that commonly  $l_x v^x = D_x$  and  $l_y D_y = D_{x,y}$ . I have, however, used the form  $l_y v^y = D_y$  and  $l_x D_y = D_{x,y}$ . The reason of this departure from the usual practice is that the symbol  $D_{x,y}^{-\frac{1}{2}}$  is the product of four factors,  $d_x l_{y+\frac{1}{2}} v^{y+\frac{1}{2}} a_{w+\frac{1}{2}}$ , of which three, namely  $l_{y+\frac{1}{2}} v^{y+\frac{1}{2}} a_{w+\frac{1}{2}} = B_y$  can be formed once for all (since  $w = y$ ), thus affording the form  $d_x B_y = D_{x,y}^{-\frac{1}{2}}$  in which only  $B_y$  is partly fractional,  $d_x$  being an integer. By this arrangement the formula is better suited to the machine. Then in the form  $\frac{N_{x,y}^{-\frac{1}{2}}}{D_{x,y}^{-\frac{1}{2}}} = a_{w-y}^{-\frac{1}{2}}$ , because  $v^y$  is symmetrically involved, the final result is correct. Here also  $D_{x,y}^{-1}$  taken from Colonel Oakes's table of reciprocals has been of much use.

12. In the tables of  $D_{x,y}$  and  $D_{x,y}^{-\frac{1}{2}}$  the decimal point is noted, the quantities being, however, divided by 100, but in the summation  $N_{x,y}$  and  $N_{x,y}^{-\frac{1}{2}}$  the decimal point has been omitted, five figures being given without regard to their local value. In like manner the reciprocals are given as integers. This will not cause any real difficulty, and it saves much room. Suppose that in the table of equal ages it were desired to verify the annuity value for  $x = 40$ , then  $15392 \times 61436 = 94562$ , or supplying the decimal point  $9.4562$ . No other value could well be supposed. A glance at the *progression* of the quantities would resolve any doubt that might arise in other cases.

13. On the table for converting annuities into reversions I may remark that such tables were first published by the late Mr. Orchard. To compute them by help of the machine is very easy.

14. From the formula, No. 27., it appears that when  $a_x = 0$ , then  $A_x = v$ ; and when  $a_x = 1$  then  $A_x = v - (1 - v)$ . Hence by continually subtracting  $(1 - v) \times .001$  from  $v$ , the required table may be formed to any extent, each turn of the machine giving a new value. A record of these would occupy many pages, and abbreviation is therefore desirable.

15. When  $a_x = r$ , then  $A_x = 1 - r$ . In the present case  $r = .045$  and  $1 - r = .955$ . Thus we have a point at which there are no decimals beyond the third place. Again, when  $a_x = .254$  then  $A_x = .946$  exactly. We may now perceive that the fourth and following decimals are recurrent, and disappear at regular intervals. These intervals correspond with a difference of  $.254 - .045 = .209$  in  $a_x$ , and of  $.955 - .946 = .009$  in  $A_x$ , and we may notice that .209 is derived from  $2(1 + r)$ , and .009 from  $2r$ . Consequently the first part of the table may be formed by the continual addition of .209 in column  $a$ , and subtraction of .009 in column  $A_x$ . The second part of the table contains the 208 successive multiples of  $1 - v$  to a sufficient number of places.

16. I have explained the construction of this table at some length because the process may be useful in other cases.

17. The arrangement of the table is a good example of *packing*. Here in one page are 315 values, from which, in pairs only, we can readily form 22470 values.

18. The table for finding the addition to be made to an annuity when made payable half-yearly, and to the date of death, is constructed on similar principles, with differences of detail that need not here be shown.

19. The tables for exchanging pounds and rupees at 1s. 11d. the rupee, are peculiar in form, and they contain much in small compass.

**DATA AND ELEMENTARY TABLES.**

## LIFE TABLES. INDIAN MILITARY.

Age.	Officers.		Wives.		Till Death or Marriage.				Age.	Sons.		Age.	
					Widows.		Daughters.						
	$l_x$	$\Sigma(l_x)$	$l_y$	$\Sigma(l_y)$	$l_w$	$\Sigma(l_w)$	$l_u$	$\Sigma(l_u)$	$l_v$	$\Sigma(l_v)$			
0	-	-	-	-	-	-	-	-	100000	222142	0	100000	
1	-	-	-	-	-	-	-	-	86529	212242	1	85440	
2	-	-	-	-	-	-	-	-	81171	2035813	2	134456	
3	-	-	-	-	-	-	-	-	78299	1854428	3	130653	
4	-	-	-	-	-	-	-	-	76406	1876143	4	121106	
5	-	-	-	-	-	-	-	-	75055	1799737	5	1157423	
6	-	-	-	-	-	-	-	-	74059	1724083	6	71348	
7	-	-	-	-	-	-	-	-	73277	1650623	7	70816	
8	-	-	-	-	-	-	-	-	72812	1577346	8	69999	
9	-	-	-	-	-	-	-	-	72054	1504734	9	69434	
10	-	-	-	-	-	-	-	-	71577	1432680	10	68986	
11	-	-	-	-	-	-	-	-	71158	1381103	11	68458	
12	-	-	-	-	-	-	-	-	70777	1289045	12	68251	
13	100000	3554921	2293	93597	68894	1593599	70415	1919168	18717	674459	11	66981	
14	99833	3454921	2271	91304	68459	1524705	70058	1449758	14	67810	13	66494	
15	90411	3385088	2249	89033	67344	1456246	69892	1078955	15	67278	14	66500	
16	98737	3285677	2237	86784	65580	1388902	68988	1008693	16	66558	15	66479	
17	97815	3186940	2205	84557	62807	123342	64187	949815	17	66140	16	661517	
18	98670	3089125	2188	82352	61199	1205935	58599	876728	18	65987	17	65877	
19	95326	2932456	2161	80169	54680	1201336	53225	817769	19	65040	18	64990	
20	98809	2897129	2139	78008	50642	1146656	47569	764544	20	64630	19	64650	
21	92140	2803320	2117	75639	47065	1066014	42393	716975	21	64650	20	64650	
22	90353	2711180	2095	73752	43885	1048949	37836	674636	22				
23	88477	2620827	2073	71657	41087	1005064	33990	639900	23				
24	86544	2532350	2051	69584	38628	98977	30689	602820	24				
25	84584	24456306	2029	67633	36511	925355	27895	572131	25				
26	82626	2381222	2007	65504	34670	888444	25497	544248	26				
27	80695	2278596	1985	63497	32031	854174	23470	518749	27				
28	78788	2197901	1963	61512	31547	821143	21740	495279	28				
29	76903	2119113	1940	59549	30183	789596	20254	473639	29				
30	75039	2042210	1916	57699	28866	759413	18971	453235	30				
31	73183	1987171	1891	55693	27616	730547	17856	434314	31				
32	71365	1893978	1865	53902	26443	702831	16887	416458	32				
33	69559	1822613	1838	51987	25374	676488	16037	399671	33				
34	67780	1753054	1811	50069	24353	651114	15281	383534	34				
35	66031	1685274	1783	48288	23447	626761	14605	368258	35				
36	64317	1619243	1755	46505	22628	608314	13994	353648	36				
37	62440	1554926	1726	44750	21889	580866	13437	339654	37				
38	61001	1482286	1697	43024	21225	558797	12927	326217	38				
39	59399	1431285	1667	41327	20626	537572	12469	313290	39				
40	57934	1371886	1637	39680	20098	516844	12039	300831	40				
41	56306	1314052	1606	38023	19625	496348	11634	248801	41				
42	54815	1287746	1574	36417	19191	477233	11270	277165	42				
43	53359	1202931	1542	34843	18786	458032	10938	265805	43				
44	51936	1149572	1509	33801	18400	439246	10621	254968	44				
45	50546	1097636	1476	31792	18082	420846	10334	244342	45				
46	49184	1047091	1442	30316	17870	402814	10069	234008	46				
47	47852	997807	1408	28874	17365	385144	9824	223939	47				
48	46556	950055	1374	27466	16981	367899	9696	214115	48				
49	45303	903499	1340	26092	16543	350908	9382	204620	49				
50	44099	858196	1305	24752	16118	334365	9160	195138	50				
51	42949	814097	1270	23447	15672	318247	9038	185958	51				
52	41857	771148	1234	22177	15219	302575	8881	178926	52				
53	40809	739291	1198	20943	14772	287356	8729	168045	53				
54	39791	688483	1162	19745	14351	272584	8575	158516	54				
55	38792	648691	1126	18583	13919	258223	8406	150741	55				
56	37800	609599	1090	17457	13497	244314	8230	142335	56				
57	36806	572099	1054	16367	13098	230517	8049	134105	57				
58	35769	535293	1018	15313	12713	217725	7854	128059	58				
59	34769	493494	982	14295	12371	205012	7655	118205	59				
60	33708	464725	946	13313	12043	192641	74449	110550	60				
61	32608	431017	910	12367	11725	180598	7234	103101	61				
62	61464	398409	874	11457	11411	168873	7010	95867	62				
63	30277	366945	838	10583	11092	157462	6779	88857	63				
64	29048	336668	802	9745	10758	146370	6588	82078	64				
65	27780	307620	766	8943	10410	135612	6288	75540	65				
66	26477	2798440	730	8177	10047	125202	6030	69252	66				
67	25143	2533633	694	7447	9869	115155	5762	63223	67				
68	23778	228220	658	6753	9276	105486	5486	57460	68				
69	22385	204442	622	6095	8869	96201	5202	51974	69				
70	20968	182057	585	5473	8449	87341	4911	46772	70				
71	19533	161089	548	4988	8015	78892	4615	41861	71				
72	18688	141566	511	4540	7570	70877	4311	37248	72				
73	16638	1234488	474	3829	7114	63307	4005	32937	73				
74	15191	1068830	437	3355	6648	56193	3698	28932	74				
75	13756	91639	401	2918	6177	495456	3391	25234	75				
76	12345	77883	365	2517	5701	435388	3087	21843	76				
77	10970	65588	330	2152	5224	37667	2788	18756	77				
78	9446	54568	296	1822	4748	32443	2497	15968	78				
79	8386	44922	263	1526	4279	27695	2216	13471	79				
80	7203	365836	231	1283	3820	23416	1948	11255	80				
81	6107	293933	201	1082	3376	19596	1694	9307	81				
82	5105	232926	173	881	2951	16220	1457	7613	82				
83	4906	18120	145	659	2550	13269	1239	6156	83				
84	3410	13914	120	514	2178	10719	1040	4917	84				
85	2718	10504	97	394	1832	8543	862	3877	85				
86	2127	7786	77	297	1520	6711	704	3015	86				
87	1632	68659	60	220	1242	5191	568	2311	87				
88	1228	4027	46	160	997	3949	449	1746	88				
89	905	2799	35	114	786	2952	350	1296	89				
90	653	1894	26	79	608	2166	268	946	90				
91	460	1241	19	53	460	1558	201	678	91				
92	317	781	14	34	341	1098	148	477	92				
93	209	464	10	20	248	757	107	529	93				
94	129	255	6	10	176	509	76	222	94				
95	72	126	3	4</td									

The following hitherto unpublished Abstract of Data obtained from the officers of the Bengal Army in the year 1850 was prepared by the late Mr. Peter Hardy, F.R.S., Actuary to the London Assurance Corporation. It is worth preserving as an authentic contribution to the Statistics of Infant Life in India. The returns furnished by the officers included all their children, living and dead, with the dates of birth and death.

The number of lives of each sex which passed through each age from birth, and the number of deaths which happened at each age, embraced in the register transmitted with Major Hannington's letter, dated 29th July 1852.

Age.	Males.		Females.		Total.		Double of Total.	
	Living.	Dying.	Living.	Dying.	Living.	Dying.	Living	Dying.
0	1440	122	1420·5	110	2860·5	232	5721	464
1	1224	144	1213·5	129	2437·5	273	4875	546
2	991·5	58	990	62	1981·5	120	3963	240
3	867	21	844	30	1711	51	3422	102
4	779	9	740	7	1519	16	3038	32
5	709·5	6	668·5	7	1378	13	2756	26
6	650·5	2	601	3	1251·5	5	2503	10
7	591·5	5	543·5	4	1135	9	2270	18
8	531·5	2	492	2	1023·5	4	2047	8
9	478·	3	446	2	924	5	1848	10
10	431·5	2	399	1	830·5	3	1661	6
11	388	2	357	3	745	5	1490	10
12	345	3	318·5	1	663·5	4	1327	8
13	306	2	282	4	588	6	1176	12
14	269·5	1	244·5	1	514	2	1028	4
15	233·5	2	213	1	446·5	3	893	6
16	198·5	1	180·5	1	379	2	758	4
17	174	6	148·5	2	322·5	8	645	16
18	149·5	0	121·5	0	271	0	542	0
19	129	2	.97	0	226	2	452	4
20	109	1	74	0	183	1	366	2
21	92·5	0	56	0	148·5	0	297	0
22	81·5	0	44	0	125·5	0	251	0
23	71·5	0	37·5	1	109	1	218	2
24	59·5	0	26·5	0	86	0	172	0
25	49·5	2	20·	0	69·5	2	139	4
26	40·5	0	15·5	0	56	0	112	0
27	35·5	1	11·5	0	47	1	94	2
28	28	0	9	0	37	0	74	0
29	21·5	0	6·5	0	28	0	56	0
30	18·5	0	5	0	23·5	0	47	0
31	16	0	4·5	0	20·5	0	41	0
32	12·5	1	3·5	0	16	1	32	2
	11523	898	10634	871	22157	769	44314	1538

Unadjusted Life Table, deduced from the record of children born in India.

	Numbers that			Log $e$	Log $s$	Log $p_x$	Log $l_x$	$l_x$	$d_x$
	Enter.	Die.	Survive.						
0	5721	464	5257	3·7574719	3·7207380	1·9632661	5·0000000	100000	8110
1	4875	546	4329	6879746	6363876	1·9484130	4·9632661	91890	10292
2	3963	240	3723	5980241	5708930	1·9728689	9·116791	81598	4942
3	3423	102	3320	5342800	5211381	1·9868581	8·845480	76656	2285
4	3038	32	3006	4825878	4779890	1·9954012	8·714061	74371	783
5	2756	26	2730	4402792	4361626	1·9958834	8·668073	73588	694
6	2503	10	2493	3984608	3967223	1·9982615	8·626907	72894	291
7	2270	18	2252	3560259	3525684	1·9965425	8·609522	72603	576
8	2047	8	2039	3111178	3094172	1·9982994	8·574947	72027	282
9	1848	10	1838	2667020	2643455	1·9976435	8·557941	71745	388
10	1661	6	1655	2203696	2187980	1·9984284	8·534376	71357	258
11	1490	10	1480	1731863	1702617	1·9970754	8·518660	71099	477
12	1327	8	1319	1228709	1202448	1·9973739	8·489414	70622	426
13	1176	12	1164	0704073	0659530	1·9955457	8·463153	70196	716
14	1028	4	1024	3·0119931	0103000	1·9983069	8·418610	69480	270
15	893	6	887	3·9508515	9479236	1·9970721	8·401679	69210	465
16	758	4	754	8796692	8773713	1·9977021	8·372400	68745	363
17	645	16	629	8095597	7986506	1·9980909	8·349421	68382	1696
18							8·240330	66686	

Note.—The large number of deaths in the second year of age seems to indicate that some births have not been recorded. But from the completion of the first year of age, the table represents facts.

## INTEREST, FOUR AND A HALF PER CENT.

Present Value of £1 to be received any Number of Years hence.

Numbers.			Logarithms.		Numbers.			Logarithms.	
x	$v^x$	$v^{x+\frac{1}{2}}$	Log. $v^x$	Log. $v^{x+\frac{1}{2}}$	x	$v^x$	$v^{x+\frac{1}{2}}$	Log. $v^x$	Log. $v^{x+\frac{1}{2}}$
0	1.00000000	0.97799511	0.0000000	T.9903367	50	0.11070965	0.10827350	T.0441855	T.0345222
1	0.95693780	.93588049	T.9808837	9712204	1	.10594225	.10361100	0.250692	T.0154059
2	.91572995	.89557941	.9617674	9521041	2	.10138014	.09914928	T.0059329	T.9961896
3	.87629660	.85701379	.9426511	9329878	3	.09701449	.09487969	T.9868366	9771733
4	.83856184	.82010890	.9235348	9138715	4	.09283683	.09079396	9677203	9580570
5	.80245105	.78479320	.9044185	8947552	5	.08883907	.08688418	9486040	9389407
6	.76789574	.75099828	.8853023	8756389	6	.08501347	.08314276	9294877	9198244
7	.73482846	.71865864	.8661860	8565226	7	.08135260	.07956245	9105714	9007083
8	.70318513	.68771162	.8470697	8374064	8	.07784938	.07613631	8912551	8815919
9	.67290443	.65809724	.8279534	8182901	9	.07449701	.07285772	8721388	8624756
10	.64392768	.62975813	.8088371	7991738	60	.07128901	.06972030	8530226	8433593
1	.61619874	.60263935	.7897208	7800575	1	.06821915	.06671799	8339063	8242430
2	.58966386	.57668838	.7706045	7609412	2	.06528148	.06384497	8147900	8051267
3	.56427164	.55185491	.7514882	7418249	3	.06247032	.06109567	7956737	7860104
4	.53997287	.52809082	.7323719	7227086	4	.05978021	.05846475	7765574	7668941
5	.51672044	.50535006	.7132556	7035923	5	.05720594	.05594713	7574411	7477778
6	.49446932	.48358858	.6941393	6844760	6	.05474253	.05353792	7383248	7286615
7	.47317639	.46276419	.6750230	6653598	7	.05238519	.05123246	7192085	7095453
8	.45280037	.44283655	.6559067	6462435	8	.05012937	.04902628	7000922	6904290
9	.43380179	.42376703	.6367904	6271272	9	.04797069	.04691510	6809759	6713127
20	.41464286	.40551869	.6176742	6080109	70	.04591497	.04489484	6618596	6521964
1	.39678743	.38805617	.5985579	5888946	1	.04392820	.04296156	6427433	6330801
2	.37970089	.37134561	.5794416	5697783	2	.04203655	.04111155	6236271	6139638
3	.36335013	.35535465	.5603253	5506620	3	.04022637	.03934119	6045108	5948475
4	.34770347	.34005230	.54202090	5315457	4	.03849418	.03764707	5853945	5757312
5	.33273060	.32540890	.5220927	5124294	5	.03683649	.03602591	5662782	5566149
6	.31840249	.31139607	.5029764	4933131	6	.03525023	.03447456	5471619	5374986
7	.30469137	.29798667	.4838601	4741969	7	.03373228	.03299000	5280456	5183824
8	.29157069	.28515471	.4647438	4550806	8	.03227969	.03156937	5089293	4992661
9	.27901502	.27287532	.4456275	4359643	9	.03088965	.03020992	4898130	4801498
30	.26700001	.26112471	.4265113	4168480	80	.02955947	.02890902	4706968	4610335
1	.25550241	.24988010	.4073950	3977317	1	.02828658	.02766414	4515805	4419172
2	.24449991	.23911972	.3882787	3786154	2	.02706850	.02647286	4324642	4228009
3	.23397121	.22882280	.3691624	3594991	3	.02590287	.02533288	4133479	4036846
4	.22389589	.21896909	.3500461	3403828	4	.02478744	.02424199	3942316	3845683
5	.21425444	.20953979	.3309298	3212665	5	.02372003	.02319808	3751153	3654520
6	.20502817	.20051655	.3118135	3021502	6	.02269860	.02219912	3559990	3463357
7	.19619921	.19188187	.2926672	2830340	7	.02172115	.02124318	3368827	3272195
8	.18775044	.18361901	.2735809	2639177	8	.02078579	.02032839	3177664	3081033
9	.17966549	.17571197	.2544646	2448014	9	.01989070	.01945301	2986501	2889869
40	.17192870	.16814543	.2353484	2256851	90	.01903417	.01861532	2795339	2698706
1	.16452507	.16090472	.2162321	2065688	1	.01821451	.01781371	2604176	2507543
2	.15744026	.15397581	.1971158	1874525	2	.01743016	.01704661	2413013	2316380
3	.15066054	.14734527	.1779995	1683362	3	.01667958	.01631255	2221850	2155217
4	.14417276	.14100296	.1588832	1492199	4	.01596132	.01561009	2030687	1934054
5	.13796437	.13492848	.1397669	1301036	5	.01527399	.01493789	1839524	1742891
6	.13202332	.12911816	.1206506	1109873	6	.01461626	.01429463	1648361	1551728
7	.12533810	.12355805	.1015343	0918711	7	.01398685	.01367907	1457198	1360566
8	.12089771	.11823736	.0824180	0727348	8	.01338454	.01309001	1266035	1169403
9	.11569158	.11314580	.0633017	0536385	9	.01280817	.01252634	1074872	0978240
					100	.01225663		T.0883710	T.0787077

NOTE.— $v^{x+\frac{1}{2}}$  is  $v^x \times \frac{1}{1-0225}$ .

TABLE for converting ANNUITIES into REVERSIONS, i.e., sums payable on decease.  
Interest Four and a Half per Cent.

$a_x$	$A_x$	$a_x$	$A_x$	$a_x$	$A_x$	$a_x$	$A_x$
0·045	.955	5·688	.712	11·331	.469	16·974	.226
0·254	.946	5·897	.703	11·540	.460	17·183	.217
0·463	.937	6·106	.694	11·749	.451	17·392	.208
0·672	.928	6·315	.685	11·958	.442	17·601	.199
0·881	.919	6·524	.676	12·167	.433	17·810	.190
1·090	.910	6·733	.667	12·376	.424	18·019	.181
1·299	.901	6·942	.658	12·585	.415	18·238	.172
1·508	.892	7·151	.649	12·794	.406	18·457	.163
1·717	.883	7·360	.640	13·003	.397	18·646	.154
1·926	.874	7·569	.631	12·212	.388	18·855	.145
2·135	.865	7·778	.622	13·421	.379	19·064	.136
2·344	.856	7·987	.613	13·630	.370	19·273	.127
2·553	.847	8·196	.604	13·839	.361	19·482	.118
2·762	.838	8·405	.595	14·048	.352	19·691	.109
2·971	.829	8·614	.586	14·257	.343	19·900	.100
3·180	.820	8·823	.577	14·466	.334	20·109	.091
3·389	.811	9·032	.568	14·675	.325	20·318	.082
3·598	.802	9·241	.558	14·884	.316	20·527	.073
3·807	.793	9·450	.550	15·093	.307	20·736	.064
4·016	.784	9·659	.541	15·302	.298	20·945	.055
4·225	.775	9·868	.532	15·511	.289	21·154	.046
4·434	.766	10·077	.523	15·720	.280	21·363	.037
4·643	.757	10·286	.514	15·929	.271	21·572	.028
4·852	.748	10·495	.505	16·138	.262	21·781	.019
5·061	.739	10·704	.496	16·347	.253	21·990	.010
5·270	.730	10·913	.487	16·556	.244	22·199	.001
5·479	.721	11·122	.478	16·765	.235		

THIRD AND FOLLOWING FIGURES OF  $A_x$ .

$A_x$	0.	1.	2.	3.	4.	5.	6.	7.	8.	9.
·00	0 0000	0431	0861	1292	1722	2153	2584	3014	3445	8876
·01	0 4306	4737	5167	5598	6029	6459	6890	7330	7751	8182
·02	0 8612	9043	9474	9904	*0335	*0766	*1196	*1627	*2057	*2488
·03	1 2919	3349	3780	4211	4641	5072	5502	5933	6364	6794
·04	1 7225	7656	8086	8517	8947	9378	9809	*0239	*0670	*1100
·05	2 1531	1962	2392	2823	3254	3684	3116	4545	4976	5407
·06	2 5837	6268	6699	7129	7560	7990	8421	8852	9282	9713
·07	3 0144	0574	1005	1435	1866	2297	2727	3158	3589	4019
·08	3 4450	4880	5311	5742	6172	6603	7033	7464	7895	8325
·09	3 8756	9187	9617	*0048	*0478	*0909	*1340	*1770	*2201	*2632
·10	4 3062	3493	3923	4354	4785	5215	5646	6077	6507	6938
·11	4 7368	7799	8230	8660	9091	9521	9952	0382	0813	1244
·12	5 1675	2105	2536	2967	3397	3828	4258	4689	5120	5550
·13	5 5981	6411	6842	7272	7703	8134	8565	8995	9426	8856
·14	6 0287	0718	1148	1579	2010	2440	2871	.3301	3732	4163
·15	6 4593	5024	5455	5885	6316	6746	7177	7608	8038	8469
·16	6 8900	9330	9761	*0191	*0622	*1053	*1483	*1914	*2344	*2775
·17	7 3206	3636	4067	4498	4928	5359	5789	6220	6651	7081
·18	7 7512	7943	8373	8804	9234	9665	*0096	*0526	*0957	*1388
·19	8 1818	2249	2679	3110	3541	3971	4402	4833	5263	5694
·20	8 6124	6555	6986	7416	7847	8277	8708	9139	9569	

Note.—The first figure in Column 0 is common to all the columns, and the asterisk shows that this leading figure is to be taken from the line next below. Thus, for example, the value for ·024 is 1 0335.

Find in Column  $a_x$  the value *next above* that of the given annuity, and note the difference. Then, to the value of  $A_x$  so found in the upper part of the Table, *add* the value for the difference, as found in the lower part of the Table. For example,—

$$\begin{aligned} \text{Given annuity } a_x &= 13\cdot475 \\ \text{Next above } - &- 13\cdot630 \quad .370 \\ \text{Difference } - &- 155 \quad 66746 \\ \text{Corresponding value of } A_x &= - \quad \underline{\underline{.3766746}} \end{aligned}$$

INTEREST BEING  $4\frac{1}{2}$  PER CENT.

Table showing the Addition to Annuities when made payable half yearly and to the day of Decease.

Annuities.	Addition.								
0·045	·494	4·045	·450	8·044	·406	12·043	·362	16·042	·318
·136	·493	135	·449	135	·405	134	·361	138	·317
·227	·492	226	·448	225	·404	225	·360	224	·316
·318	·491	317	·447	316	·403	315	·359	315	·315
·409	·490	408	·446	407	·402	406	·358	405	·314
·500	·489	499	·445	498	·401	497	·357	496	·313
·591	·488	590	·444	589	·400	588	·356	587	·312
·682	·487	681	·443	680	·399	679	·355	678	·311
·773	·486	772	·442	771	·398	770	·354	769	·310
·863	·485	863	·441	862	·397	861	·353	860	·309
·954	·484	953	·440	952	·396	951	·352	951	·308
1·045	·483	5·044	·439	9·043	·395	13·043	·351	17·042	·307
·136	·482	135	·438	134	·394	133	·350	133	·306
·227	·481	226	·437	225	·393	224	·349	223	·305
·318	·480	317	·436	316	·392	315	·348	314	·304
·409	·479	408	·435	407	·391	406	·347	405	·303
·500	·478	499	·434	498	·390	497	·346	496	·302
·591	·477	590	·433	589	·389	588	·345	587	·301
·682	·476	681	·432	680	·388	679	·344	678	·300
·773	·475	771	·431	771	·387	770	·343	769	·299
·863	·474	862	·430	861	·386	861	·342	860	·298
·954	·473	953	·429	952	·385	951	·341	951	·297
2·045	·472	6·044	·428	10·043	·384	14·042	·340	18·041	·296
·136	·471	135	·427	134	·383	133	·339	132	·295
·227	·470	226	·426	225	·382	224	·338	223	·294
·318	·469	317	·425	316	·381	315	·337	314	·293
·409	·468	408	·424	407	·380	406	·336	405	·292
·499	·467	499	·423	498	·379	497	·335	496	·291
·590	·466	589	·422	589	·378	588	·334	587	·290
·681	·465	680	·421	679	·377	679	·333	678	·289
·772	·464	771	·420	770	·376	769	·332	769	·288
·863	·463	862	·419	861	·375	860	·331	859	·287
·954	·462	953	·418	952	·374	951	·330	950	·286
3·045	·461	7·044	·417	11·043	·373	15·042	·329	19·041	·285
·136	·460	135	·416	134	·372	133	·328	132	·284
·227	·459	226	·415	225	·371	224	·327	223	·283
·317	·458	317	·414	316	·370	315	·326	314	·282
·408	·457	407	·413	407	·369	406	·325	405	·281
·499	·456	498	·412	497	·368	497	·324	496	·280
·590	·455	589	·411	588	·367	587	·323	587	·279
·681	·454	680	·410	679	·366	678	·322	677	·278
·772	·453	771	·409	770	·365	769	·321	768	·277
·863	·452	862	·408	861	·364	860	·320	859	·276
·954	·451	953	·407	952	·363	951	·319	950	·275

To use the Table.—Find in the table the annuity nearest in value to the proposed annuity, and take out the quantity opposite thereto. Add this to the proposed annuity.

Example.—Suppose the given annuity to be worth 10·325 years' purchase. Then in the table the nearest value is 10·316, opposite to which is the addition ·381, therefore  $10·325 + .381 = 10·706$  is the augmented value, as required.

## EXCHANGE TABLE.—Pounds into Rupees, at 1s. 11d.

						For Pounds + Rupees.	—	For Shillings. + Rupees.	—	For Pence. + Rupees.	Fractional Equivalents.	
Rs.	Rs.	Rs.	Rs.	Rs.	Rs.					Decimals.	Annas. Pies.	
0	240	480	720	960								
2	23	46	69	92	0·00000	0	0·00000	0	0·00000	·000	0 0	
1	24	47	70	93	10·43478	1	0·5217	1	0·0434	·043	0 8	
2	25	48	71	94	20·86956	2	1·0434	2	0·0869	·086	1 5	
3	26	49	72	95	31·30434	3	1·5652	3	0·1304	·130	2 1	
4	27	50	73	96	41·73913	4	2·0869	4	0·1739	·173	2 9	
5	28	51	74	97	52·17391	5	2·6086	5	0·2173	·217	3 6	
6	29	52	75	98	62·60869	6	3·1304	6	0·2608	·260	4 2	
7	30	53	76	99	73·04347	7	3·6521	7	0·3043	·304	4 10	
8	31	54	77		83·47826	8	4·1739	8	0·3478	·347	5 7	
9	32	55	78		93·91304	9	4·6956	9	0·3913	·391	6 3	
10	33	56	79		104·34782	10	5·2175	10	0·4347	·434	6 11	
11	34	57	80		114·78260	11	5·7391	11	0·4782	·478	7 8	
12	35	58	81		125·21739	12	6·2608			·521	8 4	
13	36	59	82		135·65217	13	6·7826			·565	9 1	
14	37	60	83		146·08695	14	7·3043			·608	9 9	
15	38	61	84		156·52173	15	7·8260			·652	10 5	
16	39	62	85		166·95652	16	8·3478			·695	11 2	
17	40	63	86		177·39130	17	8·8695			·739	11 10	
18	41	64	87		187·82608	18	9·3913			·782	12 6	
19	42	65	88		198·26086	19	9·9130			·826	13 3	
20	43	66	89		208·69565					·869	13 11	
21	44	67	90		219·13043					·913	14 7	
22	45	68	91		229·56521					·956	15 4	

To use the Table.—Find the Pounds in one of the columns headed Pounds, then will the sum of the numbers at the top and in the margin express the value in Rupees.

Example :—

Required the equivalent of 73l.—Here, 720 + 41·739 = Rs. 761. 11. 10.

Required the equivalent of 730l.—Here, 7200 + 417·391 = Rs. 7,617. 6. 3.

Required the equivalent of 15l. 11s. 7d.—Here, 15l. = 156·522

$$\begin{array}{rcl} 11s. & = & 5\cdot739 \\ 10d. & = & 0\cdot304 \end{array}$$

$$161\cdot565 = \text{Rs. } 161. 9. 1.$$

Note.—The value of the decimals in annas and pies will always be found in the small table of fractional equivalents

## EXCHANGE.—Rupees into Pounds, at 1s. 11d.

£	£	£	£	£	£	£	£	£	£	+	£
0·0	2·3	4·6	6·9	9·2	11·5	13·8	16·1	18·4	20·7	Annas.	
Rs.	Rs.	Rs.	Rs.	Rs.	Rs.	Rs.	Rs.	Rs.	Rs.		
0	24	48	72	96	120	144	168	192	216	0·00000	
1	25	49	73	97	121	145	169	193	217	0·09583	
2	26	50	74	98	122	146	170	194	218	0·19166	
3	27	51	75	99	123	147	171	195	219	0·28750	
4	28	52	76	100	124	148	172	196	220	0·38333	1 ·0060
5	29	53	77	101	125	149	173	197	221	0·47916	2 ·0120
6	30	54	78	102	126	150	174	198	222	0·57500	3 ·0180
7	31	55	79	103	127	151	175	199	223	0·67083	4 ·0240
8	32	56	80	104	128	152	176	200	224	0·76666	5 ·0299
9	33	57	81	105	129	153	177	201	225	0·86250	6 ·0359
10	34	58	82	106	130	154	178	202	226	0·95833	7 ·0419
11	35	59	83	107	131	155	179	203	227	1·05416	8 ·0479
12	36	60	84	108	132	156	180	204	228	1·15000	9 ·0539
13	37	61	85	109	133	157	181	205	229	1·24583	10 ·0599
14	38	62	86	110	134	158	182	206	230	1·34166	11 ·0659
15	39	63	87	111	135	159	183	207	231	1·43750	12 ·0719
16	40	64	88	112	136	160	184	208	232	1·53333	13 ·0779
17	41	65	89	113	137	161	185	209	233	1·62916	14 ·0839
18	42	66	90	114	138	162	186	210	234	1·72500	15 ·0898
19	43	67	91	115	139	163	187	211	235	1·82083	Note.—The value of one pie is ·0005 very nearly.
20	44	68	92	116	140	164	188	212	236	1·91666	
21	45	69	93	117	141	165	189	213	237	2·01250	
22	46	70	94	118	142	166	190	214	238	2·10833	
23	47	71	95	119	143	167	191	215	239	2·20416	

To use the Table.—Find the Rupees in one of the columns headed Rupees, then will the sum of the numbers at the top and in the margin express the value in Pounds.

Example :—

Required the equivalent of Rs. 761. 11. 10,—

$$\text{Rs. } 760 = 69$$

$$+ 3·8333$$

$$, 1 = 0·0958$$

$$\text{As. } 11 = 0·0659$$

$$\text{Pies } 10 = 0·005$$

$$\underline{\underline{\text{£73·0000}}}$$

TABLE SHOWING THE RATE OF MARRIAGE. From the Fourteenth Annual Report of the Registrar General, page viii.

ENGLAND.—Number of Bachelors, Spinsters, Widowers, and Widows, at different Ages, who were enumerated; also the Proportions who were married in the Year 1851.

Age.	Numbers enumerated in 1851.				Estimated Numbers married in 1851. (See note.)				Proportion married to 100 living.			
	Bachelors.	Spinsters.	Widowers.	Widows.	Bachelors.	Spinsters.	Widowers.	Widows.	Bachelors.	Spinsters.	Widowers.	Widows.
Total -	2297759	2306009	333926	661894	132643	140331	21563	13875	5·773	6·085	6·457	2·096
15	869325	861453	76	260	4035	18807	—	13	·464	2·183	—	—
20	633842	598732	2168	4326	71049	75872	667	850	11·209	12·672	30·766	5·000
25	308363	306607	8290	14303	37647	29136	2967	2132	12·209	9·503	35·790	19·649
30	159956	163604	14249	26328	12558	9857	4079	3057	7·851	6·025	28·627	14·906
35	95889	99443	18584	34839	4371	3759	3775	2527	4·558	3·780	20·313	11·611
40	67380	71520	24576	49207	1885	1789	3459	2132	2·798	2·501	14·075	7·253
45	47522	51044	27172	54868	688	724	2407	1466	1·448	1·418	8·858	4·333
50	37155	43102	34057	70033	262	258	1945	909	·705	·599	5·711	2·672
55	25815	30823	32586	67181	90	96	1043	491	·349	·311	3·201	1·298
60	21649	29550	41725	88283	33	25	728	213	·152	·085	1·745	·731
65	13055	19319	37567	77698	19	5	324	53	·146	·026	·862	·241
70	9629	15217	39284	74625	3	—	124	19	·031	—	·316	·068
75	5068	8837	28139	52527	3	—	28	8	·059	—	·100	·025
80 and upwards.	3111	6758	25453	47416	—	3	17	5	—	·044	·067	·011

The Table may be read thus:—Of the persons enumerated in 1851, of the age of 20 and under 25, there were 633,842 Bachelors, 598,732 Spinsters, 2,168 Widowers, and 4,326 Widows, while the numbers who were married during the same year and of the same ages were respectively 71,049, 75,972, 667, and 850, being in the proportion of 11·209 Bachelors, 12·672 Spinsters, 30·766 Widowers, and 19·649 Widows married to every 100 living, and so on at other ages. By disregarding the decimal point, the proportions to 10,000 will be represented.

Note.—Of the total number of marriages solemnized in 1851, the ages of the Males and Females were stated only of the following numbers, viz., 48,555 Bachelors, 51,141 Spinsters, 7,792 Widowers, and 5,206 Widows. In this Table these numbers have been proportionally raised to the total numbers married under these respective headings.

London,

26th February 1870.

My dear Dr. Farr,

Having occasion to make a practical application of the rate of marriage among spinsters, I some time since mentioned the matter to you, and you have kindly placed in my hands the Fourteenth Report of the Registrar-General, where, in p. viii, a table (V. c.) is given to show approximately the rate of marriage at different ages for bachelors, spinsters, widowers, and widows.

Of these rates that for spinsters is considerably the lowest. For this class I have supplied the intermediate years by interpolation with differences to the fourth order, and the result is a well graduated scale, which I send herewith.

The benefits derived from the several Funds established in India terminate on remarriage. It has, therefore, been necessary to ascertain the rate of marriage for this class. Investigations on scant data were made by the late Mr. Griffith Davies, by Mr. Neison, and by Mr. Samuel Brown. I have entered some of the results in the table, and you will observe that they are much below the British spinsters' rate. One reason for this may be that the loss of pension restricts marriage.

Comparing the British spinsters and the Indian widows' marriage rates, it seems reasonable to ask whether the widows' rate could fairly be applied to the class for whom I am at present concerned, namely, the daughters of Indian Officers, and if not, how far could the British spinsters' rate be held applicable?

The forfeiture of pensions on marriage has not the same restrictive effect on spinsters as on widows. The pensions are small, and besides this, many daughters marry in their father's lifetime, when their interest in the pension is only reversionary.

It is noticeable that in the Table V. c., the rate of marriage of widows greatly exceeds that of first marriages, but if the British spinsters' rate be compared with the Indian widows' rate, the reverse of this obtains.

Perhaps a safe rate, following the same law of progression as the spinsters' rate, may be deduced by taking an uniform percentage from the British table. Thus, at the age of 20, deducting one-fifth, the marriage rate would become 10·118 per cent. as a maximum, instead of 12·672, and so throughout. Even thus, I find that there would be a wide departure from the Indian widows' rate.

The question is important, and its determination will affect large pecuniary intérêts. Safety is on either hand advantageous, but the exaction of an over-high premium, when only safety and not profit is sought, would be unjust.

In a conflict of data, the leaning must ever be to the largest and most authentic body of facts. That the census of 1851, with its 2,306,009 spinsters and 140,331 marriages, is more to be relied on, than an experience drawn from 635 widows and 119 remarriages, is not open to dispute. But the smaller experience, as applicable to a class, has much weight. I am therefore disposed to reduce the British rate for the purpose in hand.

How far such a reduction should be carried must partly rest on opinion. I submit the subject to you because I have your permission to do so, and because I rely on your judgment.

With sincere apologies for this trespass on your time and attention,

I am, &c.,

(Signed) J. HANNYNGTON.

W. Farr, Esq., M.D.

General Register Office, Somerset House,

7th March 1870.

My dear General Hannyngton,

I have read your paper and the table interpolated, which you have had the goodness to send me. The subject is most difficult, as you are dealing with a class in peculiar conditions, and the observations at your disposal are limited.

Your view appears to be judicious. You take into account all the data relating to the class, and the estimate of the best authorities, and then, after reasoning on probable results, you turn to account the experience of the whole nation in fixing the quota of marriage at the several ages. You must, I imagine, assume that your widows will marry at a slower rate than our spinsters, although in England widows marry more frequently than spinsters. But widows have often fortunes or perquisites, which tempt, while your widows, losing income, may be deterred from marriage, or deter future husbands.

It is a special case. But I know you have given the subject so much thought that I should be quite willing myself to act on your decision.

At the end of every five years you will naturally investigate the progress, and should take power to alter the scheme in accordance with the results of experience.

I am, &c.,  
(Signed) WILLIAM FARR.

DIFFERENCES FOR INTERPOLATION. MARRIAGES PER CENT., SPINSTERS. DATA FROM  
14TH REPORT OF THE REGISTRAR GENERAL.

	+ Δ₁	- Δ₂	+ Δ₃	- Δ₄
2183	+	10489	-	13658 + 13349 - 11807
12672	-	3169	-	309 + 1542 - 1809
9503	-	3478	+	1233 - 267 - 503
6025	-	2245	+	966 - 770 + 838
3780	-	1279	+	196 + 68 + 199
2501	-	1083	+	264 + 267 - 736
1418	-	819	+	531 - 469
599	-	288	+	62
311	-	226		
		85		

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	+ Δ₁	- Δ₂	+ Δ₃	- Δ₄	Military Officers' Widows.
	.2	.08	.048	.0336	S. Brown:
	.4	.12	.064	.0416	Bengal,
	.6	.12	.056	.0336	Madras,
	.8	.08	.032	.0176	Bombay.
					—
15				2.183	10.69
	+ 10489	+	4228	6.411	
	+ 13658		7180	9.363	
	+ 13349		9077	11.260	
	+ 11807		10119	12.302	6.849
20	.			12.672	7.10
	- 3169	-	474	12.198	
	+ 309		1059	11.615	
	+ 1542		1717	10.955	
	+ 1809		2429	10.243	5.102
25				9.503	4.88
	- 3478	-	790	8.713	
	- 1233		1535	7.968	
	- 267		2233	7.270	
	+ 503		2881	6.622	3.329
30				6.025	3.20
	- 2245	-	591	5.434	
	- 966		1098	4.927	
	- 770		1534	4.491	
	- 838		1913	4.112	2.857
35				3.780	1.68
	- 1279	-	275	3.505	
	- 196		539	3.241	
	+ 68		794	2.986	
	- 199		1040	2.740	1.653
40				2.501	0.90
	- 1083	-	200	2.301	
	- 214		417	2.084	
	+ 267		642	1.859	
	+ 736		866	1.635	0.802
45				1.418	0.91
	+ 819	+	617	1.216	
	- 264		441	1.040	
	- 68		257	.856	
	- 838	+	111	.710	0.877
50				.599	.67

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## ELEMENTS FOR COMPUTING THE DURATION OF UNMARRIED LIFE. FEMALES.

Age.	1.	2.	3.	4.	5.	6.	7.	
	Living.	Dying.	Proportions Marrying.	(3)+(4) $1-p_u$	$p_u$	Log $p_u$		
15	.99445	.00555	.01746	.02301	.97699	9898901		
6	400	.00600	.05129	.05729	.94271	9743781		
7	345	.00655	.07490	.08145	.91855	9531028		
8	282	.00718	.09008	.09726	.90274	9555627		
9	214	.00786	.09842	.10628	.89372	9512015		
20	144	.00856	.00137	.10993	.89007	9494242		
1	121	.00879	.09758	.10637	.89363	9511577		
2	100	.00900	.09292	.10192	.89808	9533150		
3	079	.00921	.08764	.09685	.90315	9557599		
4	059	.00941	.08194	.09135	.90865	9583966		
5	039	.00961	.07602	.08563	.91437	9611220		
6	019	.00981	.06970	.07951	.92049	9640191		
7	000	.01000	.06374	.07374	.92626	9667329		
8	.98981	.01019	.05816	.06835	.93165	9692528		
9	962	.01038	.05297	.06335	.93665	9715773		
30	943	.01057	.04820	.05877	.94123	9736958		
1	924	.01076	.04347	.05423	.94577	9757855		
2	904	.01096	.03942	.05038	.94962	9775499		
3	884	.01116	.03593	.04709	.95291	9790519		
4	863	.01137	.03290	.04427	.95573	9803352		
5	842	.01158	.03024	.04182	.95818	9814471		
6	820	.01180	.02804	.03984	.96016	9823436		
7	797	.01203	.02593	.03796	.96204	9831931		
8	774	.01226	.02389	.03615	.96385	9840095		
9	749	.01251	.02192	.03443	.96557	9847838		
40	728	.01277	.02001	.03278	.96722	9855253		
1	696	.01304	.01841	.03145	.96855	9861220		
2	668	.01332	.01667	.02999	.97001	9867762		
3	638	.01362	.01487	.02849	.97151	9874473		
4	606	.01394	.01308	.02702	.97298	9881039		
5	573	.01427	.01134	.02561	.97439	9887328		
6	558	.01462	.00973	.02435	.97565	9892940		
7	502	.01498	.00832	.02330	.97670	9897612		
8	463	.01537	.00685	.02222	.97778	9902411		
9	422	.01578	.00568	.02146	.97854	9905786		

## DERIVED FROM ENGLISH LIFE TABLE. NO. 3. FEMALES.

With the Rate of Marriage reduced by one fifth, from 14th Report of Registrar General.

	Log $p_u$	Log $l_u$		Log $p_u$	Log $l_u$		Log $p_u$	Log $l_u$
0	1.9371604	6.0000000	40	1.9855258	5.0802771	80	1.9394234	4.2894835
1	9722410	5.9371604	1	9861220	0658024	1	9346135	2289069
2	9843554	9094014	2	9867762	0519244	2	9294933	1635204
3	9893710	8937568	3	9874473	0387006	3	9240517	0930137
4	9922523	8831278	4	9881039	0261479	4	9182778	4.0170654
5	9941950	8753801	5	9887328	0142518	5	9121607	3.9353432
6	9953928	8695751	6	9892940	5.0029846	6	9056896	9475039
7	9960392	8649679	7	9897613	4.9922786	7	8988532	7531935
8	9966496	8610071	8	9902411	9820398	8	8916408	6520467
9	9971161	8576567	9	9905786	9722809	9	8840415	5436875
10	9974514	8547728	50	9929018	9628595	90	8760443	4277290
1	9976674	8522242	1	9927015	9557613	1	8676383	3037733
2	9977764	8498916	2	9924906	9484628	2	8588123	1714113
3	9977906	8476680	3	9922685	9409534	5	8495557	3.0302239
4	9977224	8454586	4	9918715	9332219	4	8398575	2.8797796
5	9898901	8431810	5	9907919	9245934	5	8297066	7196371
6	9743781	8330711	6	9901864	9153853	6	8190921	5493437
7	9631028	8074492	7	9895440	9055717	7	8080033	3684358
8	9555627	7705520	8	9888536	8951157	8	7964288	2.1764391
9	9512015	7261197	9	9881047	8839693	9	7843582	1.9728679
20	9494242	6773212	60	9872859	8720740	100	7717801	7572261
1	9511577	6267454	1	9863865	8593599	1	7586838	5290062
2	9533150	5779031	2	9853955	8457464	2	7450583	3876900
3	9557599	5312181	3	9843019	8311419	3	7308927	0327483
4	9583996	4869780	4	9830950	8154438	4	7161761	0.7636410
5	9611220	4453776	5	9817635	7985388	5	7008974	4798171
6	9640191	4064996	6	9802967	7803023	6	6850457	1807145
7	9667329	3705187	7	9786837	7605990	7	6686102	1.8657602
8	9692528	3372516	8	9769134	7392827	8	1.6515799	5343704
9	9715773	3065044	9	9749749	7161961			1859503
30	9736958	2780817	70	9728573	6911710			
1	9757855	2517775	1	9705496	6640283			
2	9775499	2275630	2	9680410	6345779			
3	9790519	2051129	3	9653205	6026189			
4	9803352	1841648	4	9623770	5679394			
5	9814471	1645000	5	9591998	5303164			
6	9823436	1459471	6	9557777	4895162			
7	9831931	1282907	7	9521001	4452939			
8	9840095	1114838	8	9481557	3973940			
9	9847838	5.0954933	9	9439338	4.3455497			

LOGARITHMS FOR COMPUTING  $D_{x \cdot y}$  AND  $D_{x \cdot y}^{-\frac{1}{2}}$ .

$x$ or $y$	Log. $I_x$	Log. $D_y$	Log. $d_x$	Log. $B_y$	Numbers.	
					$d_x$	$B_y$
15		3.0652451		4.0681829		11699.920
6		0418395		0371105		10892.071
7		3.0184316		4.0125905		10294.173
8	4.9852917	2.9949604	3.1283993	3.9962777	1344	9914.657
9	9792114	9714452	1809856	9845847	1517	9631.2728
20	4.9722445	2.9478850	3.2224563	3.9725715	1669	9387.9656
1	9644682	9242788	2521246	9600950	1787	9122.1032
2	9559426	9006256	2732328	9469881	1876	8850.9147
3	9468304	8769246	2862319	9329509	1933	8569.4095
4	9372370	8531747	2922561	9174886	1960	8269.6776
5	9272882	8293747	2918127	9004430	1958	7951.0233
6	9171167	8055238	2857823	8821412	1931	7623.2690
7	9068466	7816206	2803507	8631058	1907	7296.3516
8	8964601	7576641	2753114	8433381	1885	6971.6905
9	8859433	7334292	2704459	8243275	1864	6673.0981
30	4.8752870	2.7089063	3.2662317	3.8041409	1846	6370.0213
1	8644695	6840865	2619762	7825890	1828	6061.6226
2	8534853	6596556	2567177	7619667	1806	5780.5171
3	8423533	6335079	2501759	7404723	1779	5501.3909
4	8311016	6079646	2427898	7185212	1749	5230.2359
5	8197479	5820811	2340108	6954180	1714	4959.2729
6	8083258	5560906	2245331	6713483	1677	4691.8946
7	7968517	5297380	2145790	6457805	1639	4423.6476
8	7853370	5032627	2046625	6193692	1602	4161.6426
9	7737791	4764002	1945143	5915014	1565	3903.9246
40	4.7621832	2.4493971	3.1842134	3.5623218	1528	8650.2437
1	7505547	4219776	1734776	5314582	1491	3399.8378
2	7388994	3941205	1631614	4996387	1456	3159.6478
3	7272077	3660839	1532049	4666837	1423	2928.7594
4	7154685	3375724	1433271	4332293	1391	2711.6231
5	7036782	3088533	1338581	3984411	1361	2502.8869
6	6918238	2796159	1245042	3631690	1332	2307.6452
7	6799001	2501370	1126050	3273923	1296	2125.1627
8	6679757	2204047	0979511	2914096	1253	1956.1832
9	6561270	1904065	0806265	2553800	1204	1800.0301
50	4.6444287	2.1597960	3.0606978	3.2198756	1150	1659.1116
1	6329531	1288729	0382226	1837129	1092	1526.5567
2	6217681	0972681	0203613	1470642	1048	1403.0207
3	6107560	0652934	3.0077478	1096021	1018	1287.0692
4	5997849	0329264	2.9995655	0714789	999	1178.9052
5	5887422	2.0001424	9965117	3.0328148	992	1078.4867
6	5774918	1.9669142	2.99733864	2.9931456	994	984.34112
7	5659186	9332120	3.0030295	9520578	1007	895.48367
8	5538709	8990029	0128372	9091046	1030	811.15625
9	5411822	8642503	0257154	8641285	1061	731.35539
60	4.5277330	1.8289137	3.0413927	2.8174589	1100	656.83887
1	5133242	7929477	0584260	7691010	1144	587.62593
2	4978139	7563014	0744507	7190617	1187	523.66866
3	4811128	7189177	0895519	6676530	1229	465.21421
4	4631162	6807318	1031193	6148733	1268	411.97720
5	4437322	6416699	1149444	5606992	1303	363.66303
6	4228688	6016477	1251558	5050070	1334	319.89465
7	4004171	5605680	1351327	4476552	1365	280.32064
8	3761753	5183181	1439511	3885365	1393	244.64507
9	3499571	4747663	1513699	3267492	1417	212.20186
70	4.3215570	1.4290155	3.1568519	2.2635340	1435	183.45606
1	2907690	3815239	158678	1963908	1445	157.17765
2	2573905	3320480	1613680	1281932	1450	134.33624
3	2211011	2802891	1604685	120552905	1447	113.57702
4	1811184	2258750	1568519	1'9808476	1435	95.68581
5	1384922	1694226	1495270	9026423	1411	79.91755
6	0914911	1094548	1383027	8213315	1375	66.27226
7	4.0402066	1.0465595	1218880	735351	1324	54.36571
8	3.9843473	0.9802210	1003705	6449680	1260	44.15377
9	9235549	9097687	0729847	5512741	1183	35.58556
80	3.8575134	0.8343088	3.0398106	1.4518730	1096	28.30563
1	7858279	7547766	3.0004341	3479337	1001	29.28095
2	7080808	6679926	2.9542425	2329689	900	17.09893
3	6238693	5747159	9009131	1.1161440	796	13.06604
4	5327544	4734128	8401061	0.9834857	692	9.62688
5	4342495	3618870	7715871	8470494	591	7.03152
6	3277675	2424897	6946052	7034355	495	5.05167
7	2127202	0.1150340	6063814	5459283	404	3.51502
8	3.0891984	1.9805242	5092025	3808676	323	2.40363
9	2.9566486	8427181	4014005	2271963	252	1.68731
90	2.8149132	1.6945072	2.2855573	0.0360305	193	1.086502
1	6627578	5391712	1553360	1.8819138	143	761928
2	5010593	3874293	2.0334238	6873962	108	486851
3	3201463	1.2221850	1.9030900	4674080	80	293365
4	2.1105897	1.9812200	7558749	1.1111863	57	132186
5	1.8573325	6610737	5682017	1.7702260	37	058915
6	1.5440680	1.1648361	3222193	1.1101385	21	025773
7	1.1461280	1.0000000	1.0000000		10	
8	0.6020600	0.4771213	0.4771213		3	
9	0.0000000	0.0000000	0.0000000		1	

NOTE.— $\log. I_x + \log. D_y = \log. D_{x \cdot y}$ ; and  $\log. d_x + \log. B_y = \log. D_{x \cdot y}^{-\frac{1}{2}}$ ; the logarithms of the whole series, for every value of  $x$  and  $y$  may be derived from these, they are given here to afford a ready means of verifying the values that have been

**A N N U I T I E S,**  
**SINGLE LIFE, JOINT LIVES, REVERSIONARY;**  
**WITH SUBSIDIARY CALCULATIONS.**

INDIAN ARMY OFFICERS.—ANNUITIES AND ASSURANCES,  $4\frac{1}{2}$  PER CENT.

$x$	$D_x$	$N_x$	$D_x^{-1}$	$a_x$	$A_x$
18	4377·22	61989·67	22845	14·162	·347091
19	4130·67	57859·00	24209	14·007	·353766
20	3889·76	53969·24	25709	13·875	·359450
21	3659·00	50310·24	27337	13·753	·364703
22	3430·60	46879·64	29149	13·665	·368493
23	3214·92	43664·72	31105	13·582	·372067
24	3009·03	40655·69	33233	13·511	·375124
25	2814·23	37841·46	35534	13·447	·377880
26	2630·96	35210·50	38009	13·383	·380636
27	2458·86	32751·64	40669	13·319	·383392
28	2297·29	30454·35	43529	13·256	·386105
29	2145·62	28308·73	46607	13·194	·388775
30	2003·57	26305·16	49911	13·129	·391574
31	1870·02	24435·14	53475	13·067	·394244
32	1745·00	22690·14	57307	13·003	·397000
33	1627·50	21062·64	61444	12·942	·399627
34	1517·57	19545·07	65895	12·879	·402340
35	1414·72	18130·35	70685	12·815	·405096
36	1318·74	16811·61	75830	12·748	·407981
37	1228·99	15582·62	81368	12·679	·410952
38	1145·28	14437·34	87315	12·608	·414096
39	1067·21	13370·128	93702	12·528	·417455
40	994·264	12375·864	10058	12·448	·420900
41	926·441	11449·423	10794	12·359	·424732
42	863·088	10586·835	11586	12·265	·428780
43	803·924	9782·411	12439	12·168	·432957
44	748·833	9033·578	13354	12·063	·437478
45	697·410	8336·168	14339	11·953	·442215
46	649·291	7686·877	15401	11·839	·447124
47	604·628	7082·349	16542	11·716	·452421
48	562·900	6519·449	17765	11·582	·458191
49	524·083	5995·366	19081	11·440	·464306
50	488·229	5507·137	20482	11·280	·471196
51	455·022	5052·115	21077	11·103	·478818
52	424·377	4627·738	23564	10·905	·487344
53	395·916	4231·822	25258	10·689	·496646
54	369·398	3862·424	27071	10·456	·506679
55	344·607	3517·817	29018	10·208	·517359
56	321·851	3196·466	31119	9·947	·528598
57	299·459	2897·007	33393	9·674	·540354
58	278·701	2618·306	35881	9·395	·552368
59	259·026	2359·280	38606	9·108	·564727
60	240·815	2118·965	41612	8·817	·577258
61	222·463	1896·502	44951	8·525	·589833
62	205·376	1691·126	48691	8·234	·602364
63	189·160	1501·966	52865	7·940	·615024
64	173·661	1328·305	57583	7·649	·627555
65	158·918	1169·387	62926	7·358	·640086
66	144·958	1024·429	68985	7·067	
67	131·696	892·733	75932	6·779	
68	119·208	773·525	83887	6·489	
69	107·406	666·119	93105	6·202	
70	96·263	569·856	10388	5·920	
71	85·792	484·064	11656	5·642	
72	76·044	408·020	13150	5·365	
73	66·937	341·083	14939	5·095	
74	58·472	282·611	17102	4·833	
75	50·687	231·924	19729	4·576	
76	43·534	188·390	22971	4·328	
77	37·004	151·386	27024	4·091	
78	31·150	120·236	32103	3·860	
79	25·916	94·320	38586	3·639	
80	21·283	73·037	46986	3·432	
81	17·283	55·754	57860	3·226	
82	13·832	41·922	72296	3·031	
83	10·905	31·017	91701	2·844	
84	8·452	22·565	11832	2·670	
85	6·452	16·113	15499	2·497	
86	4·835	11·278	20683	2·333	
87	3·541	7·737	28241	2·185	
88	2·557	5·180	39108	2·026	
89	1·810	3·370	55249	1·862	
90	1·237	2·133	80841	1·724	
91	0·8379	1·2950	11935	1·546	
92	·5578	0·7372	17928	1·322	
93	·3503	0·3869	28547	1·104	
94	·2075	0·1794	48193	0·865	
95	·1069	0·0725	93545	0·678	
96	·0585	0·0140	17094	0·239	
97	·0140	0·0000			

## ANNUITIES—SINGLE LIVES, WIDOWS, 4½ PER CENT.

<i>w</i>	<i>l<sub>w</sub></i>	<i>D<sub>w</sub></i>	<i>N<sub>w</sub></i>	<i>a<sub>w</sub></i>	$\frac{1+R}{4}$	Pensions.
15	67344	34798·02	351090·86	10·089	384	10·473
6	65560	32417·41	318673·45	9·830	386	10·216
7	62807	29718·79	288954·66	9·723	388	10·111
8	59199	26805·33	262149·33	9·780	387	10·167
9	54680	23692·94	238456·39	10·064	384	10·448
20	50642	20998·34	217458·05	10·356	381	10·737
1	47065	18674·80	198783·25	10·644	377	11·021
2	43885	16663·17	182120·08	10·929	374	11·303
3	41087	14928·97	167191·11	11·199	371	11·570
4	38622	13429·00	153762·11	11·450	369	11·819
5	86511	12148·32	141613·78	11·657	366	12·023
6	84670	11039·01	130574·77	11·828	364	12·192
7	83031	10064·26	120510·511	11·974	363	12·337
8	81547	9198·181	111312·330	12·110	361	12·471
9	80183	8421·510	102890·820	12·218	360	12·578
30	28866	7707·222	95183·598	12·432	358	12·790
1	27616	7055·955	88127·643	12·490	357	12·847
2	26443	6465·311	81662·332	12·631	355	12·986
3	25354	5932·106	75730·226	12·766	354	13·120
4	24353	5452·537	70277·689	12·889	353	13·242
5	23447	5023·624	65254·065	12·989	352	13·341
6	22628	4639·377	60614·688	13·065	351	13·416
7	21889	4294·605	56320·083	13·114	350	13·464
8	21225	3985·003	52335·080	13·133	350	13·483
9	20626	3705·780	48629·300	13·123	350	13·473
40	20098	3455·423	45173·877	13·073	351	13·424
1	19625	3228·804	41945·073	12·991	352	13·343
2	19191	3021·436	38923·637	12·882	353	13·235
3	18786	2830·309	36693·328	12·752	354	13·106
4	18400	2652·779	33440·549	12·606	356	12·962
5	18032	2487·774	30952·775	12·442	357	12·799
6	17670	2332·852	28619·923	12·268	360	12·628
7	17305	2186·281	26433·642	12·091	363	12·453
8	16931	2046·919	24386·723	11·914	363	12·277
9	16543	1913·886	22472·837	11·742	365	12·107
50	16118	1784·418	20688·419	11·594	367	11·961
1	15672	1660·327	19028·092	11·464	368	11·832
2	15219	1542·904	17485·188	11·333	370	11·703
3	14772	1433·098	16052·090	11·200	371	11·571
4	14351	1332·301	14719·789	11·048	373	11·421
5	13919	1236·551	13483·238	10·904	374	11·278
6	13497	1147·427	12335·811	10·751	376	11·127
7	13092	1065·068	11270·743	10·582	378	10·960
8	12713	989·6992	10281·0442	10·388	380	10·768
9	12371	921·6025	9359·4417	10·156	383	10·539
60	12043	858·5335	8500·9082	9·902	385	10·287
1	11725	799·8695	7701·0387	9·628	389	10·017
2	11411	744·9270	6956·1117	9·388	392	9·730
3	11092	692·9208	6263·1909	9·039	395	9·434
4	10758	643·1155	5620·0754	8·739	398	9·137
5	10410	595·5138	5024·5616	8·437	402	8·839
6	10047	549·9982	4474·6634	8·136	405	8·541
7	9669	506·5124	3968·0510	7·834	408	8·242
8	9276	465·0000	3503·0510	7·533	412	7·945
9	8869	425·4520	3077·5990	7·234	415	7·649
70	8449	387·8511	2689·7479	6·935	418	7·353
1	8015	352·0845	2337·6634	6·639	422	7·061
2	7570	818·2167	2019·4467	6·346	425	6·771
3	7114	286·1704	1733·2763	6·057	428	6·485
4	6648	255·9090	1477·3673	5·773	431	6·204
5	6177	227·5390	1249·8283	5·493	434	5·927
6	5701	200·9616	1048·8667	5·219	437	5·656
7	5224	176·2174	872·6493	4·952	440	5·392
8	4748	153·2640	719·3853	4·694	443	5·137
9	4279	132·1768	587·2085	4·443	446	4·889
80	3820	112·9172	474·39131	4·200	448	4·648
1	3376	95·49549	378·79583	3·967	451	4·418
2	2951	79·87914	298·91668	3·742	453	4·195
3	2550	66·05232	232·86436	3·525	456	3·981
4	2176	53·93747	178·92689	3·317	458	3·775
5	1832	43·45509	135·47180	3·118	460	3·578
6	1520	34·50187	100·96993	2·927	462	3·389
7	1242	26·97767	73·99226	2·743	464	3·207
8	997	20·72343	53·26883	2·570	466	3·036
9	786	15·63409	37·63474	2·407	468	2·875
90	608	11·57278	26·06196	2·252	470	2·722
1	460	8·37867	17·68329	2·111	472	2·583
2	341	5·94368	11·73961	1·975	473	2·448
3	248	4·13654	7·60307	1·838	474	2·312
4	176	2·80919	4·79388	1·707	476	2·183
5	122	1·86343	2·93045	1·573	477	2·050
6	83	1·21315	1·71730	1·415	479	1·894
7	55	0·76928	·94802	1·232	481	1·713
8	36	·48184	·46618	0·967	484	1·451
9	23	·29459	·17159	0·582	488	1·070
100	14	·17159	·00000	0·000	495	0·495

## WIDOWS TILL REMARRIAGE OR DECEASE. MEAN VALUES.

Age. W.	Pension. $a_{w+\frac{1}{2}}$	Logarithms.	Age. W.	Pension. $a_{w+\frac{1}{2}}$	Logarithms.
15 to 16	10.345	1.0147305	58 to 59	10.654	1.0275127
16 " 17	10.164	1.0070647	59 " 60	10.413	1.0175759
17 " 18	10.189	1.0059951			
18 " 19	10.308	1.0131744	60 " 61	10.152	1.0065516
19 " 20	10.593	1.0250190	61 " 62	9.874	0.9944931
20 " 21	10.879	1.0365890	62 " 63	9.582	0.9814562
21 " 22	11.162	1.0477420	63 " 64	9.286	0.9678287
22 " 23	11.437	1.0583121	64 " 65	8.988	0.9536631
23 " 24	11.695	1.0680002	65 " 66	8.690	0.9390198
24 " 25	11.921	1.0763127	66 " 67	8.392	0.9218655
25 " 26	12.108	1.0830724	67 " 68	8.094	0.9081632
26 " 27	12.265	1.0886676	68 " 69	7.797	0.8919275
27 " 28	12.404	1.0935618	69 " 70	7.501	0.8751192
28 " 29	12.525	1.0977777	70 " 71	7.207	0.8577545
29 " 30	12.684	1.1032362	71 " 72	6.916	0.8398550
30 " 31	12.819	1.1078541	72 " 73	6.628	0.8213825
31 " 32	12.917	1.1111617	73 " 74	6.345	0.8024316
32 " 33	13.053	1.11157103	74 " 75	6.066	0.7829024
33 " 34	13.181	1.1199484	75 " 76	5.792	0.7628286
34 " 35	13.292	1.1235903	76 " 77	5.524	0.7422537
35 " 36	13.379	1.1264237	77 " 78	5.265	0.7213984
36 " 37	13.440	1.1283993	78 " 79	5.013	0.7000977
37 " 38	13.474	1.1294965	79 " 80	4.769	0.6784273
38 " 39	13.478	1.1296255	80 " 81	4.533	0.6563857
39 " 40	13.449	1.1286900	81 " 82	4.307	0.6341749
40 " 41	13.384	1.1265859	82 " 83	4.088	0.6115109
41 " 42	13.289	1.1234923	83 " 84	3.878	0.5886078
42 " 43	13.171	1.1196187	84 " 85	3.677	0.5654936
43 " 44	13.034	1.11150777	85 " 86	3.484	0.5420781
44 " 45	12.881	1.1099496	86 " 87	3.298	0.5182507
45 " 46	12.714	1.1042822	87 " 88	3.122	0.4944329
46 " 47	12.542	1.0983668	88 " 89	2.956	0.4707044
47 " 48	12.365	1.0921941	89 " 90	2.798	0.4408477
48 " 49	12.192	1.0860750	90 " 91	2.653	0.4237372
49 " 50			91 " 92	2.516	0.4007106
50 " 51	12.034	1.0804100	92 " 93	2.380	0.3765770
51 " 52	11.897	1.0754375	93 " 94	2.248	0.3517963
52 " 53	11.768	1.0707027	94 " 95	2.117	0.3257209
53 " 54	11.637	1.0658410	95 " 96	1.972	0.2949069
54 " 55	11.496	1.0605468	96 " 97	1.803	0.2559957
55 " 56	11.350	1.0549959	97 " 98	1.582	0.1992065
56 " 57	11.203	1.0493343	98 " 99	1.260	0.1003705
57 " 58	11.044	1.0431264	99 " 100	0.782	0.8932068
	10.864	1.0359898	100 " 101	0.247	0.3926970

N.B.—This table is to be used for the valuation of the pensions of incumbent widows.

EXTENDED VALUES OF  $D_{x,y}$  FORMED BY ACTUAL MULTIPLICATION OF THE FACTORS  $I_x$  AND  $D_y$  ON THE ARITHMOMETER. From these the intermediate values for each difference of age were computed on the machine by a continuous process, and verified at each tenth interval.

(INTEREST  $4\frac{1}{2}$  PER CENT.)

$x$	$y = x + 10$	$y = x$	$y = x - 10$	$y = x - 20$	$y = x - 30$	Diff.	The initial values of $D_{x,y}$ for each difference of Age.
18	553293935	955547375					
9	515989247	892599491				-10	553293935
20	479900577	832011615				9	584672147
1	445179109	773975079				8	617753974
2	412665462	718734081				7	652629224
3	380485695	666430706				6	689392245
4	350914717	617179709				5	728142414
5	323124160	571035381	982954301			4	768984136
6	297308509	528008068	909863631			3	812027033
7	273265387	489053366	841934430			2	857386627
8	251028417	450945718	778790386			1	905184239
9	230326331	416267557	720092930				
30	211195239	383878513	665536724			+0	955547375
1	193395888	853635712	614820468			1	1008610215
2	176850320	825942367	567689592			2	1064513799
3	161598495	299130897	523935639			3	1123406227
4	147459931	274831294	483366156			4	1107787545
5	134462491	252248787	445782148	767349090		5	1090158423
6	122445161	231428259	411007369	708247999		6	1070762902
7	111426538	212123971	378854487	653556883		7	104996098
8	101330896	194356811	349141237	602972437		8	1028195022
9	920843095	177901431	321520313	556191565		9	1005731545
40	835563077	162772231	295862550	512941949		10	982954301
1	757578649	148775824	272045311	472969837		1	960200299
2	685752643	135837600	250354247	436038744		2	937760065
3	620156440	123962882	229464563	401913221		3	915598736
4	560266871	112990248	210587756	370376287		4	893693070
5	505615788	102927513	193089836	341234552	587385618	5	872031446
6	455761962	936355188	176976033	314302384	541605945	6	850579000
7	410310087	851210517	162045917	289414830	499265708	7	829335734
8	868959419	773358011	148333236	266464802	460188927	8	808348130
9	831418899	702317459	135683572	245220201	424201527	9	787674295
50	297401010	637125153	124115445	225598136	391123336		
1	266624944	577864622	113482983	207510284	36077171	20	767849090
2	238819341	523644046	108726250	191171718	332961301	1	747430623
3	213685646	474296073	948068975	175494656	307383509	2	727942134
4	190772896	429250983	865679865	161342756	283765458	3	708895244
5	169985574	888047238	789942444	148191530	26138826	4	690278333
6	151056549	350272490	719627327	136013623	241554776	5	672091401
7	133809391	315593403	654719850	124639765	222607252	6	654334447
8	118083467	283709474	594669719	114060089	204867578	7	637007472
9	103742943	254356305	539012333	104133989	188200807	8	620087233
60	905208452	227324730	487000038	948702559	172440690		
1	784960971	202428605	438729879	861592380	157547215	30	587385618
2	675668116	179521030	893624394	779712530	143704206	1	571569379
3	577300642	158500489	851889588	703391025	130202938	2	556090150
4	488643423	139266947	813859367	631958702	117782523	3	541029278
5	410350325	121731265	277891118	5565699141	106123961	4	526468111
6	340661819	105807520	245348273	504062771	952707064	5	512476375
7	279883076	914081811	215590263	447253741	851442049	6	499112176
8	227193749	784320421	188442243	394984680	757596803	7	486421997
9	181855248	667918481	163759840	347027268	670436122	8	474243144
70	143174494	563083269	141406934	302937486	590138699	9	462412922
1	111056883	470211073	121259751	262810069	516115185	40	450803500
2	842137848	388542540	103202911	226286487	448240537		
3	624909304	317241737	871001463	193372493	386531687		
4	451855232	255541939	728313202	163875039	330490383		
5	316503963	203195791	602784481	137605120	280120856		
6	215764922	158834844	493331507	114394547	235021147		
7	142968609	122114200	398817860	940629671	195138748		
8	922298721	921654850	818174564	764451963	160233082		
9	583811936	681276795	250219539	613486719	130005391		
80	356468115	491837983	193432315	485765998	104066135		
1	211348430	347219775	147011674	379119079	821676697		
2	194597735	237724229	109680352	291327987	638776429		
3	701543136	157973827	801970638	220184647	488835620		
4	526568539	101430211	573627813	163488119	367858524		
5	124544196	625369127	401487467	119102081	271889150		
6	3108877	371755358	273666839	849992803	197097774		
7		212693501	181668528	593318822	139936884		
8		117414766	117332797	405057396	973198228		
9		630037922	735220009	270031818	662062343		
90		323162125	445883941	175359297	440379283		
1		159194822	261537738	110734190	285565378		
2		77355037	147588289	680937556	180867552		
3		34860322	78498644	398506570	109411772		
4		12354059	38370960	217002897	618474117		
5		3299184	16566070	106354296	315502200		
6		511569	6117272	45032155	139867175		
7			1824577	15584310	50897448		
8			382459	3821915	13194052		
9			69617	812398	2983777		

NOTE.—The local value of the figures is not assigned in these columns.

$D_{x+y}$   $x$  BEING THE YOUNGER AGE.  $4\frac{1}{3}$  PER CENT.

$$y = x + n$$

x	-10	-9	-8	-7	-6	-5	-4	-3	-2	-1	z
18	553294 9	584672 515899	617764 576543	652629 609166	689393 643557	728143 718019	748954 755293	812027 806737	857347 804646	905184 864646	18 9
20	479901 1	507778 445179	536919 471136	567368 498744	599471 527336	633314 557274	669999 588806	704593 622047	744226 657087	787095 691011	20 20
1	412665 3	436545 404097	462221 427481	49071 452024	517138 478916	546468 506401	577386 535120	600093 553120	644949 584398	681561 631645	1 3
4	530915 5	572175 321124	595269 342967	618148 363744	642735 386317	669453 408678	695307 432708	723429 457844	753429 484419	781575 611575	4 4
6	297309 7	315644 273265	335028 293680	355324 309288	377374 327198	399212 347020	422691 368555	447246 389882	472913 412813	499793 436393	5 7
8	251028 9	266808 230326	283498 260424	300983 276716	319466 293782	338819 311823	359445 330713	380608 331723	403057 351236	426471 371561	6 9
30	211195 1	224744 198396	239084 206000	254112 219215	270009 232302	286661 247861	304265 263366	322697 279600	342723 294780	362355 314754	30 1
2	176850 3	188566 161988	200955 172375	213740 187944	227378 195772	241670 208381	250789 221264	272024 235554	289497 250290	300497 265730	30 3
4	147480 5	157466 184462	167966 153402	179093 163632	190765 174472	203003 185842	215958 197784	224399 210939	234007 223607	243495 237596	3 4
6	122445 7	130973 111427	139926 119253	149420 127557	159385 136278	169943 145524	181018 155229	192681 165513	204023 171809	217463 187608	6 6
8	10131 9	108511 920843	116182 98689	124220 105661	132712 113082	141717 120957	151187 129227	161181 137995	171686 147197	182699 156948	8 9
40	885563 1	896591 757579	906070 813487	102377 872893	110103 935119	117770 101059	125823 107194	134959 114659	143519 122447	152813 130009	40 1
2	685753 3	737518 62015	791946 667538	840779 717828	910551 77091	975071 827207	104355 886385	111623 940171	119254 101545	134241 110066	5 5
4	506026 5	603618 505616	649735 545201	698782 58761	750351 632334	805147 680066	862727 730254	925858 730254	987475 830621	105760 866115	6 6
6	455762 7	492001 410310	503057 443491	516183 478087	516120 516120	561754 558484	571059 545843	570428 545303	581701 562839	584405 572623	7 7
8	368959 9	399197 331419	413410 359029	465713 388453	502229 419799	541009 453179	582430 488712	592652 526527	606755 506537	621747 565820	8 9
50	297401 1	322611 239645	349488 314198	379130 340374	408642 363829	441115 383795	475724 397855	512574 429631	551098 463318	589357 486168	50 50
2	238819 3	259846 232840	282281 272702	303020 274070	313172 268348	358920 29109	384786 315456	418707 384119	451518 386772	487050 390441	4 4
4	190773 5	204830 169956	227603 203073	247020 221352	268348 204919	291095 240199	315466 261611	341190 283787	365743 307424	386424 323607	5 5
6	151057 7	165639 147084	181217 161283	197863 176462	215672 192680	234848 210000	254921 201000	276550 228409	290546 249217	294119 262925	6 7
8	118083 9	130148 103743	143060 114686	150870 126404	171634 138944	187408 152357	204255 166896	222283 182016	241426 198378	261891 215844	8 9
60	905208 1	100577 971961	111186 975669	123547 107558	134704 115457	147708 103098	161009 124887	176442 156335	192324 170703	202857 186008	60 60
2	675868 3	757423 653171	8144947 728348	938816 813071	103784 903298	114388 908691	125737 110073	137874 120693	150850 132073	164714 145159	1 3
4	589643 5	553567 467313	623971 529690	698262 598733	780047 667738	8066729 796016	854153 828893	954560 916351	105650 916351	110408 100027	127289 110073
6	410350 6	390662 391103	445394 45394	504845 504845	589733 568733	598744 568744	637378 637378	711024 709016	790016 767529	873347 750211	962880 111015
8	279883 9	323495 327194	371898 264688	422964 305986	479409 351285	540089 539092	560529 545382	605259 571067	675239 627239	723845 638554	7 7
9	181855 10	213884 170344	249184 200345	283408 234408	330658 269781	376559 309727	420322 352722	490846 399608	538866 450407	583886 504755	9 10
11	111057 1	133376 102841	158886 123509	186634 144947	217433 172827	251318 201349	284530 232726	325683 287186	372447 304275	419582 384489	1 1
13	842138 3	774629 642909	945971 945971	113608 113608	135167 135167	158973 158973	185602 185602	214070 214070	245767 215767	279883 244303	3 3
4	451855 5	570561 409171	707260 616664	863700 640448	103728 728112	123411 939273	145147 111753	160101 131136	195453 153127	214518 176989	5 5
6	215765 7	234039 367201	284022 463668	374756 374756	501888 412024	701888 510739	842494 623711	944046 749058	102091 891200	117954 104518	137420 120000
8	142969 9	191783 125718	252402 168592	326302 221939	412024 296920	510739 382298	623711 484097	749058 548438	891200 658652	981200 785630	7 7
9	583812 10	801824 170344	109253 109253	146570 146570	192949 192949	249441 249441	314971 286666	390434 314971	476793 390434	512618 447575	9 9
12	356468 1	501454 211348	688712 322288	988745 421514	125893 583919	165730 795906	214253 196738	270539 180532	335354 287436	400534 329359	80 80
14	124598 2	176706 252690	256467 256467	488208 488208	665449 665449	892423 892423	117461 117461	151879 151879	191777 151777	212255 182255	1 1
16	70154 3	102386 8	145559 83211	208150 118012	292811 168757	402155 237396	548155 326046	785121 444415	967715 859597	125107 784597	13 13
18	32856 4	56877 26029	83211 453535	118012 632525	168757 940663	237396 134611	326046 187920	444415 259881	596715 384229	625745 475650	5 5
20	129454 5	26029 20746	83469 83469	134616 83469	168757 547477	237396 738160	326046 105263	444415 148076	596715 203742	625745 277245	5 5
22	3109 6	23885 1794	20746 1794	15829 15829	272291 17760	389824 290483	467675 299885	687655 424966	80365 607722	820163 544643	7 7
24	356468 1	501454 322288	688712 421514	988745 583919	125893 795906	165730 892423	214253 117461	270539 151879	335354 191777	400534 182255	80 80
26	124598 2	176706 252690	256467 256467	488208 488208	665449 665449	892423 892423	117461 117461	151879 151879	191777 151777	212255 182255	1 1
28	70154 3	102386 8	145559 83211	208150 118012	292811 168757	402155 237396	548155 326046	785121 444415	967715 859597	125107 784597	13 13
30	32856 4	56877 26029	83211 453535	118012 632525	168757 940663	237396 134611	326046 187920	444415 259881	596715 384229	625745 277245	5 5
32	129454 5	26029 20746	83469 83469	15829 15829	272291 17760	389824 290483	467675 299885	687655 424966	80365 607722	820163 544643	7 7
34	3109 6	23885 1794	20746 1794	15829 15829	272291 17760	389824 290483	467675 299885	687655 424966	80365 607722	820163 544643	7 7
36	356468 7	501454 322288	688712 421514	988745 583919	125893 795906	165730 892423	214253 117461	270539 151879	335354 191777	400534 182255	80 80
38	124598 8	176706 252690	256467 256467	488208 488208	665449 665449	892423 892423	117461 117461	151879 151879	191777 151777	212255 182255	1 1
40	70154 9	102386 8	145559 83211	208150 118012	292811 168757	402155 237396	548155 326046	785121 444415	967715 859597	125107 784597	13 13
42	32856 10	56877 26029	83211 453535	118012 632525	168757 940663	237396 134611	326046 187920	444415 259881	596715 384229	625745 277245	5 5
44	129454 11	26029 20746	83469 83469	15829 15829	272291 17760	389824 290483	467675 299885	687655 424966	80365 607722	820163 544643	7 7
46	3109 12	23885 1794	20746 1794	15829 15829	272291 17760	389824 290483	467675 299885	687655 424966	80365 607722	820163 544643	7 7
48	356468 13	501454 322288	688712 421514	988745 583919	125893 795906	165730 892423	214253 117461	270539 151879	335354 191777	400534 182255	80 80
50	124598 14	176706 252690	256467 256467	488208 488208	665449 665449	892423 892423	117461 117461	151879 151879	191777 151777	212255 182255	1 1
52	70154 15	102386 8	145559 83211	208150 118012	292811 168757	402155 237396	548155 326046	785121 444415	967715 859597	125107 784597	13 13
54	32856 16	56877 26029	83211 453535	118012 632525	168757 940663	237396 134611	326046 187920	444415 259881	596715 384229	625745 277245	5 5
56	129454 17	26029 20746	83469 83469	15829 15829	272291 17760	389824 290483	467675 299885	687655 424966	80365 607722	820163 544643	7 7
58	3109 18	23885 1794	20746 1794	15829 15829	272291 17760	389824 290483	467675 299885	687655 424966	80365 607722	820163 544643	7 7
60	356468 19	501454 322288	688712 421514	988745 583919	125893 795906	165730 892423	214253 117461	270539 151879	335354 191777	400534 182255	80 80

$D_{x'y}$   $x$  BEING THE OLDER AGE.  $\frac{1}{4}$  PER CENT.

$$y = x - n$$

$n$	0	1	2	3	4	5	6	7	8	9	$x$
18	955547	1008610	1064514	1123406	1090158	1070763	1040996	102195	100915	990927	18
9	892699	942263	994588	1048714	1107788						9
20	832012	878395	927267	978760	1033009	1090158	1070763	1040996	102195	100915	20
1	77975	817209	862767	919770	961346	1014630	1070763	1040996	102195	100915	1
2	71874	768664	801360	848034	893106	942762	994062	1040996	102195	100915	2
3	666431	703811	743206	784721	828488	874563	923128	974294	102195	100915	3
4	617180	651871	684434	724969	767577	810383	855456	902960	953008	1005732	4
5	571035	608202	637108	672843	710505	750193	792015	836082	882510	931425	5
6	528008	557817	589239	622460	657248	694058	732827	773681	816728	862063	6
7	488053	515468	544780	575468	607815	641907	677837	715701	755604	797640	7
8	460946	476520	503492	531906	561989	593451	626783	661818	695787	737743	8
9	416288	440157	465119	491436	519180	548426	579252	611743	645984	682069	9
20	883879	408178	429488	451845	479525	506596	535133	565212	596915	639327	20
1	853496	874435	891186	418923	442380	467728	494134	521088	551308	582231	1
2	825642	844904	865083	886291	408460	431824	458046	481793	508933	537539	2
3	290111	317894	330078	355844	376515	399123	420701	444506	468610	496053	3
4	274631	291461	309569	327483	344744	366946	387941	409842	431817	457590	4
5	252240	267740	283959	301581	318032	337796	357319	377931	399944	421960	5
6	231428	248701	260790	276588	293752	310751	329048	348141	368120	385997	6
7	212124	225394	239295	253900	268693	284093	302648	320449	339063	358523	7
8	194357	206572	219496	233033	247344	262328	278607	294729	312064	330192	8
9	177901	189253	201149	213732	226914	240848	255439	271291	286959	303569	9
40	162772	173214	184266	195849	208101	220935	234503	248709	264143	279423	40
1	149776	158473	169839	178399	190675	202603	215098	228307	242138	257164	1
2	135638	144836	154275	164173	174467	185625	197233	204042	222261	235728	2
3	120363	132229	140089	150177	159911	170008	180495	191999	203840	216359	3
4	112990	120457	127479	137293	144179	155550	165475	175876	186878	194404	4
5	102027	109964	117425	125256	133564	142258	151353	161043	171165	181873	5
6	99853·5	100156	107003	114264	121883	129958	138427	147307	156706	166537	6
7	85121·1	91090·5	97443·6	104105	111169	118588	128438	134678	143318	152442	7
8	77353·8	82815·7	84632·2	94904·5	101286	109158	115371	123014	131051	139438	8
9	70231·7	75254·4	80688·8	86246·8	92251·9	98559·7	105247	112266	119703	127504	9
50	63719·5	68863·5	72524·4	78445·1	83954·6	88901·8	93540·3	102450	109292	116523	50
1	57786·5	62051·0	66562·4	71344·1	76399·4	81765·3	87459·4	93488·4	98778·5	104492	1
2	52364·4	56517·2	60473·4	64889·5	69530·1	74568·4	80235·7	91062·7	97241·6	102452	2
3	47429·6	51053·3	54007·3	58593·8	63264·8	67789·2	72592·7	77691·2	81310·6	87872·7	3
4	42925·1	46246·5	49779·8	53537·5	57448·5	61886·7	66094·2	70781·8	75753·2	81024·6	4
5	38804·7	41847·4	45058·5	48530·0	52193·9	56045·2	60138·0	64433·7	69001·8	73151·3	5
6	35027·2	37812·4	40777·3	43924·4	47289·0	50853·7	54612·0	58660·1	62720·9	67240·2	6
7	31559·5	34106·2	36818·1	39705·0	42777·2	46045·4	49521·8	53175·9	57059·1	61139·7	7
8	28370·9	30698·1	33179·0	35310·7	384018·7	41806·8	44785·7	48106·4	51721·0	55498·0	8
9	25435·6	27554·7	29812·9	32218·6	34780·4	37507·5	40409·7	43407·1	46780·5	50232·9	9
60	22732·5	24453·6	26713·8	28903·1	31235·4	33719·1	36363·0	39176·6	42169·8	45353·0	60
1	20242·9	21990·6	23854·7	25942·3	27959·9	30216·1	32618·7	35176·3	37898·1	40748·6	1
2	17053·1	19533·7	21219·1	23017·8	24935·4	26879·0	29156·0	31474·3	33942·3	36508·5	2
3	16450·0	17274·8	18795·8	20418·6	22149·5	23894·7	25961·2	28026·9	30268·1	32061·7	3
4	15028·7	15206·7	16578·6	18092·8	19598·8	21250·4	23020·7	24907·4	26917·2	29057·5	4
5	12173·1	13518·8	14542·9	15850·2	17245·7	18734·7	20322·8	22015·8	23520·1	25742·2	5
6	10580·8	11602·2	12094·1	13860·7	15106·7	16486·8	17855·9	19369·5	20993·2	22702·9	6
7	9140·82	10047·7	11017·6	12054·5	13162·4	14345·6	15606·6	16956·3	18391·6	19426·0	7
8	7843·20	8644·67	9502·18	10419·5	11400·1	12474·8	13566·8	14761·2	16035·7	17305·0	8
9	6679·18	7383·73	8138·14	8945·50	9809·05	10782·8	11718·6	12772·0	13898·5	15096·3	9
70	5630·83	6256·38	6916·32	7622·98	8379·24	9188·13	10052·8	10976·8	11963·5	13018·8	70
1	4702·11	6245·47	6829·21	6443·99	7101·28	7805·79	8559·81	9164·85	10225·6	11144·8	1
2	3883·43	4354·26	4857·43	5307·06	5966·35	6375·95	7228·84	7926·12	8672·06	9409·09	2
3	3172·42	3573·93	4005·21	4468·04	4944·41	5483·97	6048·66	6648·89	7290·73	7976·88	3
4	2655·43	2896·51	3263·13	3636·88	4079·45	4532·66	5010·77	5522·74	6070·64	6656·66	4
5	2031·96	2314·02	2622·90	2934·88	3311·43	3694·09	4104·43	4517·43	5091·04	5407·18	5
6	1584·86	1823·63	2076·67	2333·86	2651·79	2971·77	3315·18	3683·47	4072·01	4489·06	6
7	1211·14	1411·44	1620·43	1845·37	2091·88	2356·43	2640·77	2945·93	3273·20	3611·47	7
8	921·655	1073·76	1241·09	1424·85	1622·64	1839·23	2078·03	2322·05	2590·34	2878·15	8
9	681·277	801·265	933·500	1078·97	1238·73	1410·69	1598·98	1801·37	2018·73	2262·01	9
80	401·838	585·170	688·231	801·813	926·763	1063·99	1211·68	1373·42	1547·25	1733·95	80
1	347·220	417·000	498·131	583·511	679·810	785·747	902·091	1027·82	1164·44	1311·88	1
2	237·724	290·307	348·650	414·810	487·867	568·382	656·955	751·229	853·928	973·576	2
3	157·974	195·823	239·136	287·196	341·695	401·874	468·197	541·158	621·286	707·530	3
4	101·430	128·077	158·763	193·879	232·848	277·028	325·810	379·549	438·742	503·706	4
5	62·539	80·8467	102·086	128·544	154·535	185·591	220·810	259·699	302·553	349·707	5
6	57·1753	45·9389	63·2875	79·8883	99·0255	120·963	145·237	172·797	203·230	234·770	6
7	21·9894	28·6240	37·5498	48·5487	61·9265	75·9824	92·7890	111·437	132·53	155·934	7
8	11·7415	16·0041	21·4629	28·2544	38·5269	46·1226	57·1730	69·8193	83·8509	99·7624	8
9	8·3003	8·6581	11·7946	15·8175	20·8226	28·9193	33·9910	42·1348	51·4547	61·7356	9
90	3·2316	4·5460	6·2436	8·5103	11·4131	15·0245	19·4234	24·5261	30·4023	37·1270	90
1	1·8919	3·3764	8·2023	4·3982	5·9550	8·6398	10·5839	13·6827	17·2772	21·4166	1
2	·7736	1·0670	1·5688	2·2068	3·0308	4·1313	5·5406	7·2396	9·4291	11·9033	2
3	·8486	·5100	·7239	1·0343	1·4550	1·9983	2·7238	3·6528	4·4057	6·2166	3
4	·1233	·2151	·3147	·4464	·6384	·8980	1·2334	1·6813	2·2546	2·9680	4
5	·0329	·0689	·1200	·1756	·2401	·3563	·5013	·6884	·9383	1·2544	5
6	·0061	·0180	·0335	·0583	·0854	·1211	·1733	·2436	·3346	·4561	6
7	·0020	·0064	·0005	·0004	·0004	·0009	·0007	·0017	·0024	·0034	7
8	·0003	·0003	·0003	·0003	·0004	·0004	·0009	·0017	·0024	·0034	8
9	·0003	·0003	·0003	·0004	·0004	·0004	·0009	·0017	·0024	·0034	9

$D_{x,y}$   $x$  BEING THE OLDER AGE.  $4\frac{1}{2}$  PER CENT.

$$y = x - n$$

$x$	10	11	12	13	14	15	16	17	18	19	$y$
25	989854										25
6	909864	960200									6
7	841934	888600	937760								7
8	778780	822038	867600	915590							8
9	720083	760158	802370	846843	893693						9
30	665537	702639	741733	782922	820317	872031					30
1	614820	649164	685854	723466	763662	805989	850579				1
2	567690	599465	632951	668237	705417	744590	785859	829396			2
3	523936	553333	584295	616933	651324	687563	725747	765973	808348		3
4	483366	510534	539172	569531	601155	634468	669980	707186	746383	787674	4
5	447582	470893	497362	525259	554460	583643	618281	652692	689437	727123	5
6	411007	434211	458870	484452	511925	540262	570441	602242	636750	671064	6
7	378854	402921	422889	446711	471820	498285	526175	555567	585539	619173	7
8	349141	368942	389817	411824	435022	469475	495247	512408	541031	571193	8
9	321520	339972	359253	379390	401009	423598	447408	472503	498941	520823	9
40	205863	313049	331015	349787	386959	390448	412437	435620	460054	485805	40
1	272045	283046	304778	322289	340446	359814	380128	401540	424111	447709	1
2	250954	264841	280418	296708	317375	331628	350286	370603	390905	412380	2
3	228465	247474	257507	272970	288826	305402	322723	340488	360233	380524	3
4	210588	223345	237205	250981	265690	281124	297257	314115	331889	350023	4
5	193090	204948	217363	230652	244211	258574	273595	293926	305703	324000	5
6	176976	187891	199429	211510	224436	237635	251618	266228	281506	297471	6
7	162046	172183	182802	194028	205783	218558	231199	244707	259017	273849	7
8	148333	157657	167520	177851	188773	200209	212433	224938	239167	255203	8
9	135684	144341	153414	163011	173065	183693	194921	206610	218884	231757	9
50	124115	132078	140505	149387	158679	168465	178811	189643	201412	213067	50
1	113483	120879	128633	136841	146442	154541	164072	174148	184407	195169	1
2	103728	110598	117805	125383	133369	141744	150613	159900	169720	180001	2
3	94806 9	101129	107829	114486	122224	130023	138198	146841	156897	166470	3
4	86568 0	92441 9	98608 5	105139	111991	119175	126779	134748	143178	152048	4
5	78904 2	84494 6	90121 0	96130 8	102499	109179	116183	123506	131365	139583	5
6	71962 7	76974 2	82236 4	87816 4	93672 6	99877 9	106387	112121	120436	129006	6
7	65472 0	70070 4	74950 0	80073 9	85507 2	91209 8	97251 5	103589	110235	117269	7
8	59467 0	63680 2	68153 3	72899 4	77883 1	83167 7	88713 9	94650 7	100755	107219	8
9	53901 2	57758 0	61848 5	66192 4	70302 0	75643 8	80774 9	86181 4	91868 2	97850 4	9
60	48700 0	52256 4	55993 5	59961 1	64172 5	68641 4	73334 0	78310 0	83538 1	89065 7	60
1	43873 0	47110 8	50551 1	54161 3	58004 4	62078 3	66401 4	70940 9	75754 4	80806 2	1
2	39362 4	42833 8	45458 0	48777 6	52268 0	55949 4	59909 4	64071 8	68462 0	73098 7	2
3	35189 0	37877 5	40736 7	43743 0	46937 4	50294 2	53857 9	57640 8	61654 7	65869 6	3
4	31335 9	33780 6	36339 9	39083 1	41967 4	45032 2	48252 6	51617 7	55300 9	59152 0	4
5	27789 1	29968 1	32286 9	34763 6	37677 1	40135 5	43008 4	46140 8	49418 2	52856 9	5
6	24534 8	26485 7	28562 4	30772 5	33123 5	35623 9	38252 9	41046 6	43941 9	47098 3	6
7	21559 0	23293 7	25151 2	27123 4	29222 0	31454 7	33829 1	36325 6	38978 4	41765 9	7
8	18944 2	20388 6	22038 3	23785 8	25650 9	27655 6	29747 0	31992 5	34358 5	38062 2	8
9	16376 0	17740 3	19194 2	20743 0	22392 3	24148 1	26016 0	28004 3	30118 3	32341 0	9
70	14140 7	15359 4	16617 3	17679 1	19429 0	20074 9	22619 5	24869 7	26231 6	28211 8	70
1	12128 0	13172 9	14289 6	15480 0	16748 7	18100 2	19539 4	21071 5	22701 9	24344 4	1
2	10320 3	11228 0	12198 4	13212 5	14334 9	15509 7	16761 2	18093 9	19519 7	21022 5	2
3	8710 01	9493 98	10328 8	11220 6	12171 7	13186 7	14246 4	15417 5	16453 5	17948 5	3
4	7288 13	7952 51	8667 38	9430 49	10244 7	11113 1	12039 0	13245 6	14076 7	15198 0	4
5	6027 84	6595 14	7201 28	7848 63	8539 65	9279 96	10063 3	10901 7	11793 2	12747 0	5
6	4933 32	5409 55	5918 65	6462 62	7043 66	7663 71	8325 39	9031 12	9783 60	10565 3	6
7	3988 18	4388 84	4907 03	5259 48	5742 81	6259 04	6810 11	7398 10	8025 15	8603 80	7
8	3181 75	3504 83	3854 74	4226 85	4624 65	5049 09	5563 62	5988 18	6508 20	7056 63	8
9	2502 20	2768 13	3048 76	3351 22	3674 72	4020 56	4390 08	4784 72	5205 68	5655 47	9
80	1934 32	2149 21	2375 92	2618 67	2878 47	3156 34	3453 39	3770 73	4109 74	4471 58	80
1	1470 12	1640 00	1822 19	2014 40	2220 23	2440 48	2678 07	2927 93	3197 02	3484 41	1
2	1098 80	1229 15	1371 19	1523 52	1684 22	1856 30	2040 46	2237 44	2448 01	2643 00	2
3	801 971	903 477	1012 50	1124 60	1254 68	1387 35	1529 10	1690 80	1843 06	2016 51	3
4	573 628	650 195	732 491	820 677	915 735	1017 47	1124 79	1239 72	1362 71	1404 25	4
5	401 487	457 220	518 249	583 845	654 295	729 903	810 991	896 536	988 138	1086 17	5
6	273 607	314 188	357 802	405 561	458 894	512 025	571 193	634 649	701 594	773 278	6
7	191 669	209 979	241 070	274 534	311 178	350 565	392 864	438 264	486 952	538 317	7
8	117 333	136 697	157 999	181 393	208 573	234 146	263 783	295 612	329 772	366 408	8
9	73 5220	86 4708	100 741	116 440	133 681	152 238	172 539	194 400	217 657	243 038	9
90	44 8884	53 0406	62 9928	72 8807	84 0171	96 4574	109 847	124 609	140 260	157 194	90
1	28 1538	31 4099	37 3703	43 9520	51 2056	59 1851	67 9486	77 8809	87 7066	98 8111	1
2	14 7588	18 0234	21 6455	25 7530	30 2887	35 2973	40 7863	46 5254	53 5255	60 4435	2
3	7 8468	9 7305	11 8829	14 2710	16 9791	19 9695	23 2651	26 8906	30 8723	35 1278	3
4	3 8371	4 8461	6 0059	7 8344	8 8084	10 4799	12 3257	14 8598	16 8976	19 0551	4
5	1 6566	2 1416	2 7042	3 3521	4 0936	4 9163	5 8402	6 8784	8 0147	9 2337	5
6	6117	8052	1 0410	1 3145	1 6295	1 9899	2 3898	2 8433	3 3441	3 8960	6
7	1824	2446	3221	4164	5258	6518	7959	9569	1 1373	1 3376	7
8	1082	10521	10699	10920	1189	1502	1863	2274	2731	3249	8
9	10069	10095	10180	10174	10230	10297	10375	10465	10568	10683	9

**D<sub>x'y</sub>** *x* BEING THE OLDER AGE. 4½ PER CENT.

*y* = *x* - *n*

<i>x</i>	20	21	22	23	24	25	26	27	28	29	<i>x</i>
35	787349										35
6	708248	747431									6
7	653567	689781	727942								7
8	602972	636456	671733	708895							8
9	556192	587127	616742	654092	690278						9
40	512942	541537	571668	603413	636868	672091					40
1	472970	499390	527230	556564	587471	620032	654334				1
2	436059	466445	496166	513289	541826	571914	603614	637007			2
3	401913	424427	448215	473252	499635	527454	557723	587580	620067		3
4	370976	391195	413137	438262	460631	488311	513369	541876	571911	603550	4
5	341235	360457	380717	402073	424577	448294	473296	499619	527363	558593	5
6	314308	332046	350751	370466	391246	413145	436223	460542	486166	513163	6
7	289415	305790	323054	341253	360433	380650	401956	424409	449069	472999	7
8	266445	281576	297509	314304	332009	350971	370341	391070	412915	435934	8
9	246220	259293	273998	289501	305845	323074	341235	360373	380545	401802	9
50	225598	238703	252402	266716	281808	297717	314488	332165	350796	370431	50
1	207510	219715	232478	245820	259781	274459	289953	306286	323503	341648	1
2	191173	202214	214120	228567	239570	253156	267480	282581	298469	315277	2
3	175465	188385	197171	20767	220895	233572	246818	260783	275506	291025	3
4	161343	171117	181736	192252	203560	215384	227745	240681	254278	268633	4
5	148192	157293	168821	177173	187424	198449	209977	220207	234619	247894	5
6	138014	144402	153720	162556	172624	182633	193374	204407	216350	229619	6
7	124640	132437	140805	149299	158280	168103	177830	188289	199226	210660	7
8	114060	121230	128814	136758	145156	153950	163503	172985	183138	193776	8
9	104134	110778	117742	125107	132823	140950	149320	158799	167988	177868	9
60	94870·3	100956	107398	114149	121290	129770	136678	144058	153953	162863	60
1	86159·3	91774·3	97061·7	103893	110424	117332	124568	132127	140227	148293	1
2	777971·3	83188·5	88554·6	94235·4	100248	108550	113215	120197	127579	135308	2
3	70389·1	75029·7	80000·1	85213·8	90680·3	96468·3	102530	108944	115683	122768	3
4	63195·9	67448·9	71984·1	76754·7	81761·8	86999·5	92550·6	98368·1	104523	110968	4
5	58589·9	60437·3	64538·9	68841·9	73402·3	78188·1	83201·8	88510·6	94074·1	99599·3	5
6	50404·8	55916·5	57602·5	61511·0	65612·9	69959·5	74618·8	79299·3	84359·0	89661·7	6
7	44725·4	47868·6	51200·0	54700·3	58441·9	62307·1	66454·7	70764·8	75303·9	80109·7	7
8	38498·5	42297·3	45268·0	48420·4	51730·6	55240·7	58924·5	62829·0	66922·5	71215·7	8
9	34708·7	37184·5	39818·3	42618·0	45583·8	48700·1	52004·5	55472·5	59147·3	63002·0	9
70	30203·7	32508·0	34930·7	37298·7	39918·4	42608·3	45617·3	48719·6	51961·0	55403·2	70
1	26281·0	29230·5	30281·4	32446·9	34744·1	37158·4	39776·1	42495·4	45378·8	48404·9	1
2	22228·6	24318·8	26193·8	28041·8	30046·6	32175·7	34435·5	36833·6	39351·7	42021·8	2
3	19337·9	20814·7	22385·9	24087·9	25793·5	27638·0	29596·3	31675·0	33880·9	36197·1	3
4	16387·5	17855·5	19004·4	20439·0	21947·4	23550·1	25254·3	27022·4	28920·3	30634·3	4
5	13760·5	14393·5	15987·7	17209·2	18509·2	19874·1	21325·5	22850·6	24469·7	26188·3	5
6	11439·5	121449·0	13317·3	14347·8	15444·0	16609·8	17835·8	19138·0	20508·7	21959·8	6
7	9498·30	10165·3	10973·6	11834·0	12749·7	13723·8	14759·8	15849·0	17006·4	18222·7	7
8	7644·58	8271·02	8938·44	9649·16	10405·8	11210·9	12067·4	12978·4	13933·2	14953·9	8
9	6134·87	64·556	7190·63	7770·86	8388·75	9046·51	9746·49	10491·1	11283·1	12115·8	9
80	4887·68	5209·43	5708·42	6176·28	6674·64	7205·36	7770·34	8371·57	9011·18	9691·40	80
1	3701·19	4118·58	4467·64	4859·84	5238·49	5659·05	6109·00	6588·01	7097·76	7640·05	1
2	2913·23	3169·78	3443·46	3735·35	4046·54	4378·17	4731·45	5107·67	5508·17	5944·87	2
3	2201·85	2399·78	2611·06	2836·60	3076·94	3333·28	3606·46	3897·48	4207·38	4637·28	3
4	1634·88	1785·14	1945·61	2116·91	2299·68	2464·62	2702·45	2923·93	3169·87	3411·12	4
5	1191·02	1303·11	1422·88	1550·78	1687·38	1833·00	1983·38	2154·03	2330·57	2518·63	5
6	849·993	932·046	1019·76	1113·40	1213·58	1320·43	1434·44	1556·03	1685·66	1823·81	6
7	609·319	652·181	715·138	753·448	854·354	931·154	1013·14	1100·61	1193·91	1293·37	7
8	405·057	446·443	490·734	538·107	583·749	642·860	700·640	762·335	822·156	898·356	8
9	270·638	298·515	329·016	361·656	399·589	433·891	473·769	516·357	561·819	610·327	9
90	175·359	194·841	215·393	237·400	260·958	286·143	313·073	341·846	372·576	405·379	90
1	110·734	123·530	137·254	151·733	167·234	183·625	201·571	220·541	240·811	262·458	1
2	64·0938	76·3103	85·1285	94·5857	104·583	115·246	126·680	138·909	151·983	165·960	2
3	39·8007	41·8946	50·3118	58·1257	62·3609	69·9389	75·9826	83·5207	91·5833	100·202	3
4	21·7003	24·5968	27·7101	31·0537	34·6423	38·4907	42·5508	46·8954	51·5510	56·5275	4
5	10·6354	12·1118	13·7285	15·4681	17·3323	19·3359	21·4833	23·7403	26·1759	28·7727	5
6	4·5093	5·1700	5·8876	6·6735	7·5182	8·4254	9·3990	10·4433	11·5448	12·7344	6
7	1·5594	1·8013	2·0680	2·3550	2·6994	3·0073	3·3701	3·7598	4·1772	4·6179	7
8	·3891	·4453	·5146	·5908	·6738	·7628	·8598	·9629	·1·0741	·1·9335	8
9	·0812	·0955	·1113	·1286	·1477	·1653	·1906	·2148	·2407	·2686	9

**D<sub>x·y</sub>** *x* BEING THE OLDER AGE.  $4\frac{1}{2}$  PER CENT.

$$y = x - n$$

<i>x</i>	30	31	32	33	34	35	36	37	38	39	<i>y</i>
45	587388										45
6	541606	571569									6
7	499266	526938	556090								7
8	460189	485744	512667	541029							8
9	424202	447803	472671	498869	526468						9
50	391123	412928	435902	460109	485611	512476					50
1	360771	380924	402159	424595	448110	472947	499112				1
2	332961	351598	371239	391834	413741	436717	460923	486422			2
3	307384	324625	342795	361944	382121	403382	425782	449382	474243		3
4	283765	299718	316527	334244	352915	372689	398319	415160	438172	462418	4
5	261893	276841	292151	308580	325582	344054	363235	383445	404738	427171	5
6	241555	255192	269567	284719	300689	317520	335266	353946	374639	394386	6
7	222607	235203	249481	262478	272732	290170	309170	326440	344639	363814	7
8	204897	216517	228768	241683	255297	269647	284778	300711	317509	335209	8
9	188201	199002	210287	222186	234229	247952	261889	276578	292059	308374	9
60	172441	182458	192929	203870	215406	227566	240385	253897	268138	283147	60
1	157547	166813	176504	186683	197217	208376	220140	232541	246612	259349	1
2	147074	152020	160961	170311	180085	190298	201068	212417	224493	239095	2
3	130203	138283	146235	154889	163886	173291	183119	193440	204443	215917	3
4	117782	124918	132670	140347	148601	157234	166257	175886	185627	191106	4
5	106124	112641	119465	126878	134220	142115	150370	159000	164017	177524	5
6	95270·7	101146	107358	113861	120927	127925	135449	143817	151549	160198	6
7	85144·2	90470 6	96050 2	101949	108125	114835	121480	128625	136096	143007	7
8	75759 7	80521·8	85559 0	90885·7	98414·0	102255	108600	114845	121642	128708	8
9	67043 6	71321 4	75804·5	80546·7	85514·2	90765·7	96264·8	102238	108154	114515	9
70	59013 9	62799·7	66806·7	71006 0	75448·0	80101·1	85020·1	90170·6	95786·8	101508	70
1	51611 5	54975 1	58501 8	62234 6	66146·5	70284 5	74619·1	79201 5	83999 5	89212·3	1
2	44824 1	47793·4	50908·2	54174 0	57630 6	61253·2	65085·0	69099 0	73442·4	77795 5	2
3	38653 2	41230 8	43962·1	46327·2	49831·2	53010 7	56342·9	59867 6	63559·8	67443·0	3
4	33049·0	35291·5	37645·0	40138 8	42754·7	45497·4	49400·4	51442·8	54460 9	58012 0	4
5	28012 1	29927 1	31957·7	34088·9	36347·1	38715 0	41199 6	43428 3	46553·3	49497 4	5
6	23502·1	25158·3	26857 4	28679 7	30592 8	32018·9	34744·7	36973 8	39332·7	41406 1	6
7	19513 9	20884·4	22338 8	23866·0	25485·4	27154 9	28945 7	30874·8	32855 4	34951·6	7
8	16023 8	17158·7	18363 8	19642 7	20985 5	22409·5	23905 8	25497 4	27144 4	29490·0	8
9	13000 5	13930·3	14917 3	15965·1	17076·9	18244 8	19482·2	20781·4	22158·1	23602·2	9
80	10408·6	11166·6	11985 2	12813 0	13712·9	14667·9	15670·6	16733 9	17848 8	19032·3	80
1	8116·77	8823·16	9497·48	10144 6	10863·4	11628·4	12458·0	13284·8	14187 7	15133·8	1
2	6387·76	6869·95	7376·95	7915·88	8481·76	9082·76	9720·68	10397 6	11108 4	11862 2	2
3	4888·36	5261·84	5659·03	6076·66	6520·42	6936·73	7481·80	8007·28	8584·90	9150·43	3
4	3678·59	3963·22	4268·01	4588·04	4920·63	5246·41	5664·47	6065·84	6481·89	6945·97	4
5	2718·89	2932·08	3159·95	3400·30	3656·98	3826·86	4213·63	4614·98	4934·89	5174·46	5
6	1970·98	2127·70	2284·53	2472·07	2680·94	2861·81	3073·01	3297·42	3633·23	373·59	6
7	1399·37	1512·29	1632·54	1761·54	1896·77	2041·68	2195·80	2357·85	2530·04	2710·97	7
8	973·193	1052·98	1137·92	1228·40	1324·72	1427·22	1538·27	1652·23	1774·17	1903·73	8
9	662·062	717·219	775·998	833·615	905·297	976·281	1031·82	1132·18	1217·65	1307·51	9
90	440·379	477·709	517·507	559·919	605·100	653·214	704·432	759·919	816·923	878·590	90
1	285·585	310·221	336·518	364·553	394·430	428·253	460·151	496·211	534·628	575·474	1
2	180·863	198·792	213·783	231·905	251·225	271·814	293·747	317·104	341·969	384·428	2
3	109·412	119·247	129·746	140·949	152·898	165·84	179·208	193·669	209·069	225·462	3
4	61·8474	67·5317	73·6023	80·0925	86·9968	94·3718	102·233	110·612	119·537	129·042	4
5	31·5502	34·5195	37·6921	41·0803	44·6972	49·5564	52·6724	57·0905	61·7309	66·7146	5
6	13·9867	15·3369	16·7803	18·3226	19·9698	21·7278	23·6039	25·6046	27·7377	30·0110	6
7	5·0897	5·5946	6·1347	6·7121	7·3290	7·9878	8·6911	9·4415	10·2418	11·0651	7
8	1·3194	1·4542	1·5934	1·7527	1·9177	2·0940	2·2323	2·4531	2·6975	2·9282	8
9	·2938	·3298	·3635	·3996	·4391	·4794	·5235	·5705	·6207	·6743	9

NOTE.—The summation of the values on this page is not given, but may easily be made if required in any extreme case.

EXTENDED VALUES OF  $D_{x,y}^2$ , FORMED BY ACTUAL MULTIPLICATION OF THE FACTORS  $d_x$  AND  $B_y$  ON THE ARITHMOMETER. From these the intermediate values for each difference of age were computed on the machine by a continuous process, and verified at each tenth interval.

$$B_y = l_y + \frac{1}{12} r^y + \frac{1}{12} a_w + \frac{1}{12}$$

(INTEREST  $\frac{1}{12}$  PER CENT.)

$x$	$y = x + 10$	$y = x$	$y = x - 10$	$y = x - 20$	$y = x - 30$	Diff.	The initial values of $D_{x,y}^2$ for each difference of Age.
18	936995203	133252990				-10	936995203
9	101230898	146409808				9	980629655
20	106315655	156685146				8	1024567353
1	108391196	163011984				7	1068617531
2	108442501	166043160				6	1111444669
3	106341896	165646686				5	1151728636
4	102512624	162085681				4	1189562935
5	971025634	155681036	229084434			3	1226010670
6	906004847	147205324	210325891			2	1261742576
7	843589597	139141425	196309879			1	1297131064
8	784658130	131416366	186891284				
9	727691545	124386549	179899725				
30	673834987	117590593	173301845			+0	1332529900
1	621490850	110806461	166752046			1	1383536851
2	570632393	104396139	159847519			2	1463894342
3	521026297	978697441	152449795			3	1572469248
4	474262880	914768259	144636661			4	1774877864
5	428994815	850019375	136280539	200536629		5	1952716648
6	386992100	786830724	127842221	182660031		6	2090775704
7	848314167	725035842	119587203	168721495		7	2194904992
8	813380549	666855345	111686482	158832805		8	2261594536
9	281704711	610964200	104433985	151042419		9	2293184320
40	253512252	557757237	973339255	143448114		10	2290844336
1	227609604	506915816	903787930	136010559		1	2259254552
2	204279814	460044720	841643290	128869318		2	2231174744
3	183149947	416762463	782847925	121942697		3	2205434920
4	163985713	377186773	727525814	115031215		4	2180865088
5	146782040	340642907	674953042	108213427	159235911	5	2159805232
6	131114237	307376341	624960361	101541943	145082386	6	2138745376
7	116054684	275421086	573304729	945607167	133412482	7	2113005552
8	101637878	245109755	521579118	873552820	124230653	8	2081415768
9	880551890	216723524	470032522	803441011	116201324	9	2046316008
50	755364700	190797834	419778025	732552449	107961604	20	2005366288
1	641687516	166699992	871262288	661929188	996133669	1	1962076584
2	548804756	147036569	831131089	605798192	927575861	2	1917616888
3	479588066	131023645	298147707	560041594	872365887	3	1874327184
4	411565228	117772629	270891148	522500566	826140792	4	1831037480
5	360753736	106985881	248286380	49159872	788741511	5	1787747776
6	317975282	978435073	229379933	466374323	757752939	6	1744458072
7	282232884	901752056	214003384	445461813	734742606	7	1703508352
8	251984422	835490937	20146870	428752188	718084121	8	1664898616
9	225146173	775968069	190983194	414206400	708015708	9	1627458872
60	201801666	722522757	182502276	401526807	700702343	30	1592359112
1	179811233	672244064	174638086	388941444	693449625	1	1558429344
2	159457117	621594699	166538557	375050194	686147380	2	1516309632
3	139586158	571748264	158180805	359945450	676120942	3	1465999976
4	121329607	522387090	149485179	343833809	663193972	4	1408670368
5	104132568	473852928	140526817	326126163	646193259	5	1345490800
6	884071948	426739463	131311105	307839870	625893740	6	1277631264
7	742091942	382637674	122233521	290084708	603827897	7	1226151616
8	615062016	340790583	112924066	272496320	579856114	8	1191051856
9	504247385	300690036	103633059	255064265	553186116	9	1168822008
70	406185790	263259446	942563778	238082515	523809971	40	1160632064
1	321959727	227121704	849119469	220587443	491276562		
2	247934485	194787548	759319557	203438001	458148931		
3	189065599	164345948	673164962	186238913	423791485		
4	198145757	137309137	591187282	169172896	389117915		
5	992149306	112763663	513128535	152174473	358157342		
6	694605312	911243575	439855144	135346904	317301215		
7	465389310	719802000	371144527	118562038	281371541		
8	302857254	556337502	308252788	102205687	246479083		
9	199609364	420977175	251034800	865193427	212943561		
80	119080619	310229705	201067842	719895402	181838631		
1	762690028	223032309	157334828	588213556	152808326		
2	438165990	153890370	120902616	471301794	126217863		
3	233518460	104005678	904073079	370310511	102450708		
4	914739196	666180234	662145805	285086222	815802398		
5	348188241	415563068	472312720	214924851	637385640		
6	63788670	250057912	328047687	158347852	487248854		
7		142007010	219637468	113249539	361775403		
8		776372167	142616677	790203576	262003469		
9		425203380	896756112	534748687	184301558		
90	209694886	546298659	354070196	126769902			
1	108955718	318617585	224764039	840305080			
2	525799188	184668444	145083139	565562153			
3	234691920	104528320	908616160	372171368			
4	753461910	548732274	545409117	234827004			
5	217985870	260166388	295694935	134555321			
6	27061860	106085175	139171746	671778765			
7		35150250	54365710	280320640			

NOTE.—The local value of the figures is not assigned in these columns.

D  $\frac{2}{x+y}$ .  $x$  BEING THE YOUNGER AGE. (4½ PER CENT.)

<i>x</i>	-10	-9	-8	-7	-6	-5	-4	-3	-2	-1	<i>s</i>
18	98700	98083	102467	106862	111144	116173	118856	122601	126174	129713	18
9	101231	105761	110688	115645	120617	125451	129998	134268	138382	142415	9
20	106316	111374	116357	121776	127232	132703	138021	143023	147722	152246	20
1	108321	118832	119248	124684	130386	136228	142045	147779	153135	158193	1
2	108443	113716	119502	125187	130789	136890	143013	149181	155149	160703	2
3	106342	111737	117171	123133	128991	134763	141038	147358	153083	158553	3
4	102513	107827	113298	118808	124853	130793	136645	143008	149416	155440	4
5	97103	102403	107717	113125	118887	124725	130659	136506	142463	148294	5
6	98600	95764	100996	106232	111623	117050	123005	128858	134623	140495	6
7	84559	89474	94573	99741	104013	110234	115595	121476	127256	132950	7
8	78466	83386	88442	93482	98590	103701	108963	114263	120475	125793	8
9	72769	77592	82457	87457	92441	97492	102546	107740	112889	118737	9
10	67388	72066	76842	81661	86612	91548	96550	101556	106706	111898	10
1	62149	66726	71364	76093	80864	85768	90656	95809	100505	105494	1
2	57063	61401	65923	70605	75177	79891	84738	89564	94458	99355	2
3	52103	56210	60483	64938	69451	74053	78897	83449	88225	93048	3
4	47426	51224	55262	59463	63843	68280	72805	77370	82061	86738	4
5	42898	46477	50199	54156	58273	62565	66913	71344	75821	80419	5
6	38699	41973	45474	49145	52987	57015	61215	65449	69899	74145	6
7	34831	37822	41022	44444	48009	51787	55723	59827	63093	68226	7
8	31358	34045	36968	40096	43440	46919	50618	54445	58477	62541	8
9	28170	30614	33269	36115	39170	42437	46835	49443	53207	57138	9
10	26351	27504	29890	32472	35261	38244	41434	44751	48279	51950	10
1	22761	24737	26838	29167	31686	34407	37318	40430	43648	47110	1
2	20428	22227	24157	26208	28482	30942	33669	36442	39411	42043	2
3	18515	19965	21723	23609	25614	27836	30241	32838	35616	38456	3
4	16399	17903	19516	21234	23078	25058	27211	29561	32099	34915	4
5	14078	16045	17517	19095	20776	22581	24408	26624	28923	31407	5
6	13111	14365	15703	17144	18688	20834	22099	24076	26066	28307	6
7	11805	12767	13977	15279	16680	18183	19784	21503	23324	25373	7
8	10164	11220	12334	13513	14773	16127	17580	19123	20789	22554	8
9	8805-5	9768-3	10782	11851	12995	14194	15496	16892	18380	19976	9
10	7555-6	8410-6	9328-3	10298	11320	12403	13557	14801	16135	17555	10
1	6416-9	7172-7	7986-4	8857-8	9778-7	10749	11777	12874	14053	15321	1
2	5488-0	6168-3	6883-7	7664-6	8500-9	9384-7	10316	11303	12165	13498	2
3	4785-9	5330-9	5982-0	6698-6	7445-2	8257-6	9116-0	10021	10979	12001	3
4	4118-7	4647-5	5231-4	5870-4	6581-6	7308-2	8103-5	8845-9	9535-6	10774	4
5	3807-5	4086-8	4614-9	5194-8	5829-2	6515-8	7255-0	8046-7	8883-2	9784-7	5
6	3179-8	3614-8	4095-1	4624-2	5205-8	5841-0	6529-0	7269-7	8062-9	8901-1	6
7	2822-8	3221-3	3682-1	4148-6	4684-7	5273-3	5917-4	6614-4	7347-4	8169-3	7
8	2519-8	2887-9	3294-7	3745-7	4243-4	4791-7	5398-8	6063-5	6765-6	7533-0	8
9	2251-5	2595-7	2974-2	3394-1	3858-5	4371-1	4935-9	5556-1	6234-7	6969-1	9
10	2018-0	2334-2	2691-1	3083-5	3518-8	4000-3	4531-7	5117-4	5760-9	6430-9	10
1	1798-1	2098-7	2427-6	2798-7	3206-9	3659-6	4160-3	4713-0	5329-1	5900-8	1
2	1694-6	1865-7	2117-6	2518-8	2903-9	3327-4	3879-1	4316-7	4890-2	5322-1	2
3	1395-9	1651-0	1931-7	2254-7	2608-0	3009-7	3445-1	3931-6	4409-4	5063-8	3
4	1218-8	1440-2	1703-4	1983-0	2328-2	2690-7	3102-1	3654-4	4168-3	4611-2	4
5	1041-3	1246-8	1479-9	1750-9	2048-0	2390-4	2765-0	3187-7	3662-6	4168-2	5
6	884-07	1066-1	1276-4	1515-1	1792-9	2096-7	2447-3	2830-8	3263-6	3789-8	6
7	742-09	904-62	1090-9	1306-1	1550-3	1833-7	2146-5	2504-2	2896-6	3339-6	7
8	615-06	757-31	923-17	1113-3	1339-2	1582-1	1871-3	2189-5	2555-5	2956-0	8
9	504-25	625-68	770-36	939-08	1132-4	1355-7	1609-4	1903-5	2227-3	2569-6	9
10	406-19	510-65	633-61	780-15	951-01	1146-8	1373-1	1629-8	1927-7	2255-1	10
1	321-06	409-02	514-21	638-08	785-58	957-63	1154-8	1383-7	1641-2	1941-1	1
2	247-38	323-07	410-43	515-99	640-23	758-30	960-95	1158-1	1347-4	1646-9	2
3	188-07	247-42	322-41	409-58	514-93	638-91	786-87	958-96	1156-4	1384-6	3
4	138-15	187-50	245-37	319-73	408-19	510-65	633-61	780-15	951-01	1146-6	4
5	99-215	135-84	184-36	241-27	314-38	399-39	502-11	623-61	767-10	935-10	5
6	69-461	96-683	132-37	179-66	235-11	306-36	389-20	489-30	607-11	747-53	6
7	46-539	66-884	98-997	127-46	172-99	228-39	295-00	374-77	471-15	554-60	7
8	30-286	44-289	63-651	88-597	121-30	164-63	215-46	280-74	356-65	448-38	8
9	19-961	28-435	41-583	59-761	83-183	113-89	154-57	202-28	263-58	334-86	9
10	11-908	18-493	26-344	38-525	55-366	77-066	105-51	143-20	187-40	244-20	10
1	7-6269	10-876	18-890	24-060	35-185	50-567	70-388	96-365	130-79	171-16	1
2	4-9817	6-8574	9-7785	15-186	21-633	31-635	45-465	63-284	86-642	117-59	2
3	2-3352	3-8753	6-0649	8-6486	13-481	19-133	27-980	40-211	55-971	76-630	3
4	1-9147	2-0301	3-3690	5-2725	7-5188	11-676	16-633	24-324	34-956	46-668	4
5	3-5461	7-7812	1-7388	2-8773	4-5030	6-4213	9-9720	14-205	20-774	29-855	5
6	-0637	2-916	6-643	1-4622	2-4099	3-7715	5-3782	8-3522	11-898	17-399	6
7	-0520	-0280	-5340	-1-1852	-1-9669	-3-0783	-4-9865	-6-8168	-9-7107	-13-0004	7
8	-0416	-1908	-4269	-9475	-1-5725	-2-4610	-5-5094	-8-19201	-1-2238	-2-7380	8
9	-0324	-1-1454	-3-8381	-7-7392	-10-228	-15-228	-20-774	-26-855	-31-0078	-36-0047	9
10	-0248	-1-1137	-2-2551	-5-5661	-8-4195	-11-0842	-14-1890	-17-0842	-20-1427	-23-3168	10
1	-0184	-1-0139	-3-0638	-6-1427	-9-0103	-12-0073	-15-0073	-18-0073	-21-0073	-24-0073	11
2	-0139	-1-0139	-3-0638	-6-1427	-9-0103	-12-0073	-15-0073	-18-0073	-21-0073	-24-0073	12
3	-0139	-1-0139	-3-0638	-6-1427	-9-0103	-12-0073	-15-0073	-18-0073	-21-0073	-24-0073	13
4	-0139	-1-0139	-3-0638	-6-1427	-9-0103	-12-0073	-15-0073	-18-0073	-21-0073	-24-0073	14

D  $\frac{1}{x,y}$ . x BEING THE OLDER AGE. (4½ PER CENT.)

x	0	1	2	3	4	5	6	7	8	9	x
18	133253	138354	146380	157247							
9	146410	150405	156163	165233	177488						
20	156695	161090	165476	171010	181780	195273					
1	163012	167763	172468	177175	183957	194641	209078				
2	168043	171131	176118	181058	185599	193119	204335	219400			
3	165647	171098	176330	181449	186559	191650	198986	210544	226159		24
4	162096	167960	172478	178793	184094	189165	194327	201768	213445	229318	
5	155681	161920	167789	173301	178311	183816	188973	194123	201560	213267	5
6	147205	153574	159987	165475	170911	176148	181283	186368	191452	197780	6
7	139141	143376	151626	157703	163419	169787	173959	179029	184050	189073	
8	131416	137356	143899	149877	155883	161533	168840	171952	176963	181926	8
9	124387	129952	136004	142098	148207	154157	159734	164981	170036	174693	
30	117591	125185	128697	134461	140726	146776	152658	158191	163388	169394	
1	110906	116444	121984	127443	133377	139353	145345	151170	156949	161795	1
2	104396	109473	115043	120516	125909	131772	137678	143595	149350	154764	
3	97870	102835	107836	113323	118714	124026	129802	135618	141449	147118	
4	91477	96219	101101	106018	111412	116712	122193	127613	133331	139063	
5	85002	89646	94294	99078	103896	109182	114377	119495	125059	130663	
6	78883	83167	87711	92258	96939	101653	106925	111909	116915	122260	
7	72504	76900	81282	85724	90168	94743	99350	104485	109672	114236	
8	66646	70867	75164	79448	83788	88132	92604	97107	102048	106903	
9	61098	65145	69230	73428	77613	81853	86097	90465	94864	99691	9
40	55776	59652	63805	67593	71692	75778	79918	84061	88326	92622	
1	50993	54425	58208	62065	65957	69958	73943	77983	82026	86188	
2	46004	49502	53149	56841	60608	64408	68314	72207	76152	80100	
3	41676	44092	48580	51943	55553	59234	62949	66766	70570	74426	
4	37719	40739	43951	47202	50775	54304	57902	61533	65264	68983	
5	34064	38005	42060	45003	48272	51080	53132	56654	60206	63857	
6	30738	33398	36119	39011	42087	45286	48621	52000	55446	58923	
7	27542	29907	32437	35143	37957	40949	44063	47307	50595	53948	
8	24611	26628	28915	31361	33977	36697	39590	42600	45738	48916	
9	21672	23553	25587	27784	30135	32648	35263	38043	40934	43949	
50	19090	20700	22406	24430	26538	28783	31184	33691	36336	39098	
1	18670	19117	19656	21362	23207	25199	27333	29611	31962	34503	50
2	14704	15098	17387	18804	20601	22273	24184	26230	28418	30693	
3	13102	14283	15540	16990	18124	19014	21634	22492	25479	27604	
4	11777	12458	14016	15250	16575	17082	18542	21230	23053	25004	
5	10690	11695	12708	13918	15143	16458	17856	19405	21082	22892	
6	9784·4	10720	11718	12793	13846	15174	16493	17892	19444	21124	
7	9017·5	9912·3	10480	11872	12961	14128	15373	16707	18126	19699	
8	8364·9	9223·5	10139	11108	12143	13257	14451	15724	17089	18540	
9	7759·7	8606·4	9501·1	10444	11443	12508	13656	14886	16197	17603	
60	7225·2	8044·9	8623·7	9050·3	10628	11963	12963	14158	15453	16792	
1	6722·4	7154·2	8366·7	9279·6	10244	11261	12338	13487	14724	16051	
2	6215·9	6975·1	7796·7	8681·2	9628·4	10629	11884	12902	13994	15278	
3	5717·5	6435·9	7221·9	8072·5	8988·4	9969·1	11003	12098	13255	14489	
4	5223·9	5988·9	6640·1	7451·1	8328·7	9273·6	10285	11355	12481	13675	
5	4798·5	5348·1	6061·7	6823·4	7656·8	8558·6	9529·6	10589	11668	12826	
6	4267·4	4851·3	5405·8	6206·0	6985·7	7838·9	8762·3	9758·3	10821	11946	
7	3820·4	4368·6	4984·0	5623·5	6350·3	7148·1	8021·1	8943·9	9983·0	11072	
8	3407·9	3904·9	4458·1	5065·8	5738·8	6480·4	7294·7	8185·6	9140·8	10188	
9	3006·9	3406·6	3972·1	4532·9	5153·1	5837·7	6592·1	7420·4	8326·7	9307·4	
70	2632·6	3045·1	3610·7	4022·6	4590·5	5128·6	5911·9	6675·8	7514·6	8432·4	
1	2271·2	2650·9	3066·3	3535·1	4030·6	4622·5	5254·9	5953·1	6722·3	7567·0	70
2	1947·9	2279·1	2660·1	3076·9	3547·4	4064·6	4638·5	5273·1	5973·7	6745·6	
3	1643·5	1943·8	2274·4	2654·6	3070·6	3650·0	4056·2	4628·9	5262·3	5961·3	
4	1373·1	1629·8	1927·7	2255·6	2632·6	3045·1	3510·7	4022·6	4650·5	5218·6	
5	1127·6	1350·1	1602·6	1895·5	2217·8	2588·6	2994·3	3451·9	3955·3	4513·7	
6	911·24	1008·9	1315·8	1561·7	1847·1	2161·2	2522·5	2917·8	3363·9	3854·4	
7	719·80	877·44	1058·1	1268·9	1503·8	1778·6	2081·0	2429·0	2809·6	3239·1	
8	556·34	685·01	835·03	1007·0	1205·6	1431·1	1693·6	1980·4	2311·5	2673·7	
9	420·98	523·34	645·15	784·00	945·42	1132·0	1348·6	1589·2	1839·4	2170·3	
80	810·23	900·02	463·98	595·85	726·34	875·90	1048·7	1244·8	1473·3	1729·7	
1	223·03	283·34	356·21	441·98	544·20	663·39	799·97	957·81	1136·9	1344·7	
2	153·89	200·53	254·75	320·27	397·38	489·29	596·45	719·26	861·17	1022·2	
3	104·01	136·11	177·36	225·31	283·26	351·46	432·75	527·53	638·14	761·66	
4	66·618	90·417	118·33	154·18	195·87	246·25	305·54	376·21	458·60	563·08	
5	41·556	58·895	77·220	101·05	131·88	167·29	210·31	260·95	321·30	391·87	
6	25·004	34·608	47·653	64·677	84·640	110·23	140·11	176·14	218·56	269·11	
7	14·201	20·408	28·407	38·893	52·787	69·080	90·015	114·35	148·77	178·38	
8	7·7637	11·364	16·317	22·713	31·055	42·263	55·250	71·967	91·427	114·94	
9	4·2520	6·0371	8·8579	12·730	17·719	24·260	33·926	43·069	56·148	71·330	
90	2·0069	3·2565	4·6390	6·7840	9·7497	13·571	18·630	25·217	33·001	43·002	
1	1·0866	1·5537	2·4129	3·4372	5·0265	7·2239	10·055	13·766	18·684	24·451	
2	·5258	·8228	1·1734	1·6223	2·5959	3·7963	5·4558	7·5940	10·897	14·111	
3	·2344	·3894	·6095	·8693	1·3499	1·9229	2·8120	4·0413	5·6253	7·7015	
4	·0753	·1673	·2775	·4343	·6183	·9617	1·1701	2·0036	2·8795	4·0080	
5	·0217	·0489	·1085	·1801	·2819	·4020	·6243	·8803	1·3006	1·8691	
6	·0027	·0133	·0277	·0616	·1023	·1600	·2281	·3543	·5047	·7381	
7	·0013	·0058	·0003	·0138	·0293	·0486	·0761	·1086	·1687	·2403	
8	·0	·0001	·0001	·0005	·0013	·0013	·0029	·0048	·0325	·0506	
9	·0	·0	·0	·0	·0	·0	·0	·0	·0	·0	

D  $\frac{2}{x}$ .  $x$  BEING THE OLDER AGE. (4½ PER CENT.)

$x$	10	11	12	13	14	15	16	17	18	19	$x$
25	229084										
6	210326	225925									
7	196310	207712	223117								
8	186891	194045	205316	220543							
9	179900	184809	191883	203023	218087						
30	173302	178162	183025	190030	201068	215981					
1	166752	171612	176425	181240	188177	199107	213875				
2	159848	164745	169547	174302	179059	185913	196711	211501			
3	152450	157458	162283	167012	171896	176382	181333	188770	203143		
4	144637	149870	154803	159544	164196	168801	173407	180045	186513	204653	84
5	136281	141743	146980	151705	156835	160910	165423	169637	174443	184850	85
6	127842	133339	138683	143709	148430	152978	157436	161863	166329	172633	86
7	119587	124445	130317	135540	140453	145096	149511	153969	158144	162901	87
8	111686	116888	122125	127375	132430	137248	141792	146138	150945	155113	88
9	104434	109107	114188	119304	124434	129420	134111	138517	142761	146923	89
40	97334	101965	106527	111488	116484	121498	126361	130041	135248	139946	40
1	90379	94977	99496	103948	108759	113643	118550	123001	127770	131867	
2	84164	88257	92748	97160	101503	106235	110995	115767	120407	124771	
3	78285	82257	86257	90645	94985	99207	103827	108479	113143	117678	
4	72753	76524	80407	84817	88607	92423	96376	101463	106040	111070	4
5	67496	71184	74874	78673	82499	86696	90921	94845	98303	103713	5
6	62496	66058	69867	73279	76996	80741	84848	88866	92463	97147	6
7	57330	60807	64273	67784	71298	74915	78559	82555	86443	90553	7
8	52158	55428	58789	62140	65535	69483	72430	75953	79416	83614	88
9	47003	50118	53261	56490	59710	62973	66237	69597	72983	76085	9
50	41978	44895	47870	50879	53957	57092	60148	63266	66476	69709	50
1	37126	39861	42631	45456	48306	51235	54155	57114	60075	63123	1
2	33113	35630	38255	40918	43624	46360	49171	51973	54413	57455	2
3	29815	32165	34610	37159	39742	42378	45053	47763	50485	53244	3
4	27089	29258	31565	33964	36468	39000	41845	44192	46478	48543	4
5	24829	26899	29053	31344	33726	36210	38727	41293	43493	45454	5
6	22938	24379	26654	29112	31407	33794	36283	38406	41377	43371	56
7	21400	23238	25204	27306	29493	31818	34236	36759	39313	41918	7
8	20149	21889	23769	25780	27930	30166	32544	35018	37598	40210	8
9	19098	20755	22548	24484	26556	28770	31074	33524	36078	38729	9
60	18250	19800	21518	23377	25334	27532	29928	32216	34756	37398	60
1	17464	18980	20592	22379	24313	26399	28433	31021	33505	36146	1
2	16654	18120	19694	21368	23220	25226	27392	29709	32147	34746	2
3	15818	17243	18761	20390	22123	24041	26118	28361	30740	33126	3
4	14949	16320	17790	19357	21038	22824	24904	26947	29291	31737	4
5	14053	15361	16771	18231	19891	21618	23454	25489	27601	29409	5
6	13131	14387	15727	17170	18716	20364	22133	24013	26005	28230	6
7	12228	13436	14721	16092	17568	19151	20387	22047	24370	26703	7
8	11299	12474	13712	15023	16423	17929	19544	21296	23111	25374	8
9	10363	11494	12689	13948	15252	16708	18238	19881	21631	23510	9
70	9425·6	10495	11640	12850	14125	15476	16917	18469	20133	21906	70
1	8491·2	9391·3	10568	11721	12940	14424	15884	17035	18408	20274	1
2	7593 2	8520 6	9524 2	10605	11768	12945	14273	15638	17084	18403	2
3	6731 6	7577 5	8502 9	9504 5	10583	11737	12958	14243	15606	17059	3
4	5911 9	6675 8	7514 6	8432 4	9425 6	10495	11640	12850	14125	15476	4
5	5131 3	5813 0	6564 2	7389 0	8291 4	9268 0	10319	11445	12635	13449	5
6	4398 6	5000 4	5684 7	6306 7	7200 4	8079 9	9031 5	10056	11158	12113	6
7	3711 4	4235 4	4914 9	5454 6	6159 4	6933 4	7780 2	8696 5	9493 1	10740	7
8	3082 5	3532 0	4030 7	4582 2	5190 9	5861 7	6508 2	7274 1	8276 3	9115 1	8
9	2510·3	2894 2	3316 2	3784 4	4302 1	4873 7	5303·5	6195 0	6861·6	7770 4	9
80	2010·7	2325·7	2681 3	3072·3	3508·0	3985·7	4515·3	5098 7	5739·4	6440·6	80
1	1573 3	1836 4	2124 1	2448 9	2906 0	3202 1	3640 3	4123 9	4636 8	5241 9	1
2	1209 0	1414 6	1651 1	1909 8	2201 8	2522 9	2879 1	3273 6	3707 8	4146 9	2
3	904 07	1069 3	1251 1	1460 3	1689 1	1947 4	2231 4	2546 4	2894 8	3289 8	3
4	662·15	785 95	929·61	1057·7	1269 6	1463·4	1692 9	1930·8	2213·7	2516 6	4
5	472 31	565 50	671 24	783 93	923 99	1084 2	1254 1	1445 9	1656 7	1840 6	5
6	328 05	395 59	473 64	562 21	664 96	778 03	908 11	1050 4	1210 0	1347 6	6
7	219 64	267 74	322 87	386 57	453 85	542 73	635 00	741 16	857 30	948 37	7
8	142 63	175 60	214 06	258 13	309 07	366 85	483 91	507 68	592 56	645 41	8
9	69 676	111 27	137 00	167 01	201 39	241 13	286 21	333 53	386 09	463 31	9
90	54 630	68 680	85 217	104 93	127 91	154 24	184 67	219 20	259 27	303 35	90
1	31 862	40 477	50 887	63 140	77 748	94 769	114 29	136 63	162 42	182 10	1
2	18 467	24 063	30 670	38 432	47 686	59 715	71 574	86 311	103 34	123 66	2
3	10 463	13 679	17 825	22 645	28 408	35 323	43 403	53 018	63 934	76 540	3
4	5·4873	7 4476	9 7464	12 700	16 134	20 244	25 198	30 948	37 775	46 553	4
5	2·6017	3 5619	4·8344	6 3268	8 2440	10 473	13 167	16 337	20 115	24 111	5
6	1·0609	1·4766	2 0216	2 7439	3 5908	4 6790	5·0442	7 4730	9 2723	11 417	6
7	·3515	·5051	·7031	·9636	1·3066	1 7099	2·2241	2 8306	3 5546	4 4154	7
8	·0721	·1054	·1515	2109	·2888	·3919	·5129	·6944	·8441	1 0676	8
9	·0168	·0240	·0351	·0505	·0703	·0963	·1306	·1709	·2223	·2830	9

**D <sub>2</sub>  
x being the older age. (4½ per cent.)**

x	20	21	22	23	24	25	26	27	28	29	x
55	200537										
6	182660	196208									
7	168721	178521	191762								
8	158533	164013	174491	187433							
9	151042	155164	161104	170461	183104						
40	143448	147471	151496	157295	166481	178775					
1	134011	139975	143600	147828	152466	162401	174446				
2	128469	132818	136489	140523	144357	149883	158589	170351			
3	121948	125049	126908	134591	137338	141046	149486	154094	166460		
4	115031	119200	123116	126888	130597	134249	137913	145192	151509	162746	44
5	108218	112550	116630	120461	124152	127770	131354	134838	140104	148241	5
6	101542	105908	110152	114145	117894	121306	125048	128555	132063	137118	6
7	94581	98798	103045	107175	111060	114708	118223	121668	125080	128494	7
8	87355	91423	95520	99626	103819	107375	110902	114300	117681	120930	8
9	80344	83939	87948	91786	95730	99567	103176	106665	109830	113031	9
50	73255	76741	80174	83908	87668	91437	95101	98548	101786	104904	50
1	66193	69501	72770	76131	79976	83246	86825	90305	93578	96653	1
2	60580	63528	66758	69934	73063	76466	79892	83237	86366	89807	2
3	55004	58946	61707	64847	67932	70973	74277	77605	80941	84185	3
4	52250	54959	57747	60556	63637	66694	69647	72891	76158	79481	4
5	40198	51884	54574	57343	60131	63191	66197	69159	72380	75623	5
6	40637	42925	51980	54684	57453	60253	63318	66331	69299	72526	6
7	44540	47247	49940	52688	55399	58210	61041	64146	67198	70205	7
8	42875	45564	48327	51081	53871	56664	59539	62485	65511	68733	8
9	41421	44186	46935	49781	52018	55493	58370	61351	64514	67586	9
60	40153	42943	45789	48660	51611	54553	57533	60515	63586	66678	60
1	38804	41759	44661	47621	50607	53675	56734	59834	62936	66129	1
2	37505	40356	43328	46340	49411	52509	55698	58867	62088	65302	2
3	35994	38632	41784	44861	47979	51159	54367	57663	60949	64280	3
4	34383	37137	40064	43110	46285	49502	52782	56092	59463	62884	4
5	32613	36332	39162	41170	44300	47563	50868	54239	57640	6135	5
6	30784	33889	36173	39070	42150	45354	48694	52078	55530	59011	6
7	29008	31469	34164	37014	39978	43129	46408	49826	53289	56820	7
8	27250	29604	32145	34865	37773	40798	44014	47360	50848	54382	8
9	25506	27719	30114	32899	35466	38424	41501	44772	48176	51724	9
70	23808	25830	28071	30496	33115	35916	38912	42028	45341	48788	70
1	22059	23974	26010	28287	30700	33345	36167	39183	42321	45457	1
2	20344	22135	24057	26100	28345	30815	33461	36292	39319	42467	2
3	18424	20302	22089	24077	26046	28306	30751	33392	36217	39237	3
4	16917	18409	20133	21906	23808	25830	28071	30496	33115	35916	4
5	15217	16034	18161	19797	21540	23410	25398	27602	29946	32561	5
6	15335	16429	18210	19787	20292	20990	22813	24750	26898	29221	6
7	14886	15833	16279	17400	18569	19746	20212	21967	23832	25900	7
8	10241	11283	12403	13589	14854	16217	17679	19235	20905	22680	8
9	8651·9	95936·0	10594	11645	12758	13946	15226	16598	18059	19627	9
80	7199·0	8015·7	8890·3	9814·5	10788	11820	12921	14106	15377	16731	80
1	5882·1	6575·0	7320·9	8119·7	8963·8	9853·3	10796	11801	12884	14044	1
2	4713·0	5298·6	5911·5	6592·3	7300·4	8059·4	8859·1	9708·4	10610	11584	2
3	3703·1	4168·4	4677·5	5228·4	5821·6	6456·8	7128·0	7835·4	8584·7	9344·1	3
4	2830·9	3219·3	3623·8	4066·3	4545·3	5061·0	5613·2	6196·7	6811·6	7463·1	4
5	2140·3	2434·8	2749·4	3094·9	3472·9	3881·9	4322·3	4793·9	5292·3	5817·5	5
6	1583·5	1800·1	2039·3	2302·8	2592·3	2908·7	3251·4	3620·2	4015·3	4432·6	6
7	1139·5	1299·4	1469·9	1664·4	1879·5	2115·6	2374·0	2653·6	2954·7	3277·1	7
8	790·20	905·44	1033·3	1174·6	1330·7	1502·6	1691·4	1898·0	2121·6	2392·3	8
9	534·76	616·51	706·41	808·13	916·43	1033·2	1172·3	1319·6	1480·8	1635·2	9
90	354·07	409·55	472·10	541·02	617·40	701·87	795·12	897·86	1010·7	1134·1	90
1	234·76	263·34	303·45	349·84	400·86	467·45	520·04	589·13	665·26	748·85	1
2	145·08	169·75	198·13	229·18	264·23	302·75	345·49	392·76	444·94	502·43	2
3	90·862	107·47	125·74	146·76	169·76	195·73	224·26	255·92	290·93	329·68	3
4	54·541	64·739	76·673	89·591	104·56	120·96	139·46	169·78	182·84	207·29	4
5	29·569	35·404	42·023	49·704	58·156	67·879	78·515	86·519	103·72	118·36	5
6	13·917	16·783	20·094	23·851	28·211	33·007	38·626	44·562	51·375	58·867	6
7	5·4866	6·6273	7·9018	9·5886	11·350	13·484	15·718	18·346	21·220	24·465	7
8	1·3246	1·6310	1·9883	2·3975	2·8706	3·4073	4·0301	4·7153	5·5038	6·3661	8
9	·3558	·4415	·5436	·6627	·7991	·9568	1·1358	1·3434	1·5718	1·8346	9

**D<sub>x,y</sub><sup>2</sup>. X BEING THE OLDER AGE. (4½ PER CENT.)**

<i>x</i>	80	81	82	83	84	85	86	87	88	89	<i>y</i>
45	159236										
6	145082	155843									
7	133413	141161	151631								
8	124231	128096	136478	146600							
9	116201	119372	123942	131141	140867						
50	107943	110990	114019	118983	125259	134549					
1	99613	102517	105392	109268	112413	118941	127763				
2	92768	95800	98386	101145	103906	107883	114140	122615			
3	87237	90102	92863	95569	98250	100831	104795	110881	119105		
4	82614	85608	88421	91180	93786	96418	99497	102839	108813	116882	54
5	78874	82035	85009	87901	90461	93129	95741	98353	102118	108449	55
6	75775	79033	82201	85180	87978	90674	93116	95834	98558	102324	56
7	73474	76766	80067	83276	86294	89129	91860	94537	97188	99941	78
8	71808	75152	78520	81896	85178	88265	91164	93958	96698	99448	78
9	70802	73970	77414	80883	84360	87741	90921	93908	96788	99666	9
60	70070	73404	76689	80260	83856	87461	90966	94263	97340	100543	60
1	69345	72737	76340	79756	83470	87210	90960	94605	98454	101254	1
2	68615	71951	75612	79210	82754	86608	90493	94379	98161	101719	5
3	67612	71043	74497	78288	82013	85683	89973	93890	97718	101634	5
4	66319	69758	73297	76861	80773	84415	88401	92518	96603	100419	4
5	64619	68150	71683	75320	79893	83001	86950	90841	95071	98331	5
6	62590	66157	69771	73389	77112	80862	84676	88019	92002	97333	5
7	60388	64044	67694	71393	75064	78904	82741	86951	91098	95164	7
8	57986	61621	65358	69083	72867	76634	80523	84458	88734	92668	8
9	55319	58985	62683	66484	70273	74113	77955	81910	85893	90203	9
70	52381	56021	59734	63479	67329	71166	75054	78945	82950	86944	70
1	49128	52746	56412	60150	63922	67798	71661	75577	79445	83528	1
2	45815	49298	52929	56607	60353	64143	68032	71909	75438	79770	2
3	42379	45720	49196	52819	56460	60233	64010	67893	71761	75683	3
4	38912	42028	45541	48788	52381	56021	59734	63479	67329	71166	4
5	35316	38261	41325	44583	47973	51505	55084	58735	62418	66203	5
6	31730	34415	37285	40270	43446	46748	50191	53679	57238	60825	6
7	28137	30553	33133	35902	38777	41834	45014	48429	51888	55113	7
8	24648	26777	29076	31536	34168	36902	39813	42938	45993	49189	8
9	21294	23142	25141	27299	29608	32078	34647	37379	40220	43183	9
80	18184	19728	21440	23292	25292	27432	29719	32099	34630	37263	80
1	15281	16608	18013	19581	21273	23100	25054	27143	29317	31629	1
2	12627	13739	14932	16200	17608	19128	20789	22526	24445	26559	2
3	10245	11168	12151	13207	14328	15371	16916	18369	19923	21545	3
4	8168°0	8906°5	9708°9	10564	11481	12456	13837	14706	15959	17320	4
5	6373°9	6967°3	7606°6	8291°9	9021°9	9805°3	10638	11561	12560	13638	5
6	4872°5	5338°5	5835°6	6371°0	6945°0	7556°4	8212°6	8910°1	9883°1	10520	6
7	3617°8	3976°7	4357°1	4762°8	5199°8	5663°2	6167°3	6702°8	7272°1	7943°0	7
8	2620°0	2892°4	3179°4	3483°5	3807°9	4157°2	4531°7	4930°8	5338°9	5814°1	8
9	1843°0	2044°1	2256°6	2480°5	2717°8	2970°6	3245°6	3535°6	3846°9	4181°0	9
90	1287°7	1411°5	1565°5	1723°3	1809°8	2031°4	2275°3	2464°0	2707°8	2946°8	90
1	840°31	939°29	1045°8	1160°0	1280°5	1407°6	1542°3	1685°8	1840°5	2006°3	1
2	595°56	634°64	709°39	789°86	876°05	987°13	1063°1	1164°8	1273°2	1360°0	2
3	372°17	418°93	470°10	525°47	585°08	648°93	716°39	787°47	862°79	943°13	3
4	234°83	265°17	298°49	334°95	374°39	416°87	462°38	510°43	561°07	614°74	4
5	134°56	152°43	173°13	193°76	217°42	243°03	270°60	300°18	351°33	384°21	5
6	67°178	76°369	86°515	97°695	108°97	123°40	137°93	163°58	176°34	184°06	6
7	28°032	31°989	36°366	41°198	46°521	52°367	58°768	65°694	73°198	81°116	7
8	7°3394	8°4098	9°5968	10°910	12°359	13°956	15°710	17°629	19°705	21°941	8
9	2°1220	2°4465	2°8032	3°1989	3°6366	4°1198	4°6521	5°2367	5°8763	6°5684	9

NOTE.—The summation of the values on this page is not given, but may easily be made if required in any extreme case.

**DIFFERENCE OF AGE Ten YEARS.**  
(Female the elder).

x	N <sub>x'y</sub>	N <sub>x'y</sub> <sup>-2</sup>	D <sub>x'y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
18	62081	18299	18074	11.221	3.307
9	56921	17362	19380	11.031	3.365
20	52122	16350	20838	10.861	3.407
1	47670	15287	22463	10.708	3.434
2	43543	14204	24233	10.552	3.442
3	39738	13119	26282	10.444	3.448
4	36229	12056	28497	10.324	3.436
5	32998	11031	30948	10.212	3.414
6	30025	10060	33635	10.099	3.384
7	27292	91537	36595	9.988	3.350
8	24782	83101	39820	9.868	3.309
9	22479	75254	43417	9.760	3.267
30	20367	67977	47350	9.644	3.219
1	18433	61239	51706	9.531	3.166
2	16664	55024	56545	9.423	3.111
3	15048	49318	61881	9.312	3.052
4	13574	44107	67815	9.205	2.991
5	12229	39365	74937	9.164	2.950
6	11005	35075	81967	9.020	2.875
7	98903	31205	89748	8.876	2.801
8	88770	27722	98686	8.760	2.736
9	79562	24588	10860	8.640	2.670
40	71206	21771	11968	8.522	2.606
1	63631	19286	13200	8.399	2.539
2	56773	16960	14583	8.279	2.473
3	50571	14917	16125	8.155	2.405
4	44969	13086	17849	8.027	2.336
5	39913	11446	19778	7.894	2.264
6	35355	99780	21941	7.757	2.189
7	31252	86669	24372	7.617	2.112
8	27562	75064	27103	7.470	2.034
9	24248	64900	30173	7.317	1.958
50	21274	56094	33625	7.153	1.886
1	18608	48541	37506	6.979	1.821
2	16220	42124	41872	6.792	1.764
3	14083	36636	46809	6.592	1.715
4	12173	31900	52418	6.382	1.672
5	10476	27784	58828	6.163	1.634
6	89651	24177	66200	5.935	1.601
7	76270	20997	74733	5.700	1.569
8	64462	18174	84686	5.459	1.539
9	54087	15654	96391	5.214	1.509
60	45035	13403	11047	4.975	1.481
1	37186	11385	12739	4.737	1.450
2	30427	95868	14796	4.502	1.418
3	24654	79922	17322	4.271	1.384
4	19767	65964	20465	4.045	1.350
5	15664	53831	24369	3.817	1.312
6	12257	43418	29355	3.598	1.275
7	94586	34577	35729	3.379	1.235
8	71866	27156	44015	3.163	1.195
9	53681	21006	54988	2.952	1.155
70	39364	15963	69846	2.749	1.115
1	28258	11901	90048	2.545	1.072
2	19837	86819	11874	2.356	1.031
3	13588	62026	16002	2.174	0.993
4	90693	43119	22131	2.007	0.954
5	59042	29304	31596	1.865	0.926
6	37466	19382	46346	1.736	0.898
7	23169	12436	69945	1.621	0.870
8	13946	77825	10842	1.512	0.844
9	81079	47539	17129	1.389	0.814
80	45432	27578	28053	1.275	0.774
1	24297	15670	47315		
2	11837	80436	80257		
3	48220	86619	14254		
4	15563	13267	30621		
5	81089	41198	80293		
6	00000	63788	82166		

**DIFFERENCE OF AGE Nine Years.**  
(Female the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub> <sup>-2</sup>	D <sub>x'y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
18	66123	19502	17104	11.310	3.336
9	60667	18521	18328	11.119	3.395
20	55589	17464	19694	10.948	3.439
1	50875	16350	21215	10.793	3.469
2	46510	15212	22907	10.654	3.485
3	42469	14074	24746	10.509	3.483
4	38747	12957	26869	10.411	3.481
5	35317	11879	29158	10.298	3.464
6	32161	10855	31681	10.189	3.439
7	29257	98971	34440	10.076	3.409
8	26589	90023	37480	9.966	3.374
9	24139	81685	40813	9.852	3.334
20	21892	73926	44495	9.741	3.289
1	19832	66719	48544	9.627	3.239
2	17946	60046	53032	9.517	3.184
3	16222	53906	58013	9.411	3.127
4	14648	48285	63506	9.302	3.066
5	13211	43163	69611	9.196	3.005
6	11901	38515	76352	9.087	2.941
7	10709	34318	83855	8.980	2.878
8	96237	30536	92157	8.869	2.814
9	86370	27131	10135	8.754	2.750
40	77404	24069	11153	8.633	2.684
1	69269	21319	12293	8.513	2.621
2	61894	18846	13559	8.392	2.555
3	55219	16623	14980	8.272	2.490
4	49182	14627	16567	8.148	2.423
5	43730	12836	18340	8.020	2.354
6	38810	11232	20325	7.888	2.283
7	34376	97953	22552	7.752	2.209
8	30384	85196	25050	7.611	2.134
9	26793	73976	27853	7.463	2.060
50	23567	64209	30997	7.305	1.990
1	20671	55799	34524	7.136	1.926
2	18072	48626	38483	6.955	1.871
3	15744	42468	42948	6.762	1.824
4	13661	37137	48005	6.558	1.783
5	11801	32489	53769	6.345	1.747
6	10145	28402	60372	6.125	1.715
7	86739	24788	67990	5.987	1.685
8	73124	21566	76834	5.818	1.657
9	61655	18679	87192	5.376	1.629
60	51598	16083	99426	5.130	1.599
1	42841	13749	11420	4.892	1.570
2	35267	11650	13203	4.656	1.538
3	28763	97847	15376	4.423	1.505
4	23224	81337	18055	4.193	1.469
5	18551	66935	21399	3.970	1.432
6	14640	54467	25569	3.743	1.393
7	11405	43806	30912	3.526	1.354
8	87582	34760	37780	3.309	1.313
9	66194	27187	46754	3.095	1.271
70	49160	20930	58705	2.886	1.229
1	35822	15824	75976	2.722	1.202
2	25538	11734	97237	2.483	1.141
3	17792	85031	12909	2.296	1.098
4	12086	60289	17527	2.118	1.057
5	79947	41539	24440	1.954	1.015
6	51543	27955	35206	1.815	0.984
7	32370	18286	52156	1.688	0.954
8	19799	11598	79546	1.575	0.923
9	11781	71692	12472	1.469	0.894
80	67661	43257	19942	1.349	0.863
1	37438	24764	33087		
2	19767	13888	56591		
3	95039	70303	97432		
4	38161	31550	17582		
5	12132	11249	38417		
6	23854	34369	10260		
7	00000	52062	41922		

DIFFERENCE OF AGE Eight Years.  
(Female the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
18	70367	20753	16188	11.391	3.359
9	64602	19728	17345	11.205	3.422
20	59233	18621	18625	11.032	3.468
1	54245	17458	20050	10.876	3.500
2	49623	16265	21635	10.736	3.519
3	45348	15070	23393	10.608	3.525
4	41396	13899	25299	10.473	3.516
5	37758	12766	27492	10.380	3.510
6	34408	11688	29848	10.270	3.489
7	31325	10679	32439	10.162	3.464
8	28490	97300	35278	10.049	3.433
9	25886	88486	38399	9.940	3.398
30	23495	80240	41826	9.827	3.356
1	21303	72556	45617	9.718	3.310
2	19295	65420	49787	9.606	3.257
3	17457	58828	54409	9.498	3.201
4	15777	52779	59536	9.393	3.142
5	14243	47253	65188	9.285	3.080
6	12844	42233	71466	9.179	3.018
7	11568	37686	78396	9.069	2.954
8	10407	33584	86109	8.961	2.892
9	93502	29887	94642	8.849	2.829
40	83895	26561	10409	8.733	2.765
1	75166	23572	11456	8.611	2.700
2	67246	20888	12627	8.491	2.638
3	60067	18472	13929	8.367	2.573
4	53570	16300	15891	8.245	2.509
5	47695	14348	17023	8.119	2.442
6	42389	12597	18847	7.989	2.374
7	37603	11026	20891	7.856	2.303
8	33289	96287	23180	7.716	2.232
9	29404	83953	25743	7.569	2.161
50	25909	73171	28613	7.413	2.094
1	22767	63843	31827	7.246	2.032
2	19944	55857	35426	7.065	1.979
3	17411	46973	39457	6.870	1.932
4	15141	42991	44047	6.669	1.894
5	13110	37760	49242	6.456	1.859
6	11298	33145	55178	6.234	1.829
7	96848	29050	62004	6.005	1.801
8	82542	25387	69901	5.770	1.775
9	69902	22093	79111	5.530	1.748
60	58783	19118	89994	5.290	1.721
1	49053	16427	10278	5.042	1.688
2	40604	14000	11835	4.805	1.657
3	33315	11882	13720	4.571	1.630
4	27076	99503	16026	4.339	1.595
5	21779	82469	18879	4.112	1.557
6	17325	67670	22452	3.890	1.519
7	13611	54906	26925	3.665	1.478
8	10552	43997	32686	3.449	1.438
9	80597	34766	40132	3.235	1.395
70	60563	27062	49914	3.023	1.351
1	44694	20726	63018	2.817	1.306
2	32343	15584	80966	2.619	1.262
3	22884	11480	10571	2.419	1.214
4	15811	82555	14139	2.236	1.167
5	10645	58017	19355	2.060	1.123
6	69728	39581	27233	1.899	1.078
7	44487	26345	39619	1.763	1.044
8	27628	17035	59315	1.639	1.010
9	16703	10670	92531	1.546	0.987
80	98159	65114	14520	1.425	0.945
1	55644	38770	23521		
2	30375	21880	39574		
3	15819	12102	68700		
4	74978	60368	12018		
5	29643	26678	22058		
6	92730	93396	49092		
7	17949	27964	13372		
8	00000	41623	55714		

DIFFERENCE OF AGE Seven Years.  
(Female the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
18	74844	22241	15323	11.468	3.408
9	68753	21173	16416	11.286	3.476
20	63079	20016	17625	11.118	3.528
1	57806	18799	18963	10.962	3.565
2	52915	17553	20447	10.820	3.589
3	48389	16301	22093	10.691	3.601
4	44207	15069	23915	10.572	3.604
5	40344	13881	25885	10.443	3.593
6	36791	12563	28144	10.354	3.536
7	33519	11501	30563	10.244	3.515
8	30509	10503	33225	10.137	3.490
9	27742	95686	36138	10.025	3.458
30	25201	86940	39353	9.917	3.421
1	22869	78774	42882	9.807	3.378
2	20731	71165	46786	9.699	3.330
3	18774	64114	51080	9.590	3.275
4	16983	57620	55837	9.483	3.217
5	15346	51674	61113	9.378	3.158
6	13852	46259	66925	9.270	3.096
7	12489	41344	73379	9.164	3.034
8	11247	36900	80502	9.054	2.971
9	10116	32890	88431	8.946	2.908
40	90875	29279	97203	8.833	2.846
1	81522	26031	10692	8.716	2.783
2	73024	23115	11768	8.593	2.720
3	65315	20494	12972	8.473	2.658
4	58327	18133	14311	8.347	2.595
5	52004	16010	15815	8.224	2.532
6	46288	14100	17494	8.098	2.467
7	41126	12386	19372	7.967	2.399
8	36468	10858	21473	7.830	2.331
9	32270	95065	23821	7.687	2.265
50	28489	63214	26446	7.534	2.201
1	25085	72916	29379	7.470	2.142
2	22023	64059	32657	7.192	2.092
3	19271	56394	36335	7.002	2.049
4	16801	49707	40483	6.802	2.012
5	14588	43837	45181	6.591	1.981
6	12609	38642	50534	6.372	1.953
7	10844	34018	56669	6.145	1.928
8	92756	29869	63747	5.913	1.904
9	78861	26124	71971	5.676	1.880
60	66607	22730	81601	5.435	1.855
1	55851	19646	93973	5.248	1.829
2	46463	16847	10652	4.949	1.795
3	38332	14329	12299	4.714	1.762
4	31339	12074	14301	4.482	1.727
5	25372	10081	16758	4.252	1.689
6	20323	83306	19808	4.026	1.650
7	16094	68155	23643	3.805	1.611
8	12582	55094	28471	3.582	1.569
9	97014	43961	34721	3.368	1.526
70	73674	34570	42843	3.156	1.481
1	55010	26768	53581	2.947	1.434
2	40316	20388	68053	2.744	1.387
3	28955	15228	88022	2.549	1.340
4	20318	11133	11578	2.352	1.289
5	13913	79353	15614	2.172	1.239
6	92768	55226	21567	2.001	1.191
7	60138	37260	80646	1.843	1.142
8	37944	24514	45057	1.710	1.105
9	23287	15654	68227	1.589	1.068
80	13899	96778	10653	1.481	1.031
1	80601	58253	17125		
2	45054	34193	28132		
3	24239	19007	48042		
4	12438	10359	84723		
5	58057	50863	15077		
6	22579	22090	28187		
7	69497	75680	63983		
8	13228	22277	17772		
9	00000	32474	75599		

DIFFERENCE OF AGE Six Years.  
(Female the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
18	79560	23403	14506	11·541	3·395
9	73124	22292	15538	11·362	3·464
20	67130	21086	16681	11·198	3·517
1	61557	19813	17944	11·046	3·555
2	56386	18509	19837	10·903	3·579
3	51596	17202	20880	10·772	3·592
4	47169	15912	22587	10·654	3·594
5	43082	14663	24470	10·542	3·588
6	39309	13476	26499	10·416	3·571
7	35838	12360	28817	10·327	3·562
8	32644	11311	31301	10·218	3·540
9	29706	10325	34039	10·112	3·515
80	27006	94006	37036	10·002	3·482
1	24527	85345	40345	9·895	3·443
2	22254	77259	43979	9·787	3·398
3	20170	69741	48001	9·682	3·348
4	18263	62796	52421	9·574	3·292
5	16518	56412	57316	9·467	3·233
6	14924	50584	62741	9·363	3·174
7	13469	45286	68717	9·255	3·112
8	12142	40486	75351	9·149	3·051
9	10932	36142	82674	9·038	2·988
40	98310	32225	90824	8·929	2·927
1	88294	28698	99841	8·815	2·865
2	79189	25580	10982	8·697	2·804
3	70917	22682	12089	8·573	2·742
4	63413	20120	13327	8·451	2·681
5	56613	17812	14704	8·324	2·619
6	50460	15735	16252	8·201	2·557
7	44898	13866	17981	8·073	2·493
8	59876	12198	19911	7·940	2·429
9	85344	10721	22066	7·799	2·366
50	81258	94214	24471	7·649	2·306
1	77575	82894	27154	7·488	2·251
2	72458	73115	30146	7·313	2·204
3	71272	64614	33496	7·125	2·164
4	18589	57169	37265	6·927	2·130
5	16181	50607	41525	6·719	2·101
6	14024	44778	46367	6·503	2·076
7	12097	39573	51900	6·278	2·054
8	10301	34888	58263	6·002	2·033
9	88571	30645	65635	5·813	2·011
60	75101	26786	74237	5·575	1·989
1	63246	23267	84355	5·335	1·963
2	52868	20060	96354	5·094	1·933
3	43834	17157	11069	4·852	1·899
4	36033	14549	12819	4·619	1·865
5	29346	12222	14953	4·388	1·828
6	23658	10174	17583	4·160	1·789
7	18864	83823	20859	3·935	1·748
8	14864	68320	25000	3·671	1·708
9	11558	54991	30242	3·495	1·663
70	88599	43667	37067	3·284	1·619
1	66855	34157	45991	3·075	1·571
2	49572	26301	57861	2·868	1·522
3	36056	19899	73982	2·667	1·472
4	25683	14750	96406	2·476	1·422
5	17862	10688	12786	2·284	1·367
6	12114	75442	17399	2·108	1·313
7	79934	51931	23752	1·899	1·233
8	51242	34632	34853	1·785	1·207
9	31947	22502	51827	1·656	1·166
80	19357	14183	79432	1·538	1·127
1	11398	86466	12564		
2	65162	51281	20483		
3	35881	29648	34152		
4	19005	16217	59257		
5	95986	86984	10631		
6	44083	41954	19270		
7	16862	17855	36736		
8	51013	60030	85082		
9	95444	17334	24114		
90	00000	24871	10477		

Difference of Age Five Years.  
(Female the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
18	84527	24796	13734	11·609	3·405
19	77729	23645	14710	11·434	3·478
20	71396	22390	15790	11·273	3·535
1	65507	21063	16983	11·125	3·577
2	60043	19701	18299	10·987	3·605
3	54979	18332	19747	10·857	3·620
4	50294	16984	21347	10·736	3·626
5	45967	15676	23110	10·623	3·623
6	41975	14429	25049	10·514	3·614
7	38290	13259	27133	10·389	3·598
8	34901	12156	29514	10·301	3·588
9	31783	11119	32070	10·193	3·566
30	28917	10144	34884	10·087	3·539
1	26283	92289	37969	9·979	3·504
2	23866	83713	41379	9·876	3·464
3	21650	75724	45121	9·769	3·417
4	19629	68318	49260	9·665	3·365
5	17761	61490	53809	9·557	3·309
6	16062	55234	59021	9·480	3·260
7	14510	49582	64421	9·347	3·191
8	13093	44354	70563	9·239	3·130
9	11800	39662	77383	9·131	3·069
50	34225	10629	22669	7·758	2·409
1	30245	93890	25127	7·600	2·359
2	26656	83141	27862	7·427	2·316
3	23422	73757	30920	7·242	2·281
4	20511	65499	34353	7·046	2·250
5	17895	58193	38225	6·840	2·224
6	15548	51677	42615	6·626	2·202
7	13448	45836	47619	6·404	2·183
8	11574	40563	53360	6·176	2·164
9	99071	35771	59989	5·943	2·146
60	84300	31400	67701	5·707	2·126
1	71270	27400	76741	5·469	2·103
2	59831	23740	87483	5·234	2·077
3	49844	20413	10013	4·991	2·044
4	41177	17406	11538	4·751	2·008
5	37316	14715	13404	4·519	1·972
6	27343	12325	15689	4·290	1·934
7	21952	10228	18515	4·063	1·894
8	17408	83944	22056	3·840	1·851
9	13642	68123	26556	3·623	1·809
70	10545	54566	32286	3·405	1·762
1	80320	43098	39790	3·196	1·715
2	60185	33522	49665	2·989	1·665
3	44288	25639	62904	2·786	1·613
4	31947	19250	81030	2·589	1·560
5	22554	14143	10646	2·401	1·506
6	15535	10149	14247	2·213	1·446
7	10428	70856	19579	2·042	1·387
8	68048	48217	27609	1·879	1·331
9	43104	31754	40090	1·728	1·273
80	26531	20365	60339	1·601	1·229
1	15858	12658	93687		
2	92031	76016	15025		
3	51816	44381	24866		
4	28076	25248	42123		
5	14625	13572	74343		
6	72638	71512	13585		
7	32814	33797	25110		
8	12332	14128	48822		
9	36645	46525	11538		
90	67235	13214	33420		
1	00000	18427	14873		

**DIFFERENCE OF AGE Four YEARS.**  
(Female the elder.)

$x$	$N_{x'y}$	$N_{x'y}^2$	$D_{x'y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
$a_{x'y}$	$a_{x'y}^2$			$a_{x'y}$	$a_{x'y}^2$
18	89758	26230	13004	11.672	3.411
9	82578	25040	13927	11.501	3.487
20	75888	23740	14948	11.344	3.549
1	69668	22360	16076	11.200	3.595
2	68894	20939	17319	11.066	3.626
3	58543	19509	18687	10.940	3.646
4	53589	18098	20188	10.819	3.654
5	49011	16732	21841	10.704	3.654
6	44784	15425	23658	10.595	3.649
7	40885	14195	25649	10.487	3.641
8	37287	13039	27790	10.362	3.624
9	33980	11950	30238	10.275	3.613
30	30937	10924	32866	10.168	3.590
1	28141	99589	35764	10.064	3.562
2	25573	90523	38942	9.959	3.525
3	23217	82049	42454	9.857	3.483
4	21058	74180	46305	9.751	3.435
5	19080	66899	50565	9.648	3.383
6	17270	60208	55243	9.540	3.326
7	15615	54086	60419	9.434	3.268
8	14103	48514	66152	9.329	3.209
9	12723	43452	72467	9.220	3.149
40	11465	38869	79478	9.112	3.089
1	10318	34725	87215	8.999	3.029
2	92748	30994	95827	8.888	2.970
3	83257	27634	10536	8.772	2.912
4	74630	24610	11591	8.650	2.853
5	66794	21888	12762	8.524	2.793
6	59688	19439	14073	8.400	2.736
7	53249	17229	15532	8.271	2.676
8	47425	15250	17169	8.142	2.618
9	42160	13492	18992	8.007	2.562
50	37403	11943	21021	7.862	2.511
1	33106	10587	23276	7.706	2.464
2	29228	94094	25782	7.536	2.426
3	25728	83778	28778	7.404	2.411
4	22575	74662	31711	7.150	2.368
5	19737	66558	35237	6.955	2.345
6	17188	59303	39228	6.743	2.326
7	14903	52774	43766	6.522	2.310
8	12860	46857	48958	6.296	2.294
9	11040	41463	54940	6.065	2.278
60	94242	36527	61878	5.832	2.260
1	79954	31996	69990	5.596	2.239
2	67380	27835	79531	5.359	2.214
3	56373	24038	90849	5.121	2.184
4	46719	20593	10437	4.884	2.149
5	38502	17591	12064	4.645	2.122
6	31392	14826	14064	4.415	2.085
7	25339	12379	16522	4.187	2.045
8	20232	10233	19578	3.961	2.003
9	15963	83619	23429	3.740	1.959
70	12436	67525	28351	3.526	1.914
1	95510	53794	34558	3.310	1.864
2	72237	42246	42968	3.104	1.815
3	53716	32637	53993	2.900	1.762
4	39202	24770	68894	2.701	1.707
5	28026	18434	89483	2.508	1.650
6	19597	13413	11863	2.325	1.591
7	13360	95209	16033	2.142	1.526
8	88688	65709	22267	1.975	1.463
9	57191	44164	31749	1.816	1.402
80	35766	28707	46674	1.669	1.340
1	21715	18156	71168		
2	12790	11117	11205		
3	73089	65706	18243		
4	40485	37726	80670		
5	21563	21093	52849		
6	11037	11121	95003		
7	53886	57433	17705		
8	23920	26651	33371		
9	88248	10926	66247		
90	25711	35329	15991		
1	46334	98166	47443		
2	00000	13917	21583		

**DIFFERENCE OF AGE Three Years.**  
(Female the elder.)

$x$	$N_{x'y}$	$N_{x'y}^2$	$D_{x'y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
$a_{x'y}$	$a_{x'y}^2$			$a_{x'y}$	$a_{x'y}^2$
18	95269	27203	12315	11.732	3.412
9	87686	26477	13182	11.559	3.490
20	80620	25135	14152	11.409	3.557
1	74049	23704	15219	11.270	3.608
2	67949	22227	16394	11.140	3.644
3	62295	20735	17687	11.018	3.667
4	57061	19261	19105	10.902	3.680
5	52220	17831	20650	10.787	3.683
6	47747	16466	22359	10.676	3.682
7	43619	15178	24224	10.566	3.677
8	39812	13963	26269	10.458	3.668
9	36300	12820	28471	10.335	3.650
30	33073	11743	30989	10.249	3.639
1	30105	10727	33695	10.144	3.614
2	27379	97712	36680	10.043	3.584
3	24876	88755	39934	9.939	3.546
4	22581	80408	43567	9.838	3.503
5	20477	72671	47532	9.733	3.454
6	18551	65537	51913	9.630	3.402
7	16788	58990	56722	9.522	3.346
8	15176	53007	62042	9.415	3.289
9	13704	47560	67936	9.310	3.231
40	12360	42616	74427	9.199	3.172
1	11135	38141	81635	9.090	3.114
2	10019	84098	89587	8.976	3.055
3	90033	30453	98441	8.863	2.998
4	80794	27170	10824	8.745	2.941
5	72398	24213	11910	8.623	2.884
6	64773	21551	13115	8.495	2.826
7	57860	19153	14464	8.369	2.770
8	51596	17003	15964	8.237	2.714
9	45928	15090	17644	8.104	2.662
50	40803	13401	19511	7.961	2.615
1	36170	11921	21583	7.807	2.573
2	31983	10634	23883	7.638	2.540
3	28201	95034	26444	7.457	2.513
4	24789	85013	29309	7.265	2.492
5	21715	76067	32528	7.063	2.474
6	18950	68021	36162	6.853	2.460
7	16467	60751	40287	6.634	2.447
8	14245	54137	44996	6.410	2.436
9	12261	48084	50409	6.181	2.424
60	10497	42528	56669	5.949	2.410
1	89332	37411	63965	5.714	2.393
2	75545	32698	72530	5.479	2.372
3	63446	28381	82649	5.244	2.346
4	52885	24449	94692	5.008	2.315
5	43722	20895	10913	4.771	2.280
6	35822	17707	12658	4.534	2.241
7	29070	14877	14810	4.305	2.208
8	23346	12372	17470	4.079	2.161
9	18537	10183	20797	3.855	2.118
70	14539	82794	25012	3.638	2.071
1	11253	66496	30434	3.425	2.024
2	85816	52669	37427	3.212	1.971
3	64409	41081	46714	3.009	1.919
4	47499	31491	59136	2.809	1.862
5	34355	23689	76083	2.614	1.802
6	24326	17459	99710	2.426	1.741
7	16835	12566	13350	2.247	1.678
8	11351	88187	18234	2.070	1.608
9	74466	60113	25612	1.907	1.540
80	47412	39885	36963	1.752	1.474
1	29247	25565	55050		
2	17499	15928	85120		
3	10148	95999	13603		
4	57036	55788	22501		
5	31048	31464	38579		
6	16240	17259	67533		
7	81637	89066	12381		
8	39132	45171	23530		
9	17055	20561	45282		
90	61634	82916	91812		
1	17580	26297	22700		
2	30548	73937	68844		
3	00000	10309	32735		

**DIFFERENCE OF AGE TWO YEARS.**  
(Female the elder.)

$x$	$N_{x'y}$	$N_{x'y}^2$	$D_{x'y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
$a_{x'y}$	$a_{x'y}^2$				
18	10107	29217	11663	11.788	3.408
9	93066	27956	12488	11.622	3.491
20	85603	26572	13401	11.472	3.561
1	78663	25095	14409	11.335	3.616
2	72220	23558	15520	11.209	3.656
3	66247	22007	16741	11.090	3.684
4	60716	20470	18082	10.979	3.701
5	55600	18976	19547	10.868	3.709
6	50871	17547	21146	10.757	3.710
7	46503	16201	22894	10.646	3.709
8	42473	14928	24810	10.538	3.704
9	38757	13728	26914	10.431	3.695
30	85330	12598	29178	10.309	3.676
1	32182	11531	31770	10.224	3.663
2	29289	10525	34558	10.122	3.637
3	26631	95804	37632	10.022	3.605
4	24192	86981	41002	9.919	3.566
5	21956	78775	44721	9.819	3.523
6	19907	71193	48799	9.714	3.474
7	18031	64212	53303	9.611	3.423
8	16314	57814	58246	9.502	3.367
9	14745	51966	63715	9.395	3.311
40	13312	46645	69774	9.288	3.255
1	12004	41817	76447	9.177	3.197
2	10811	37451	83855	9.066	3.140
3	97244	33502	92032	8.950	3.083
4	87356	29941	10114	8.835	3.028
5	78365	26731	11121	8.715	2.973
6	70195	23839	12240	8.592	2.918
7	62777	21233	13480	8.462	2.862
8	56051	18900	14867	8.333	2.810
9	49955	16821	16406	8.196	2.760
50	44438	14983	18126	8.055	2.716
1	39447	13370	20033	7.902	2.678
2	34931	11964	22146	7.736	2.650
3	30849	10729	24497	7.557	2.628
4	27162	96310	27121	7.367	2.612
5	23835	86476	30064	7.166	2.600
6	20840	77593	33381	6.957	2.590
7	18147	69530	37139	6.740	2.582
8	15733	62166	41420	6.517	2.575
9	13575	55400	46330	6.289	2.567
60	11651	49165	51996	6.058	2.556
1	99443	43405	58581	5.825	2.543
2	84358	38083	66291	5.592	2.525
3	71090	33193	75873	5.358	2.502
4	59482	28793	86146	5.124	2.474
5	49383	24667	99015	4.890	2.442
6	40649	21014	11450	4.654	2.406
7	38147	17751	13330	4.418	2.366
8	26762	14854	15661	4.191	2.326
9	21373	12299	18557	3.966	2.282
70	16869	10072	22202	3.745	2.236
1	13144	81438	26850	3.529	2.187
2	10102	65026	32865	3.320	2.137
3	76441	51152	40688	3.110	2.081
4	56895	39588	51163	2.911	2.025
5	41583	30078	65305	2.716	1.965
6	29787	22407	84779	2.525	1.900
7	20875	16336	11221	2.342	1.833
8	14289	11625	15183	2.169	1.765
9	95209	80582	20973	1.997	1.690
80	61673	54224	29819	1.839	1.617
1	38736	35484	43597		
2	23548	22405	65842		
3	13871	13740	10333		
4	79110	81433	16779		
5	43687	46475	28230		
6	23350	25701	49171		
7	11988	13803	88016		
8	59109	69859	16455		
9	27789	34765	31928		
90	11855	15564	62756		
1	41821	61675	13033		
2	11462	19724	32940		
3	18955	54477	10442		
4	00000	73454	53036		

**DIFFERENCE OF AGE ONE YEAR.**  
(Female the elder.)

$x$	$N_{x'y}$	$N_{x'y}^2$	$D_{x'y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
$a_{x'y}$	$a_{x'y}^2$				
18	10719	30756	11049	11.843	3.398
19	98732	29459	11828	11.678	3.484
20	90852	28035	12690	11.529	3.558
1	83523	26512	13644	11.396	3.617
2	76717	24931	14694	11.273	3.663
3	70408	23323	15849	11.159	3.696
4	64565	21725	17115	11.050	3.718
5	59160	20166	18501	10.945	3.731
6	54162	18674	20011	10.838	3.737
7	49544	17265	21652	10.727	3.738
8	45279	15935	23448	10.617	3.736
9	41345	14677	25419	10.509	3.731
30	87719	13490	27582	10.404	3.721
1	34377	12371	29914	10.284	3.701
2	31308	11314	32584	10.201	3.687
3	28487	10321	35455	10.100	3.659
4	25898	93902	38620	10.002	3.626
5	23522	85228	42088	9.900	3.587
6	21344	77186	45913	9.800	3.544
7	19348	69767	50105	9.694	3.496
8	17521	62945	54735	9.590	3.445
9	15849	56691	59817	9.480	3.391
40	14321	50978	65439	9.372	3.336
1	12926	45783	71668	9.264	3.281
2	11652	41072	78527	9.150	3.225
3	10491	36808	86143	9.037	3.171
4	94339	32949	94554	8.920	3.115
5	84716	29468	10392	8.804	3.062
6	75957	26327	11430	8.683	3.009
7	68018	23496	12580	8.557	2.956
8	60801	20961	13855	8.424	2.904
9	54256	18706	15278	8.289	2.858
50	48322	16708	16854	8.144	2.816
1	42949	14953	18611	7.993	2.783
2	38085	13420	20556	7.829	2.759
3	33682	12072	22715	7.651	2.742
4	29702	10872	25123	7.462	2.731
5	26107	97941	27820	7.263	2.725
6	22866	88177	30853	7.055	2.721
7	19949	79276	34283	6.839	2.718
8	17330	71107	38184	6.617	2.715
9	14985	63574	42648	6.391	2.711
60	12893	56605	47788	6.161	2.705
1	11032	50141	53750	5.930	2.695
2	93852	44151	60711	5.698	2.680
3	79336	38628	68890	5.465	2.661
4	66608	33565	78562	5.233	2.637
5	55506	28954	90078	5.000	2.608
6	45880	24786	10389	4.766	2.575
7	37587	21046	12058	4.532	2.538
8	30492	17707	14095	4.298	2.496
9	24481	14751	16635	4.072	2.454
70	19433	12151	19811	3.850	2.407
1	15237	98959	23833	3.631	2.358
2	11789	79548	28995	3.418	2.306
3	89897	63079	35729	3.212	2.254
4	67457	49233	44565	3.006	2.194
5	49759	37765	56501	2.811	2.134
6	36017	28414	72770	2.621	2.068
7	25535	20939	95405	2.436	1.998
8	17699	15093	12761	2.259	1.926
9	11972	10609	17464	2.091	1.853
80	78771	72602	24418	1.923	1.773
1	50338	48182	35170		
2	31160	31066	52144		
3	18650	19307	79931		
4	10804	11644	12846		
5	60533	67780	21050		
6	32813	37925	36074		
7	17209	20526	64085		
8	86596	10816	11697		
9	41809	53656	22328		
90	19210	26276	44250		
1	79853	11571	89087		
2	26979	46093	18913		
3	69634	14410	49961		
4	10524	38350	16917		
5	00000	47680	95024		

## EQUAL AGES.

$x$	$N_{x,y}$	$N_{x,y}^{\frac{1}{2}}$	$D_{x,y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary. $a_{x,y}^{\frac{1}{2}}$
18	11363	32333	10465	11.891	3.384
9	10470	31001	11203	11.730	3.473
20	96381	29537	12019	11.584	3.550
1	86641	27970	12920	11.452	3.614
2	81454	26340	13913	11.333	3.665
3	74790	24679	15005	11.222	3.703
4	68618	23023	16203	11.118	3.730
5	62907	21402	17512	11.016	3.748
6	57627	19845	18939	10.914	3.758
7	52747	18373	20490	10.808	3.765
8	48237	16982	22175	10.696	3.766
9	44075	15668	24023	10.588	3.764
30	40236	14424	26050	10.481	3.757
1	36700	13248	28278	10.378	3.746
2	33440	12140	30680	10.259	3.725
3	30449	11096	33430	10.179	3.709
4	27700	10117	36486	10.107	3.691
5	25178	92022	39643	9.981	3.648
6	22864	83522	43210	9.880	3.609
7	20742	75654	47142	9.778	3.566
8	18799	68404	51452	9.672	3.520
9	17020	61735	56211	9.567	3.470
40	15392	55625	61436	9.456	3.417
1	13904	50048	67215	9.346	3.384
2	12546	44979	73617	9.236	3.311
3	11306	40378	80669	9.120	3.257
4	10177	36211	88503	9.007	3.205
5	91472	32439	97156	8.887	3.152
6	82109	29082	10680	8.769	3.101
7	73597	25958	11748	8.646	3.050
8	65863	23204	12931	8.517	3.001
9	58840	20753	14239 <sub>e</sub>	8.378	2.955
50	52469	18586	15696	8.236	2.917
1	46690	16678	17305	8.080	2.886
2	41454	15011	19097	7.916	2.867
3	36711	13541	21084	7.740	2.855
4	32418	12230	23296	7.552	2.849
5	28538	11053	25770	7.354	2.848
6	25035	99827	28549	7.147	2.850
7	21879	90043	31686	6.933	2.853
8	19042	81025	35247	6.712	2.856
9	16498	72671	39314	6.486	2.857
60	14925	64911	43990	6.258	2.855
1	12201	57686	49400	6.027	2.850
2	10406	50963	55704	5.797	2.839
3	88207	44747	63091	5.565	2.823
4	74280	39030	71805	5.334	2.803
5	62107	33806	82148	5.102	2.777
6	51525	29067	94511	4.870	2.747
7	42384	24800	10940	4.637	2.713
8	34541	20974	12750	4.404	2.674
9	27862	17566	14972	4.171	2.630
70	22231	14559	17759	3.948	2.586
1	17529	11926	21267	3.728	2.536
2	13644	96551	25737	3.512	2.485
3	10471	77072	31522	3.301	2.429
4	79157	60637	39133	3.098	2.373
5	58837	46906	49214	2.896	2.308
6	42954	35630	62958	2.704	2.243
7	30842	26517	82567	2.547	2.189
8	21626	19319	10850	2.346	2.096
9	14813	13756	14678	2.174	2.019
80	98948	95460	20332	2.012	1.941
1	64226	64437	28800		
2	40453	42134	42066		
3	24656	26745	63302		
4	14513	16344	98590		
5	82594	96826	15991		
6	45419	55270	26899		
7	24149	30264	47016		
8	12408	16063	85168		
9	61074	82988	15872		
90	28758	40468	30944		
1	12838	19499	62816		
2	51025	56034	12927		
3	16165	33454	28686		
4	88107	99851	80945		
5	51157	24505	30310		
6	00000	27062	19548		

DIFFERENCE OF AGE ONE YEAR.  
(Male the elder.)

$x$	$N_{x,y}$	$N_{x,y}^{\frac{1}{2}}$	$D_{x,y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary. $a_{x,y}^{\frac{1}{2}}$
18	12041	33958	99146	11.938	3.367
9	11093	32575	10613	11.779	3.457
20	10220	31071	11384	11.634	3.537
1	94033	29460	12237	11.507	3.605
2	86443	27782	13176	11.390	3.661
3	79405	26071	14208	11.282	3.704
4	72886	24360	15340	11.181	3.737
5	66854	22681	16578	11.080	3.759
6	61276	21061	17927	10.985	3.776
7	56119	19526	19392	10.883	3.786
8	51354	18072	20985	10.777	3.792
9	46952	16697	22719	10.667	3.793
80	42890	15397	24620	10.560	3.791
1	39146	14166	26707	10.455	3.783
2	35698	13001	29003	10.353	3.771
3	32521	11906	31477	10.237	3.748
4	29606	10878	34308	10.157	3.732
5	26929	99159	37350	10.058	3.703
6	24472	90195	40700	9.960	3.671
7	22218	81878	44367	9.857	3.633
8	20152	74188	48409	9.755	3.591
9	18260	67101	52839	9.648	3.546
40	16528	60587	57732	9.542	3.498
1	14948	54622	63103	9.429	3.447
2	13494	49179	69044	9.317	3.396
3	12172	44229	75626	9.205	3.345
4	10966	39733	82880	9.089	3.293
5	98659	35859	90939	8.972	3.243
6	88644	31968	99844	8.851	3.192
7	79534	28635	10977	8.730	3.143
8	71252	25644	12075	8.604	3.097
9	63727	22981	13288	8.468	3.054
60	56890	20626	14627	8.321	3.017
1	50685	18556	16116	8.168	2.990
2	45054	16744	17757	8.000	2.973
3	39948	15144	19587	7.825	2.966
4	35324	13716	21623	7.638	2.966
5	31189	12430	23896	7.441	2.970
6	27358	11261	26446	7.235	2.978
7	23947	10189	29320	7.021	2.987
8	20877	91975	32577	6.801	2.996
9	18122	82752	36291	6.577	3.003
60	15656	74145	40552	6.349	3.006
1	13457	66100	45474	6.119	3.006
2	11504	58586	51196	5.890	2.999
3	97762	51611	57888	5.659	2.988
4	82556	45175	56760	5.429	2.971
5	69237	39276	75082	5.198	2.949
6	60945	44199	54839	2.794	2.424
7	56831	33210	70850	2.609	2.353
8	26093	24435	93131	2.430	2.276
9	18081	17585	12480	2.257	2.195
80	12229	12362	17089	2.090	2.113
1	80590	84617	23981		
2	51560	56283	34446		
3	31978	36230	51067		
4	19170	22619	78078		
5	11085	13577	12369		
6	61913	78878	20434		
7	33389	44073	35058		
8	17385	23663	62484		
9	67318	12309	11557		
90	41858	62524	21997		
1	19093	29959	43927		
2	81221	14422	91153		
3	30220	61927	19607		
4	87037	22979	46475		
5	18084	62570	14503		
6	20463	13661	62485		
7	00000	12887	48869		

**DIFFERENCE OF AGE TWO YEARS.**  
(Male the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
18	12756	85661	93940	11.983	3.350
9	11761	84197	10054	11.825	3.438
20	10834	82636	10784	11.683	3.519
1	99710	80981	11591	11.557	3.592
2	91697	29256	12479	11.443	3.651
3	84265	27495	13455	11.338	3.699
4	77380	25732	14526	11.240	3.738
5	71009	23997	15696	11.146	3.767
6	65117	22319	16971	11.051	3.788
7	59669	20722	18356	10.953	3.804
8	54634	19206	19862	10.851	3.815
9	49983	17769	21400	10.696	3.803
30	45688	16409	23283	10.638	3.820
1	41726	15122	25240	10.532	3.817
2	38076	13902	27391	10.429	3.808
3	34715	12752	29755	10.329	3.794
4	31619	11673	32303	10.214	3.771
5	28780	10662	35216	10.135	3.755
6	26172	97195	38345	10.036	3.727
7	23779	88424	41789	9.937	3.695
8	21584	80296	45558	9.833	3.658
9	19572	72779	49714	9.730	3.618
40	17780	65856	54269	9.622	3.574
1	16043	59496	59299	9.513	3.528
2	14500	53675	64819	9.399	3.479
3	13091	48360	70928	9.285	3.430
4	11804	43522	77698	9.171	3.382
5	10629	89127	85161	9.052	3.332
6	95592	85141	93455	8.934	3.284
7	85848	81529	10262	8.810	3.236
8	76985	28285	11283	8.686	3.191
9	68926	25394	12409	8.553	3.151
50	61601	22835	13651	8.409	3.117
1	54942	20585	15019	8.252	3.092
2	48895	18620	16536	8.094	3.079
3	43404	16881	18213	7.905	3.075
4	38426	15327	20088	7.719	3.079
5	33918	13926	22180	7.523	3.089
6	29840	12649	24524	7.318	3.102
7	26158	11477	27161	7.105	3.117
8	22841	10391	30145	6.885	3.132
9	19860	93771	83542	6.661	3.145
60	17188	84270	87434	6.434	3.155
1	14803	75547	41920	6.205	3.159
2	12681	67080	47127	5.976	3.161
3	10801	59284	53203	5.746	3.154
4	91439	52062	60337	5.517	3.141
5	76896	45422	68762	5.288	3.123
6	64202	89360	78775	5.058	3.101
7	53184	33864	90764	4.827	3.074
8	43682	28900	10524	4.597	3.041
9	35544	24444	12288	4.368	3.004
70	28628	20472	14459	4.139	2.960
1	22800	16961	17158	3.912	2.910
2	17942	13895	20587	3.694	2.861
3	13937	11235	24967	3.480	2.805
4	10674	89604	30645	3.271	2.746
5	80510	70327	38136	3.070	2.681
6	59743	54302	48154	2.877	2.615
7	43539	41146	61712	2.687	2.539
8	31128	30565	80574	2.508	2.463
9	21793	23214	10712	2.384	2.380
80	14911	15783	14530	2.167	2.293
1	99492	10943	20156		
2	64627	73814	28682		
3	40714	48339	41817		
4	24837	30603	62987		
5	14629	18771	97957		
6	83021	11049	15806		
7	45471	62837	26631		
8	24008	34430	46592		
9	12214	18113	84785		
90	59699	92549	16016		
1	27675	46159	31227		
2	11987	22090	63743		
3	47540	10296	13826		
4	16061	42010	31767		
5	40519	14259	83269		
6	69997	34037	29834		
7	58665	62781	15588		
8	00000	03866	17104		

**DIFFERENCE OF AGE Three YEARS.**  
(Male the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
18	13508	37473	89015	12.024	3.336
9	12459	35905	95264	11.869	3.420
20	11480	34253	10217	11.729	3.499
1	10569	32535	10980	11.605	3.572
2	97231	30763	11820	11.493	3.636
3	89384	28953	12743	11.390	3.689
4	82114	27138	13756	11.296	3.733
5	75385	25350	14862	11.204	3.768
6	69162	23617	16068	11.113	3.795
7	63407	21962	17377	11.018	3.816
8	58088	20385	18800	10.921	3.832
9	53174	18886	20348	10.820	3.843
20	48635	17465	22034	10.716	3.848
1	44446	16118	23871	10.610	3.848
2	40583	14844	25887	10.506	3.843
3	37025	13639	28103	10.405	3.833
4	33750	12506	30536	10.306	3.819
5	30734	11445	33159	10.191	3.795
6	27968	10455	36155	10.112	3.780
7	25428	95321	39372	10.012	3.753
8	23098	86749	42912	9.912	3.723
9	20961	78804	46788	9.807	3.687
40	19002	71461	51060	9.702	3.649
1	17208	64702	55742	9.592	3.607
2	15566	58496	60912	9.482	3.563
3	14065	52811	66588	9.366	3.517
4	12692	47617	72871	9.249	3.470
5	11440	42888	79836	9.133	3.424
6	10297	38588	87517	9.012	3.377
7	92561	34687	96057	8.891	3.332
8	83081	31172	10548	8.763	3.288
9	74456	28036	11595	8.633	3.251
60	66611	25258	12748	8.492	3.220
1	59477	22814	14017	8.337	3.198
2	52988	20678	15411	8.166	3.187
3	47092	18791	16961	7.987	3.187
4	41738	17102	18678	7.796	3.194
5	36885	15577	20606	7.601	3.210
6	32492	14185	22762	7.396	3.229
7	28522	12906	25186	7.184	3.251
8	24941	11719	27924	6.965	3.272
9	21719	10608	31038	6.741	3.293
70	32290	24051	13118	4.227	3.155
1	25777	20028	15521	4.001	3.109
2	20380	16493	18529	3.776	3.056
3	15912	13416	22381	3.561	3.003
4	12255	10762	27346	3.351	2.943
5	92998	85064	33842	3.147	2.879
6	69459	66109	42483	2.951	2.809
7	51006	50492	54190	2.764	2.736
8	36757	37823	70183	2.580	2.655
9	25567	27753	92681	2.407	2.572
80	17949	19913	12472	2.239	2.484
1	12114	13954	17436		
2	79661	95343	24107		
3	50941	63316	34819		
4	31553	40785	51578		
5	18899	25367	79023		
6	10910	15262	12517		
7	60558	87939	20600		
8	32303	49046	35393		
9	16486	26334	63221		
90	83354	13604	11750		
1	39371	68199	22736		
2	17302	33827	45313		
3	69590	15604	96682		
4	24946	69115	22399		
5	73765	25685	56917		
6	15387	76722	17129		
7	19790	15115	74585		
8	14616	18964	54559		
9	00000	01289	68417		

**DIFFERENCE OF AGE FOUR YEARS.**  
(Male the elder.)

<i>x</i>	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
<i>a</i> <sub>x,y</sub>	<i>a</i> <sub>x,y</sub> <sup>2</sup>				
19	13183	37732	90270	11.900	3.406
20	12150	35957	96805	11.763	3.481
1	11189	34139	10402	11.639	3.551
2	10296	32299	11197	11.528	3.617
3	94675	30439	12070	11.427	3.674
4	86999	28574	13028	11.334	3.723
5	79894	26734	14075	11.245	3.763
6	73321	24948	15214	11.155	3.796
7	67243	23238	16452	11.063	3.823
8	61624	23604	17898	11.029	3.867
9	56533	20045	19261	10.889	3.861
30	51787	18563	20854	10.789	3.871
1	47310	17156	22590	10.687	3.875
2	43226	15822	24482	10.583	3.874
3	39461	14563	26559	10.480	3.868
4	35993	13376	28840	10.380	3.858
5	32803	12262	31845	10.282	3.844
6	29865	11223	34042	10.167	3.821
7	27172	10254	37122	10.086	3.806
8	24698	93519	40430	9.985	3.781
9	22429	85141	44070	9.884	3.752
40	20348	77379	48053	9.778	3.718
1	18441	70210	52444	9.671	3.682
2	16695	63614	57258	9.559	3.642
3	15097	57554	62574	9.447	3.601
4	13635	51998	68413	9.328	3.557
5	12300	46921	74876	9.210	3.513
6	11081	42294	82046	9.092	3.470
7	99690	38085	89953	9.967	3.426
8	89561	34289	98730	8.842	3.385
9	80336	30891	10840	8.708	3.349
50	71941	27878	11911	8.569	3.321
1	64801	25224	13089	8.416	3.302
2	57348	22908	14382	8.248	3.294
3	51021	20853	15807	8.065	3.296
4	45272	19021	17395	7.875	3.809
5	40053	17363	19160	7.674	3.827
6	35324	15849	21147	7.470	3.852
7	31046	14455	23377	7.258	3.879
8	27185	13158	25894	7.039	3.407
9	23707	11944	28752	6.816	3.434
60	20583	10800	32015	6.590	3.458
1	17787	97170	35765	6.362	3.475
2	15293	86926	40105	6.133	3.486
3	13078	77298	45148	5.904	3.490
4	11120	68309	51047	5.676	3.487
5	93949	59981	57985	5.448	3.478
6	78843	52324	66196	5.219	3.464
7	65680	45338	75974	4.990	3.445
8	54280	38988	87719	4.761	3.420
9	44471	33249	10195	4.534	3.390
70	36092	28096	11934	4.307	3.353
1	28991	25306	14082	4.083	3.310
2	23024	19455	16761	3.859	3.261
3	18060	15908	20143	3.638	3.204
4	13980	12837	24513	3.427	3.147
5	10669	10204	30198	3.222	3.081
6	80171	79867	37710	3.023	3.012
7	59255	61396	47808	2.833	2.935
8	43028	46358	61628	2.652	2.857
9	30641	34302	80728	2.474	2.769
80	21373	24847	10790	2.306	2.681
1	14575	17584	14710		
2	96964	12142	20497		
3	62795	81681	29265		
4	39510	53355	42947		
5	24057	33768	64710		
6	14154	20600	10098		
7	80244	12136	16314		
8	43718	68573	27377		
9	22895	87478	48025		
90	11482	19759	87619		
1	54868	10010	16680		
2	24558	49832	32992		
3	10008	23873	68729		
4	36242	10374	15664		
5	11325	41804	40132		
6	27840	13613	11709		
7	42889	83891	42824		
8	45822	45548	26105		
9	00000	05892	21824		

**DIFFERENCE OF AGE FIVE YEARS.**  
(Male the elder.)

<i>x</i>	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
<i>a</i> <sub>x,y</sub>	<i>a</i> <sub>x,y</sub> <sup>2</sup>				
20	12876	37786	91730	11.811	3.466
1	11862	35833	98558	11.691	3.532
2	10919	33887	10608	11.583	3.595
3	10044	31956	11434	11.484	3.654
4	92339	30039	12340	11.393	3.707
5	84837	28148	13330	11.309	3.752
6	77897	26310	14408	11.223	3.791
7	71477	24548	15579	11.135	3.824
8	65543	22860	16851	11.045	3.853
9	60059	21245	18234	10.951	3.874
30	54993	19703	19739	10.855	3.889
1	50315	18236	21380	10.758	3.899
2	45999	16842	23168	10.657	3.902
3	42018	15524	25118	10.554	3.899
4	38349	14284	27256	10.452	3.893
5	34971	13117	29603	10.352	3.883
6	31864	12023	32180	10.254	3.870
7	29003	11009	34954	10.138	3.848
8	26379	10061	38121	10.056	3.835
9	23971	91798	41520	9.953	3.811
40	21761	83612	45261	9.849	3.784
1	19735	76039	49358	9.741	3.753
2	17879	69039	53872	9.632	3.719
3	16179	62598	58821	9.517	3.682
4	14624	56675	64288	9.401	3.644
5	13201	51244	70295	9.280	3.602
6	11901	46276	76948	9.158	3.561
7	10716	41748	84329	9.037	3.521
8	96341	37653	92457	8.907	3.481
9	86485	33983	10146	8.775	3.448
50	77505	30718	11136	8.631	3.421
1	69328	27840	12230	8.479	3.405
2	61882	25320	13431	8.311	3.401
3	55103	23093	14752	8.199	3.407
4	48935	21102	16211	7.933	3.421
5	43330	19303	17843	7.731	3.444
6	38244	17658	19662	7.520	3.472
7	33640	16140	21718	7.306	3.505
8	29579	14727	24040	7.111	3.540
9	25828	13402	26661	6.886	3.573
60	22456	12151	29657	6.660	3.604
1	19435	10965	33095	6.432	3.629
2	16737	98385	37066	6.204	3.647
3	14337	87756	41675	5.975	3.657
4	12212	77787	47058	5.747	3.660
5	10339	68514	53377	5.519	3.657
6	86952	59955	60839	5.290	3.648
7	72607	52116	69708	5.061	3.633
8	60159	44968	60335	4.833	3.613
9	49427	38488	93178	4.606	3.586
70	40239	32650	10884	4.380	3.554
1	32433	27431	12811	4.155	3.514
2	25857	22809	15207	3.932	3.469
3	20388	18744	18285	3.728	3.427
4	15855	15204	22062	3.493	3.354
5	12161	12159	27070	3.292	3.291
6	91959	95704	33650	3.092	3.220
7	68331	74092	42437	2.900	3.144
8	49939	56306	54371	2.715	3.061
9	35932	41995	70887	2.540	2.977
80	25192	20675	93986	2.368	2.883
1	17334	21916	12727		
2	11651	15282	17594		
3	76319	10389	24894		
4	48616	68747	36097		
5	30057	44122	53882		
6	17964	27393	82690		
7	10365	16364	13161		
8	57531	94560	21681		
9	30611	52357	37148		
90	15587	28097	66558		
1	75470	14526	12438		
2	34157	73017	24205		
3	14173	35055	50041		
4	51924	15826	11135		
5	16292	62082	28065		
6	41793	21881	82558		
7	76295	58808	29271		
8	95768	10123	14988		
9	00000	18219	10443		

**DIFFERENCE OF AGE Six YEARS.**  
(Male the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
x	N <sub>x,y</sub>	N <sub>x,y</sub>	D <sub>x,y</sub> <sup>-1</sup>	a <sub>x,y</sub>	a <sub>x,y</sub>
21	12561	37658	93391	11·731	3·517
2	11566	85567	10051	11·625	3·575
3	10643	83524	10833	11·529	3·632
4	97879	81534	11690	11·442	3·686
5	89958	29591	12626	11·358	3·736
6	82630	27701	13646	11·276	3·780
7	75852	25888	14753	11·190	3·819
8	69584	24149	15956	11·103	3·853
9	63792	22480	17264	11·013	3·881
30	58441	20883	18687	10·921	3·902
1	53499	19356	20238	10·827	3·917
2	48939	17903	21927	10·731	3·926
3	44732	16526	23770	10·633	3·928
4	40852	15228	25777	10·530	3·925
5	37278	14009	27978	10·430	3·919
6	33988	12865	30392	10·330	3·910
7	30961	11797	33041	10·230	3·898
8	28175	10803	35892	10·113	3·877
9	25621	98773	39148	10·030	3·867
40	23276	90163	42643	9·926	3·845
1	21125	8172	46491	9·821	3·820
2	19153	74777	50700	9·711	3·791
3	17346	67946	55342	9·600	3·760
4	15691	61651	60432	9·482	3·726
5	14177	55861	66058	9·365	3·690
6	12793	50548	72239	9·242	3·652
7	11528	45685	79090	9·117	3·613
8	10375	41279	86677	8·903	3·578
9	93222	37320	95015	8·857	3·546
50	83628	33794	10423	8·717	3·522
1	74882	30676	11434	8·562	3·507
2	66914	27942	12549	8·397	3·506
3	59654	25524	13775	8·217	3·516
4	53045	23361	15129	8·025	3·534
5	47081	21406	16628	7·820	3·559
6	41570	19621	18311	7·612	3·593
7	36617	17972	20193	7·394	3·629
8	32139	16434	22328	7·176	3·669
9	28098	14989	24746	6·953	3·709
60	94462	13624	27500	6·727	3·747
1	21200	12327	30657	6·499	3·779
2	18284	11093	34298	6·271	3·805
3	15688	99247	38519	6·043	3·823
4	13386	88242	43474	5·819	3·836
5	11334	77957	49205	5·587	3·836
6	95680	68427	56004	5·358	3·832
7	80072	59665	64067	5·130	3·823
8	66505	51644	73709	4·902	3·807
9	54786	44349	85334	4·675	3·784
70	44734	37757	99475	4·450	3·756
1	36174	31845	11683	4·226	3·720
2	28946	26591	13834	4·004	3·679
3	22897	21952	16532	3·785	3·629
4	17886	17896	19957	3·570	3·572
5	13782	14385	24364	3·358	3·505
6	10467	11391	30164	3·157	3·436
7	78260	88684	37867	2·968	3·358
8	57540	67874	48262	2·777	3·276
9	41550	50948	62540	2·599	3·186
80	29433	37512	82500	2·429	3·096
1	20412	27025	11085		
2	18843	19026	15222		
3	91606	13061	21358		
4	59024	87335	30693		
5	36943	56781	45288		
6	22419	35750	68853		
7	18140	21739	10777		
8	74230	19738	17491		
9	40239	72145	29420		
90	20816	39219	51484		
1	10232	20639	94483		
2	46916	10584	18049		
3	19678	51283	36713		
4	73434	23163	81075		
5	23309	94621	19950		
6	59879	32190	57733		
7	11429	93733	20639		
8	16680	17540	10245		
9	00000	29336	59953		

**DIFFERENCE OF AGE Seven Years.**  
(Male the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
x	N <sub>x,y</sub>	N <sub>x,y</sub>	D <sub>x,y</sub> <sup>-1</sup>	a <sub>x,y</sub>	a <sub>x,y</sub>
22	12247	37382	95238	11·684	3·560
3	11273	35187	10264	11·571	3·612
4	10370	33081	11075	11·485	3·664
5	95342	31064	11960	11·403	3·715
6	87605	29123	12925	11·323	3·764
7	80448	27259	13972	11·240	3·807
8	73830	25469	15110	11·156	3·848
9	67712	23749	16347	11·069	3·882
30	62060	22099	17692	10·980	3·910
1	56840	20517	19158	10·889	3·931
2	52022	19006	20756	10·798	3·945
3	47577	17570	22497	10·703	3·953
4	43478	16213	24394	10·606	3·955
5	39699	14937	26460	10·504	3·952
6	36217	13742	28724	10·403	3·947
7	33013	12623	31206	10·302	3·939
8	30065	11578	33929	10·201	3·928
9	27353	10607	36861	10·083	3·910
40	24865	97028	40207	9·997	3·901
1	22582	88622	43800	9·891	3·882
2	20488	80823	47755	9·784	3·860
3	18153	72153	30783	11·732	3·845
4	16810	67363	52083	9·671	3·833
5	15199	60773	62095	9·558	3·805
6	13726	55107	67885	9·318	3·774
7	12379	49907	74251	9·192	3·706
8	11149	45177	81292	9·063	3·673
9	10027	40917	89074	8·931	3·645
50	90020	37112	97609	8·787	3·622
1	80677	33744	10702	8·634	3·611
2	72153	30783	11732	8·465	3·611
3	64384	28160	12871	8·287	3·624
4	57306	25811	14128	8·096	3·647
5	50863	23688	15519	7·893	3·676
6	45002	21747	17065	7·680	3·711
7	39684	19958	18805	7·463	3·753
8	34868	18288	20761	7·239	3·797
9	30518	16715	22990	7·016	3·843
60	26600	15227	25525	6·790	3·887
1	23083	13811	28428	6·562	3·926
2	19935	12462	31772	6·336	3·959
3	17130	11182	35643	6·106	3·986
4	14639	99720	40149	5·877	4·004
5	12437	88365	45422	5·649	4·014
6	10500	77796	51628	5·421	4·016
7	88046	68040	58975	5·193	4·013
8	73285	59074	67745	4·965	4·002
9	60513	50888	78296	4·738	3·984
70	49536	43468	91101	4·513	3·960
1	40171	36792	10678	4·289	3·929
2	32245	30839	12617	4·068	3·891
3	25596	25566	15040	3·850	3·845
4	20074	20937	18107	3·635	3·791
5	15536	16914	22039	3·424	3·728
6	11853	13463	27148	3·218	3·655
7	89069	10545	33945	3·023	3·580
8	65848	81157	43064	2·836	3·495
9	47835	61353	55513	2·655	3·406
80	34100	45461	72811	2·483	3·310
1	23827	33013	97341		
2	16285	23435	13259		
3	10873	16242	18479		
4	70774	10967	26344		
5	44804	72050	38506		
6	27525	45955	57871		
7	16381	28341	89737		
8	93989	16906	14323		
9	51854	97091	23733		
90	27328	54002	40773		
1	13645	28785	73085		
2	63518	15019	13710		
3	26989	74250	27376		
4	10177	33837	59481		
5	32923	13801	14526		
6	85568	49072	41041		
7	16283	13638	14433		
8	24402	27727	72239		
9	00000	48685	40980		

DIFFERENCE OF AGE Eight YEARS.  
(Male the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub> <sup>2</sup>	D <sub>x'y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary. a <sub>x'y</sub> <sup>3</sup>
23	11937	36883	97258	11·610	3·587
4	10984	34621	10493	11·526	3·633
5	10101	32486	11331	11·445	3·681
6	92844	30471	12244	11·368	3·731
7	85288	28556	13235	11·288	3·779
8	78300	26616	14310	11·205	3·837
9	71840	25046	15480	11·121	3·877
30	65871	23346	16753	11·035	3·911
1	60358	21712	18139	10·948	3·938
2	55268	20145	19649	10·860	3·958
3	50572	18652	21295	10·769	3·972
4	46241	17237	23087	10·676	3·980
5	42247	15904	25040	10·579	3·982
6	38566	14653	27165	10·476	3·980
7	35176	13848	29493	10·374	3·977
8	32055	12391	32045	10·272	3·971
9	29185	11370	34844	10·169	3·962
40	26544	10422	37858	10·049	3·946
1	24122	95382	41298	9·962	3·939
2	21900	87180	44992	9·853	3·922
3	19861	79565	49058	9·743	3·903
4	17992	72508	53511	9·628	3·880
5	16281	65981	58423	9·512	3·855
6	14714	59961	63814	9·390	3·826
7	13281	54416	69775	9·267	3·797
8	11970	49357	76318	9·135	3·767
9	10773	44783	83540	9·000	3·741
50	96804	40689	91506	8·858	3·723
1	86826	37056	10022	8·702	3·714
2	77720	33858	10981	8·534	3·718
3	69410	31016	12033	8·352	3·732
4	61835	28468	13201	8·163	3·758
5	54934	26163	14492	7·961	3·792
6	48655	24054	15926	7·749	3·831
7	42949	22110	17526	7·527	3·875
8	37777	20297	19335	7·304	3·924
9	33099	18588	21476	7·108	3·992
60	28882	16969	23714	6·849	4·024
1	25092	15425	26387	6·621	4·070
2	21698	13953	29462	6·393	4·111
3	18669	12554	33017	6·164	4·145
4	15978	11228	37151	5·936	4·171
5	13596	99800	41982	5·708	4·190
6	11497	88132	47657	5·474	4·200
7	96580	77311	54367	5·251	4·203
8	80544	67328	62361	5·023	4·199
9	66648	58179	71961	4·796	4·187
70	54684	49852	83588	4·571	4·167
1	44459	42337	97794	4·348	4·140
2	35787	35615	11531	4·127	4·107
3	28496	29641	13716	3·909	4·066
4	22425	24379	16473	3·694	4·016
5	17424	19789	19996	3·484	3·957
6	13552	15833	24558	3·279	3·888
7	10079	12469	30551	3·079	3·809
8	74886	96598	38604	2·891	3·729
9	54699	73483	49536	2·710	3·640
80	39226	54889	64631	2·535	3·548
1	27582	40166	85878		
2	18993	28797	11642		
3	12780	20185	16096		
4	83924	13824	22892		
5	53668	92380	33051		
6	33345	60250	49205		
7	20087	38394	75424		
8	11702	24017	11926		
9	65566	14874	19435		
90	35163	92591	32892		
1	17886	39590	57880		
2	84571	20916	10605		
3	36484	10519	20895		
4	13937	48938	44352		
5	45537	20143	10657		
6	12072	71370	29882		
7	23256	20894	11433		
8	84608	40214	50517		
9	00000	76193	28895		

DIFFERENCE OF AGE Nine YEARS.  
(Male the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub> <sup>2</sup>	D <sub>x'y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary. a <sub>x'y</sub> <sup>3</sup>
24	11630	36496	99430	11·564	3·629
5	10698	34203	10736	11·485	3·672
6	96361	32070	11600	11·410	3·720
7	90385	30082	12537	11·332	3·771
8	83007	28191	13555	11·253	3·821
9	76187	26372	14661	11·170	3·866
80	69883	24622	15865	11·088	3·907
1	64061	22938	17175	11·002	3·940
2	58686	21320	18603	10·917	3·966
3	53725	19773	20159	10·830	3·986
4	49149	18301	21854	10·741	4·000
5	44930	16911	23699	10·648	4·008
6	41040	15604	25707	10·550	4·011
7	37454	14381	27892	10·447	4·011
8	34153	13238	30285	10·343	4·009
9	31114	12169	32909	10·239	4·005
40	28320	11172	35787	10·135	6·998
1	25748	10246	38886	10·012	3·984
2	23391	93839	42421	9·923	3·981
3	21227	85829	46219	9·811	3·967
4	19243	78386	50402	9·699	3·951
5	17424	71488	54983	9·580	3·931
6	15759	65102	60040	9·462	3·909
7	14234	59210	65590	9·336	3·884
8	12840	53815	71718	9·209	3·860
9	11565	48924	78429	9·070	3·837
50	10400	44529	85821	8·925	3·822
1	93353	40619	93957	8·771	3·816
2	83628	37169	10284	8·600	3·822
3	74750	34099	11263	8·419	3·841
4	66647	31839	12341	8·225	3·868
5	59262	28838	13541	8·025	3·905
6	52538	26549	14872	7·818	3·948
7	46424	24437	16356	7·593	3·997
8	40874	22467	18019	7·365	4·048
9	35851	20613	19907	7·137	4·103
60	31316	18853	22049	6·905	4·157
1	27236	17173	24513	6·676	4·210
2	23580	15568	27346	6·448	4·257
3	20313	14041	30617	6·219	4·299
4	17408	12592	34414	5·991	4·333
5	14833	11224	38847	5·762	4·360
6	12563	99415	44047	5·534	4·379
7	10571	87469	50186	5·305	4·390
8	88310	76397	57488	5·077	4·392
9	73214	66209	66243	4·850	4·386
70	60197	56902	76824	4·625	4·371
1	49053	48470	89696	4·410	4·348
2	39583	40903	10561	4·180	4·320
3	31607	34157	12536	3·962	4·282
4	24950	28196	15022	3·748	4·236
5	19453	22977	18191	3·539	4·180
6	14965	18463	22281	3·334	4·114
7	11346	14609	27636	3·136	4·037
8	84681	11370	34744	2·942	3·950
9	62161	68693	44405	2·760	3·862
80	44821	65259	57672	2·585	3·764
1	31703	48032	76229		
2	21967	34585	10271		
3	14892	24363	14134		
4	98548	16746	19853		
5	63578	11216	28595		
6	39901	72994	42235		
7	24307	46083	64130		
8	14331	28245	10024		
9	81516	16751	16182		
90	44389	96183	26935		
1	22972	53181	46693		
2	11066	28730	83989		
3	48493	14619	16086		
4	18812	69171	33692		
5	62289	29091	79465		
6	16666	10400	21923		
7	32796	30184	74705		
8	49489	61484	85911		
9	00000	10865	20207		

**DIFFERENCE OF AGE Ten Years.**  
(Male the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub>	D <sub>x'y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
25	11327	35952	10173	11·523	3·657
6	10417	83661	10991	11·449	3·700
7	95753	81558	11877	11·373	3·748
8	87965	29595	12840	11·295	3·800
9	80764	27726	13887	11·216	3·850
80	74109	25927	15028	11·137	3·896
1	67960	24194	16265	11·054	3·935
2	62283	22526	17615	10·971	3·968
3	57044	20928	19086	10·887	3·994
4	52210	19403	20688	10·801	4·014
5	47753	17957	22432	10·712	4·028
6	43643	16594	24390	10·645	4·047
7	39854	15316	26395	10·519	4·043
8	36863	14120	28642	10·415	4·044
9	33147	13003	31102	10·309	4·044
40	30189	11959	33799	10·204	4·042
1	27468	10985	36758	10·097	4·038
2	24965	10081	39943	9·972	4·027
3	22670	92398	43580	9·880	4·027
4	20564	84570	47486	9·765	4·016
5	18633	77295	51789	9·650	4·003
6	16864	70545	56505	9·529	3·986
7	15243	64295	61711	9·407	3·968
8	13760	58562	67416	9·276	3·948
9	12403	53347	73701	9·141	3·932
50	11162	48446	80570	8·993	3·919
1	10027	44449	88119	8·836	3·917
2	89897	40736	96408	8·667	3·927
3	80417	37425	10548	8·482	3·947
4	71760	34443	11552	8·290	3·979
5	63860	31784	12659	8·084	4·017
6	56664	29251	13896	7·874	4·065
7	50117	26958	15274	7·655	4·118
8	44170	24818	16816	7·428	4·173
9	38780	22803	18552	7·194	4·230
60	33910	20893	20534	6·963	4·290
1	29523	19068	22793	6·729	4·346
2	25587	17321	25405	6·500	4·400
3	22068	15656	28418	6·271	4·449
4	18934	14074	31912	6·042	4·491
5	16155	12579	35985	5·813	4·527
6	13702	11174	40758	5·585	4·554
7	11546	98609	46384	5·355	4·574
8	96614	86386	53067	5·127	4·584
9	80238	75087	61065	4·900	4·585
70	66097	64724	70718	4·674	4·577
1	53971	55299	82467	4·451	4·560
2	43651	46807	96896	4·230	4·535
3	34941	39214	11481	4·012	4·502
4	27657	32483	13730	3·797	4·460
5	21630	26571	16590	3·588	4·408
6	16696	21439	20270	3·384	4·345
7	12708	17041	25074	3·186	4·273
8	95264	13329	31439	2·995	4·191
9	70242	10247	39965	2·807	4·095
80	50899	77365	51698	2·631	4·000
1	36198	67258	68023		
2	25230	41525	91174		
3	17210	29435	12469		
4	11474	20394	17433		
5	74587	13773	24907		
6	47321	90499	36540		
7	29054	57694	55045		
8	17321	35730	85228		
9	99684	21468	12735		
90	55096	12500	22427		
1	28942	70373	38935		
2	14163	38510	67756		
3	63331	20043	12739		
4	24960	95904	26061		
5	83939	41031	60364		
6	22767	15014	16347		
7	45208	44048	54807		
8	69617	88982	26147		
9	00000	16873	14364		

**DIFFERENCE OF AGE Eleven Years.**  
(Male the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub>	D <sub>x'y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
26	11029	35384	10415	11·487	3·685
7	10141	33124	11254	11·413	3·728
8	93186	31047	12165	11·336	3·777
9	85584	29107	13155	11·259	3·829
30	78558	27259	14232	11·180	3·880
1	72066	25477	15404	11·101	3·924
2	66601	23761	16682	11·022	3·964
3	60538	22114	18073	10·941	3·997
4	55433	20539	19587	10·858	4·023
5	50724	19040	21236	10·772	4·043
6	46382	17623	23030	10·682	4·059
7	42379	16289	24982	10·587	4·069
8	38689	15040	27105	10·487	4·076
9	35290	13871	29414	10·380	4·080
40	32159	12780	31944	10·273	4·082
1	29279	11760	34716	10·164	4·082
2	26630	10811	37759	10·055	4·082
3	24193	99280	41034	9·927	4·074
4	21960	91055	44774	9·832	4·077
5	19910	83402	48793	9·715	4·069
6	18031	76284	53222	9·596	4·060
7	16310	69673	58078	9·473	4·047
8	14733	63597	63429	9·345	4·034
9	13290	58054	69280	9·207	4·022
50	11969	53043	75713	9·062	4·016
1	10760	48553	82727	8·901	4·017
2	96541	44567	90418	8·729	4·030
3	86428	41004	98884	8·546	4·055
4	77184	37788	10818	8·350	4·088
5	68745	34862	11849	8·146	4·131
6	61047	32173	12991	7·931	4·179
7	54040	29684	14271	7·712	4·236
8	47672	27360	15703	7·486	4·296
9	41896	25171	17314	7·254	4·358
60	36671	23096	19136	7·017	4·420
1	31960	21116	21226	6·784	4·482
2	27726	19218	23622	6·549	4·540
3	23939	17406	26401	6·320	4·595
4	20563	15681	29620	6·091	4·645
5	17566	14049	33369	5·862	4·688
6	14917	12513	37756	5·632	4·724
7	12587	11075	42921	5·402	4·754
8	10548	97311	49037	5·172	4·772
9	87744	84837	56369	4·946	4·782
70	72405	73343	65192	4·720	4·781
1	59232	62848	75913	4·496	4·771
2	48004	53357	89056	4·275	4·752
3	38511	44836	10534	4·057	4·723
4	30558	37258	12575	3·843	4·685
5	23963	30583	15163	3·635	4·637
6	18554	24770	18486	3·430	4·579
7	14170	19769	22811	3·232	4·510
8	10663	15534	26516	3·041	4·430
9	78969	12002	36152	2·855	4·339
80	57477	91077	46529	2·674	4·238
1	41077	67820	60976		
2	28785	49456	81357		
3	19751	35310	11068		
4	13249	24617	15380		
5	86765	16757	21871		
6	55346	11102	31828		
7	30348	71463	47624		
8	20678	44689	73155		
9	12031	27129	11565		
90	67262	16002	18850		
1	58552	91840	31837		
2	17829	50863	55483		
3	80984	26800	10277		
4	32553	13121	20639		
5	11117	56732	46693		
6	30638	21113	12418		
7	61692	63466	40868		
8	95615	12949	19182		
9	00000	24036	10459		

## DIFFERENCE OF AGE TWELVE YEARS.

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sup>-1</sup> <sub>x,y</sub>	Annuities.	
				Joint Lives.	Rever-sionary.
x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sup>-1</sup> <sub>x,y</sub>	a <sub>x,y</sub>	a <sub>x,y</sub> <sup>2</sup>
27	10736	34821	10664	11.449	3.713
8	98684	32590	11526	11.374	3.756
9	90660	30537	12463	11.299	3.806
30	83243	28618	13482	11.223	3.858
1	76389	26788	14591	11.146	3.909
2	70060	25024	15799	11.069	3.954
3	64217	23328	17115	10.991	3.993
4	58825	21703	18547	10.910	4.026
5	53851	20157	20106	10.827	4.053
6	49265	18688	21802	10.741	4.074
7	45036	17302	23647	10.650	4.091
8	41138	15998	25653	10.553	4.104
9	37545	14777	27836	10.451	4.113
40	34235	13635	30210	10.342	4.119
1	31187	12570	32811	10.233	4.124
2	28383	11575	35661	10.122	4.128
3	25805	10648	38788	10.009	4.130
4	23433	97850	42158	9.879	4.125
5	21259	89810	46006	9.780	4.132
6	19265	82322	50143	9.660	4.128
7	17487	75355	54704	9.539	4.122
8	15762	68928	59694	9.409	4.115
9	14228	63049	65183	9.274	4.110
50	12823	57723	71172	9.126	4.108
1	11536	52936	77741	8.968	4.115
2	10358	48673	84886	8.792	4.132
3	92799	44848	92739	8.606	4.159
4	82938	41387	10141	8.410	4.197
5	73926	38230	11096	8.203	4.242
6	65703	35325	12160	7.989	4.296
7	58208	32629	13842	7.766	4.353
8	51392	30109	14673	7.541	4.418
9	45207	27732	16169	7.310	4.484
60	39608	25477	17859	7.074	4.550
1	34553	23326	19782	6.835	4.614
2	30007	21266	21998	6.601	4.678
3	25933	19297	24548	6.366	4.737
4	22299	17421	27518	6.136	4.794
5	19071	15642	30973	5.907	4.845
6	16214	13965	35011	5.677	4.889
7	13699	12392	39760	5.447	4.927
8	11496	10920	45385	5.217	4.956
9	95766	95487	52099	4.989	4.975
70	79148	82798	60178	4.763	4.983
1	64859	71158	69981	4.539	4.980
2	52660	60590	81978	4.317	4.967
3	42831	51066	96817	4.098	4.944
4	33664	42563	11538	3.884	4.911
5	26463	35049	13886	3.675	4.867
6	20544	28485	16896	3.471	4.813
7	15737	22820	20803	3.274	4.747
8	11882	18005	25942	3.083	4.671
9	88336	13974	32800	2.897	4.583
80	64577	10658	42089	2.718	4.486
1	46355	79767	54879		
2	32643	58526	72929		
3	22518	42015	98765		
4	15193	29504	13652		
5	10011	20208	19296		
6	64326	13496	27948		
7	40219	87592	41482		
8	24419	55305	63292		
9	14345	33899	99264		
90	81055	20199	16027		
1	43685	11677	26759		
2	22039	65887	46199		
3	10156	35317	84155		
4	41504	17492	16650		
5	14461	77459	36979		
6	40506	29115	96055		
7	82944	88985	31045		
8	13033	18670	14304		
9	00000	35150	76730		

## DIFFERENCE OF AGE THIRTEEN YEARS.

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sup>-1</sup> <sub>x,y</sub>	Annuities.	
				Joint Lives.	Rever-sionary.
x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sup>-1</sup> <sub>x,y</sub>	a <sub>x,y</sub>	a <sub>x,y</sub> <sup>2</sup>
28	10447	34261	10923	11.411	3.742
9	96006	32056	11809	11.337	3.785
30	88176	30026	12773	11.263	3.835
1	80941	28125	13822	11.188	3.887
2	74259	26313	14965	11.113	3.938
3	68090	24570	16209	11.037	3.983
4	62396	22900	17564	10.959	4.022
5	57144	21304	19038	10.879	4.056
6	52299	19787	20642	10.796	4.084
7	47832	18350	22386	10.708	4.108
8	43714	16995	24282	10.615	4.127
9	39918	15721	26345	10.516	4.142
40	36420	14528	28589	10.412	4.153
1	33197	13413	31030	10.301	4.162
2	30230	12374	33703	10.188	4.170
3	27501	11402	36621	10.071	4.176
4	24991	10496	39852	9.959	4.183
5	22683	96526	43318	9.826	4.181
6	20568	88658	47279	9.724	4.192
7	18627	81331	51539	9.600	4.192
8	16849	74552	56227	9.474	4.192
9	15219	68338	61345	9.336	4.192
50	13725	62689	66963	9.190	4.198
1	12357	57602	73078	9.030	4.209
2	11103	53056	79768	8.857	4.232
3	99549	48965	87063	8.667	4.263
4	89035	45249	95112	8.468	4.304
5	79422	41853	10402	8.261	4.354
6	70640	38718	11387	8.044	4.409
7	62633	35807	12488	7.822	4.472
8	55343	38077	13718	7.592	4.538
9	48724	30499	15107	7.361	4.607
60	42727	28050	16677	7.126	4.678
1	37311	25712	18462	6.888	4.747
2	32433	23475	20501	6.649	4.813
3	28059	21338	22861	6.415	4.878
4	24150	19299	25587	6.179	4.938
5	20675	17363	28774	5.949	4.996
6	17598	15535	32497	5.719	5.048
7	14886	13818	36869	5.488	5.095
8	12507	12209	42042	5.258	5.133
9	10433	10707	48209	5.030	5.162
70	86347	93119	55620	4.803	5.179
1	70867	80269	64599	4.578	5.185
2	57635	68548	75572	4.356	5.180
3	46414	57943	89122	4.137	5.164
4	36984	48438	10604	3.922	5.136
5	29135	40006	12741	3.712	5.097
6	23672	32617	15474	3.508	5.047
7	17413	26220	19013	3.311	4.985
8	13186	20766	23658	3.120	4.913
9	98349	16183	29840	2.935	4.829
80	72162	12399	38287	2.763	4.747
1	52048	93266	49643		
2	36813	68777	65637		
3	25518	49679	88535		
4	17309	35076	12182		
5	11471	24199	17128		
6	74154	16260	24657		
7	46701	10638	36425		
8	28561	67719	55129		
9	16917	41906	85881		
90	96483	25205	13757		
1	52531	14712	22752		
2	26798	63982	38830		
3	12527	45640	70072		
4	51927	22995	13634		
5	18405	10295	29831		
6	52594	89681	76070		
7	10951	12242	24014		
8	17478	26147	10866		
9	00000	50517	57215		

DIFFERENCE OF AGE Fourteen Years.  
(Male the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	a <sub>x,y</sub>	a <sub>x,y</sub> <sup>2</sup>
29	10164	83706	11190	11.374	3.772
30	93374	31525	12102	11.300	3.815
1	85737	29514	13095	11.227	3.865
2	78683	27632	14176	11.154	3.917
3	72170	25842	15353	11.080	3.968
4	66158	24125	16635	11.005	4.013
5	60612	22483	18029	10.928	4.053
6	55495	20919	19546	10.847	4.089
7	50777	19435	21195	10.762	4.119
8	46427	18030	22987	10.672	4.145
9	42417	16706	24937	10.578	4.166
40	88721	15461	27058	10.477	4.183
1	85316	14296	29364	10.370	4.198
2	82178	13209	31874	10.256	4.210
3	79290	12194	34622	10.141	4.222
4	76633	11244	37638	10.024	4.232
5	74191	10355	40948	9.906	4.240
6	71945	95030	44516	9.769	4.243
7	69887	87603	48495	9.664	4.257
8	67999	80473	52974	9.535	4.263
9	66268	73920	57782	9.400	4.271
50	14682	67949	63020	9.253	4.282
1	13227	62553	68756	9.094	4.301
2	11894	57723	74984	8.919	4.328
3	10671	53360	81817	8.731	4.366
4	95515	49386	89293	8.529	4.410
5	85265	45739	97561	8.318	4.462
6	75898	42367	10675	8.102	4.523
7	67347	39226	11695	7.876	4.587
8	59558	36277	12840	7.647	4.658
9	52478	33484	14124	7.412	4.729
60	46061	30828	15583	7.178	4.804
1	40261	28290	17240	6.941	4.877
2	35034	25859	19133	6.703	4.948
3	30340	23537	21805	6.464	5.015
4	26144	21324	23828	6.230	5.081
5	22386	19221	26612	5.957	5.115
6	19073	17232	30190	5.758	5.202
7	16151	15360	34221	5.527	5.256
8	13586	13603	38985	5.297	5.303
9	11347	11961	44658	5.067	5.342
70	94039	10433	51733	4.865	5.397
1	77291	90202	59700	4.614	5.385
2	62956	77262	69760	4.392	5.389
3	50784	65500	82158	4.172	5.381
4	40539	54917	97611	3.957	5.361
5	32000	45491	11711	3.748	5.327
6	24956	37200	14197	3.543	5.281
7	19213	30000	17413	3.346	5.224
8	14589	23840	21623	3.155	5.155
9	10914	18649	27213	2.970	5.075
80	80355	14347	34740	2.793	4.984
1	58152	10841	45041		
2	41310	80352	59375		
3	28760	58934	79683		
4	19603	41443	10920		
5	13060	28747	15284		
6	84912	19457	21887		
7	58794	12808	32136		
8	38137	82190	48409		
9	19769	51283	74805		
90	11367	31144	11902		
1	62467	18353	19529		
2	32178	10579	33015		
3	15199	58103	58896		
4	63910	29635	11353		
5	22973	13501	24428		
6	66782	52565	61368		
7	14199	16657	19018		
8	23008	85913	84048		
9	00000	70315	43462		

DIFFERENCE OF AGE Fifteen Years.  
(Male the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	a <sub>x,y</sub>	a <sub>x,y</sub> <sup>2</sup>
30	98843	33147	11467	11.334	3.801
1	90783	30987	12407	11.263	3.845
2	83337	28996	13430	11.192	3.894
3	76462	27137	14544	11.121	3.947
4	70115	25373	15756	11.047	3.998
5	64259	23685	17075	10.972	4.044
6	58856	22076	18510	10.894	4.086
7	53873	20546	20069	10.812	4.123
8	49278	19096	21764	10.725	4.156
9	45042	17723	23607	10.633	4.184
40	41138	16429	25612	10.536	4.208
1	37540	15214	27792	10.433	4.228
2	34224	14077	30163	10.323	4.246
3	31170	13015	32744	10.206	4.262
4	28359	12023	35571	10.088	4.277
5	25773	11095	38647	9.960	4.288
6	23397	10228	42081	9.846	4.304
7	21212	94202	45756	9.706	4.310
8	19210	86711	49948	9.595	4.331
9	17373	79818	54439	9.458	4.345
50	15688	73521	59360	9.312	4.364
1	14143	67817	64708	9.152	4.388
2	12725	62694	70550	8.977	4.423
3	11425	58058	76910	8.787	4.465
4	10233	53820	83910	8.587	4.516
5	91413	49920	91593	8.373	4.572
6	81425	46299	10012	8.152	4.635
7	72304	42020	10964	7.927	4.607
8	63988	39738	12024	7.694	4.778
9	56423	36721	13220	7.459	4.855
60	49559	33844	14568	7.220	4.930
1	45531	31091	16109	6.983	5.008
2	37754	28451	17867	6.746	5.083
3	32725	25929	19883	6.507	5.155
4	28222	23525	22206	6.267	5.224
5	24208	21242	24916	6.032	5.293
6	20646	19080	28071	5.796	5.356
7	17500	17044	31791	5.563	5.418
8	14737	15129	36185	5.333	5.474
9	12322	13336	41411	5.103	5.523
70	10224	11665	47676	4.874	5.561
1	84144	10118	55248	4.649	5.590
2	68635	86755	64476	4.425	5.594
3	55449	73770	75840	4.205	5.595
4	44336	62033	89984	3.990	5.582
5	35059	51538	10779	3.779	5.555
6	27395	42270	13049	3.575	5.516
7	21136	34190	15977	3.377	5.463
8	16087	27257	19803	3.186	5.398
9	12066	21395	24872	3.001	5.321
80	89096	16521	31682	2.823	5.234
1	64691	12535	40975		
2	46128	93333	53871		
3	32255	68104	72080		
4	22080	48630	98283		
5	14781	33946	13700		
6	96607	23104	19530		
7	61550	15324	28517		
8	38135	98966	42708		
9	22912	62281	65687		
90	13266	39168	10367		
1	73475	22744	16896		
2	38187	13267	28339		
3	18218	72957	50076		
4	77381	37634	95421		
5	28218	17350	20340		
6	83179	68772	50252		
7	17998	21982	15342		
8	29745	48825	66561		
9	00000	96269	33610		

## DIFFERENCE OF AGE Sixteen Years.

(Male the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
				$a_{x,y}$	$a_{x,y}^2$
31	96099	32585	11757	11.298	3.831
2	88240	30446	12725	11.229	3.874
3	80983	28479	13779	11.159	3.924
4	74283	26648	14926	11.087	3.977
5	68100	24914	16174	11.014	4.030
6	62396	23259	17580	10.938	4.077
7	57134	21685	19005	10.858	4.121
8	52282	20190	20608	10.774	4.161
9	47807	18772	22351	10.685	4.196
40	43683	17431	24246	10.591	4.226
1	39882	16167	26307	10.492	4.253
2	36379	14982	28548	10.385	4.277
3	33152	13872	30987	10.273	4.299
4	30179	12834	33641	10.153	4.317
5	27443	11864	36550	10.030	4.336
6	24927	10956	39744	9.907	4.354
7	22615	10107	43253	9.782	4.372
8	20489	93215	47029	9.636	4.384
9	18541	85972	51329	9.517	4.413
50	16752	79348	56176	9.411	4.457
1	15112	73333	60950	9.211	4.470
2	13606	67918	66397	9.034	4.510
3	12224	63000	72361	8.845	4.559
4	10956	58497	78865	8.640	4.613
5	97940	54339	86071	8.430	4.677
6	87301	50466	93996	8.206	4.744
7	77576	46838	10283	7.977	4.816
8	68705	43414	11272	7.744	4.894
9	60627	40160	12300	7.457	4.940
60	53294	37052	13636	7.267	5.052
1	46654	34069	15060	7.026	5.131
2	40664	31206	16694	6.788	5.210
3	35278	28467	18567	6.550	5.285
4	30453	25855	20724	6.311	5.358
5	26146	23375	23220	6.071	5.428
6	22321	21029	26142	5.835	5.497
7	18938	18816	29560	5.598	5.562
8	15963	16732	33617	5.366	5.625
9	13362	14778	38438	5.136	5.680
70	11100	12954	44210	4.896	5.714
1	91458	11262	51179	4.681	5.764
2	74697	97041	59662	4.457	5.790
3	60430	82768	70097	4.236	5.802
4	48391	69810	83063	4.020	5.799
5	38328	58170	99371	3.809	5.780
6	30002	47851	12011	3.604	5.747
7	23192	38819	14684	3.406	5.700
8	17689	31039	18170	3.214	5.640
9	13299	24441	22779	3.029	5.567
80	98452	18937	28957	2.851	5.484
1	71692	14422	37368		
2	51287	10782	49009		
3	35996	79028	65398		
4	24748	56714	88905		
5	16638	39785	12331		
6	10926	27244	17507		
7	69977	18163	25454		
8	43599	11813	37910		
9	26343	74738	57951		

## DIFFERENCE OF AGE Seventeen Years.

(Male the elder.)

x	N <sub>x,y</sub>	N <sub>x,y</sub> <sup>2</sup>	D <sub>x,y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
				$a_{x,y}$	$a_{x,y}^2$
32	93403	32023	12058	11.263	3.861
3	85744	29909	13055	11.194	3.905
4	78672	27971	14141	11.125	3.955
5	72145	26171	15321	11.053	4.010
6	66122	24471	16605	10.980	4.063
7	60567	22853	18000	10.902	4.114
8	55443	21314	19516	10.820	4.160
9	50718	19853	21164	10.734	4.202
40	46361	18468	22956	10.643	4.240
1	42346	17158	24904	10.546	4.273
2	38645	15925	27022	10.443	4.303
3	35236	14768	29326	10.333	4.331
4	32094	13683	31835	10.217	4.356
5	29202	12668	34566	10.094	4.379
6	26539	11719	37562	9.969	4.402
7	24091	10830	40850	9.841	4.424
8	21842	10005	44456	9.710	4.448
9	19773	92450	48330	9.556	4.468
50	17876	85491	52731	9.426	4.508
1	16135	79164	57423	9.265	4.546
2	14536	73453	62539	9.091	4.594
3	13067	68255	68101	8.899	4.648
4	11720	63479	74213	8.698	4.711
5	10484	59060	80909	8.482	4.778
6	93519	54930	88330	8.261	4.852
7	83160	51050	96535	8.038	4.928
8	73701	47374	10572	7.791	5.008
9	65085	43872	11606	7.554	5.092
60	57254	40520	12770	7.311	5.174
1	50160	37298	14096	7.071	5.258
2	43753	34196	15607	6.829	5.337
3	37981	31225	17349	6.589	5.417
4	32821	28389	19353	6.352	5.494
5	28207	25695	21670	6.112	5.568
6	24102	23146	24363	5.872	5.639
7	20470	20744	27529	5.635	5.711
8	17270	18480	31257	5.398	5.776
9	14470	16353	35709	5.167	5.839
70	12033	14365	41034	4.938	5.895
1	99258	12518	47457	4.710	5.941
2	81164	10815	55267	4.486	5.977
3	65746	92509	64861	4.264	6.000
4	52721	78266	76772	4.047	6.009
5	41819	65416	91729	3.836	6.001
6	32788	53971	11073	3.631	5.976
7	25390	43915	13517	3.432	5.936
8	19402	35219	16700	3.240	5.882
9	14617	27815	20900	3.055	5.813
80	10846	2.620	26520	2.876	5.734
1	79183	16521	34154		
2	56809	12397	44694		
3	40001	91237	59495		
4	27604	65773	80663		
5	18638	46375	11154		
6	12292	31916	15757		
7	79093	21412	22817		
8	49582	14000	33828		
9	30092	89236	51440		
90	17641	55383	80315		
1	99029	33463	12381		
2	52203	19780	21356		
3	25513	11149	37187		
4	10953	58468	69639		
5	40733	27480	14536		
6	12299	11143	35169		
7	27398	36700	10417		
8	46558	83942	45993		
9	00000	17099	21479		

## DIFFERENCE OF AGE Eighteen YEARS.

(Male the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub>	D <sup>-1</sup> <sub>x'y</sub>	Annuities.	
				Joint Lives.	Rever-sionary.
33	90757	31461	12371	11·228	3·892
4	83293	29380	13398	11·160	3·936
5	76404	27475	14515	11·090	3·988
6	70046	25710	15729	11·018	4·044
7	64181	24048	17049	10·942	4·100
8	58770	22466	18483	10·862	4·152
9	53781	20962	20042	10·779	4·201
40	49180	19534	21737	10·690	4·246
1	44939	18182	23579	10·596	4·287
2	41030	16904	25581	10·496	4·324
3	37428	15700	27760	10·390	4·358
4	34109	14569	30130	10·277	4·390
5	31052	13508	32712	10·158	4·419
6	28237	12515	35523	10·031	4·446
7	25647	11587	38607	9·902	4·473
8	23265	10722	41987	9·768	4·502
9	21076	99235	45686	9·629	4·630
50	19062	91937	49650	9·464	4·565
1	17215	85290	54143	9·321	4·618
2	15518	79282	58921	9·143	4·671
3	13959	73801	64145	8·954	4·734
4	12527	68752	69843	8·749	4·802
5	11213	64065	76124	8·536	4·877
6	10009	59677	83032	8·311	4·955
7	89067	55539	90715	8·080	5·038
8	78992	51608	99251	7·840	5·122
9	69805	47848	10885	7·598	5·208
60	61452	44241	11971	7·356	5·296
1	53876	40765	13201	7·112	5·381
2	47031	37415	14609	6·871	5·466
3	40866	34196	16219	6·628	5·546
4	35336	31120	18083	6·390	5·627
5	30394	28194	20236	6·151	5·705
6	25996	25425	22737	5·911	5·781
7	22098	22815	25655	5·669	5·853
8	18663	20358	29109	5·433	5·926
9	15651	18047	33202	5·196	5·992
70	13028	15884	38121	4·966	6·055
1	10757	13871	44049	4·738	6·110
2	88062	12011	51249	4·513	6·156
3	71418	10302	60084	4·291	6·190
4	57342	87410	71039	4·074	6·210
5	45546	73285	84780	3·861	6·213
6	35763	60650	10221	3·655	6·199
7	27788	49497	12461	3·456	6·168
8	21232	39814	15372	3·264	6·120
9	16026	31538	19209	3·078	6·058
80	11917	24586	24332	2·900	5·982
1	87197	18847	31279		
2	62717	14190	40850		
3	44286	10482	54258		
4	30659	75871	73383		
5	20778	53734	10120		
6	13762	37167	14253		
7	88923	25067	20536		
8	55946	16494	30334		
9	34160	10568	45902		
90	20133	66076	71292		
1	11862	40149	11401		
2	60296	23907	18753		
3	29424	13578	32391		
4	12826	71793	60250		
5	48115	34018	12477		
6	14678	13903	29903		
7	32999	46306	87913		
8	56856	10720	36613		
9	00000	22281	17588		

## DIFFERENCE OF AGE Nineteen YEARS.

(Male the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub>	D <sup>-1</sup> <sub>x'y</sub>	Annuities.	
				Joint Lives.	Rever-sionary.
34	88158	30909	12696	11·193	3·924
5	80887	28863	13753	11·124	3·970
6	74177	26996	14900	11·052	4·022
7	67985	25269	16151	10·980	4·081
8	62273	23644	17507	10·902	4·139
9	57005	22098	18982	10·821	4·195
40	52147	20629	20584	10·734	4·246
1	47668	19235	22326	10·642	4·294
2	43539	17915	24220	10·545	4·339
3	39734	16668	26280	10·442	4·380
4	36227	15491	28520	10·332	4·418
5	32997	14385	30960	10·216	4·454
6	30023	13347	33617	10·093	4·487
7	27284	12376	36512	9·962	4·519
8	24764	11472	39682	9·827	4·552
9	22446	10636	43148	9·685	4·589
50	20316	98690	46934	9·535	4·632
1	18354	91719	50979	9·357	4·676
2	16554	85407	55556	9·197	4·745
3	14899	79641	60434	9·004	4·813
4	13379	74317	65786	8·802	4·889
5	11983	69362	71642	8·585	4·969
6	10703	64708	78121	8·361	5·055
7	95307	60311	85274	8·127	5·143
8	84585	56119	93267	7·889	5·234
9	74799	52098	10219	7·644	5·324
60	65892	48225	11228	7·398	5·415
1	57812	44485	12375	7·154	5·505
2	50502	40871	13680	6·909	5·591
3	43915	37394	15181	6·667	5·677
4	38000	34062	16906	6·424	5·759
5	32711	30888	18908	6·185	5·840
6	28002	27881	21232	5·945	5·920
7	23825	25046	23943	5·704	5·997
8	20139	22376	27128	5·463	6·070
9	16905	19869	30921	5·227	6·144
70	14083	17518	35446	4·992	6·209
1	11640	15327	40923	4·763	6·272
2	95375	13300	47568	4·537	6·327
3	77427	11433	55715	4·314	6·370
4	62231	97275	65807	4·095	6·401
5	49484	81799	78450	3·882	6·417
6	38898	67910	94471	3·675	6·416
7	30205	55597	11502	3·474	6·395
8	23148	44857	14171	3·280	6·357
9	17493	35642	17682	3·093	6·302
80	13021	27871	22363	2·912	6·233
1	95365	21431	28699		
2	69035	16189	37979		
3	48870	12002	49591		
4	38928	87127	66923		
5	23066	61962	92067		
6	15333	43056	12932		
7	99499	29180	18576		
8	62858	19296	27292		
9	38555	12442	41147		
90	22836	78192	63616		
1	12955	47857	10120		
2	69104	28647	16544		
3	33946	16381	28443		
4	14891	87257	52479		
5	56270	41704	10795		
6	17309	17183	25667		
7	39324	57661	74757		
8	68282	13507	30773		
9	00000	28306	14645		

## DIFFERENCE OF AGE Twenty Years.

(Male the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub> <sup>2</sup>	D <sub>x'y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
x	N <sub>x'y</sub>	N <sub>x'y</sub> <sup>2</sup>	D <sub>x'y</sub> <sup>-1</sup>	a <sub>x'y</sub>	a <sub>x'y</sub> <sup>2</sup>
35	85609	30368	13032	11.157	3.958
6	78526	28363	14119	11.087	4.005
7	71991	26537	15301	11.015	4.060
8	65961	24849	16585	10.940	4.121
9	60399	23261	17979	10.858	4.182
40	55270	21751	19495	10.775	4.240
1	50540	20316	21143	10.686	4.295
2	46180	18956	22939	10.593	4.348
3	42161	17667	24881	10.490	4.396
4	38457	16448	26999	10.383	4.441
5	35045	15298	29305	10.270	4.483
6	31902	14215	31817	10.150	4.528
7	29007	13200	34552	10.022	4.561
8	26343	12254	37528	9.886	4.599
9	23891	11381	40780	9.743	4.641
50	21635	10577	44326	9.590	4.688
1	19559	98448	48190	9.425	4.744
2	17648	91829	52309	9.231	4.803
3	15893	85771	56982	9.056	4.887
4	14279	80171	61980	8.850	4.969
5	12797	74946	67480	8.635	5.057
6	11437	70026	73522	8.409	5.148
7	10191	65362	80231	8.176	5.244
8	90503	60908	87673	7.935	5.340
9	80089	56620	96030	7.691	5.437
60	70602	52478	10541	7.442	5.532
1	61986	48463	11606	7.194	5.625
2	54189	44573	12825	6.950	5.716
3	47155	40823	14217	6.704	5.804
4	40836	37224	15824	6.462	5.890
5	35179	33785	17677	6.219	5.972
6	30138	30524	19839	5.979	6.056
7	25666	27446	22359	5.739	6.137
8	21716	24545	25317	5.498	6.214
9	18245	21820	28816	5.257	6.288
70	15216	19269	33010	5.023	6.361
1	12588	16888	38050	4.790	6.426
2	10325	14682	44191	4.563	6.488
3	83914	12648	51714	4.340	6.541
4	67527	10786	61022	4.121	6.582
5	53766	90939	72672	3.907	6.609
6	42327	75722	87416	3.700	6.619
7	32921	62187	10631	3.500	6.611
8	25276	50381	13081	3.306	6.584
9	19141	40110	16300	3.120	6.538
80	14284	31458	20586	2.941	6.476
1	10492	24259	26377		
2	75790	18377	34325		
3	53772	13664	45416		
4	37423	99610	61167		
5	25513	71100	83962		
6	17013	49609	11765		
7	11080	33774	16854		
8	70293	22449	24688		
9	43290	14547	37033		
90	25754	91992	57026		
1	14681	56585	90306		
2	78711	34109	14686		
3	38861	19601	25093		
4	17160	10514	46082		
5	65251	50603	94026		
6	20219	21034	22206		
7	46343	71171	64167		
8	81240	16805	26165		
9	00000	35586	12309		

## DIFFERENCE OF AGE Twenty-one Years.

(Male the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub> <sup>2</sup>	D <sub>x'y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
x	N <sub>x'y</sub>	N <sub>x'y</sub> <sup>2</sup>	D <sub>x'y</sub> <sup>-1</sup>	a <sub>x'y</sub>	a <sub>x'y</sub> <sup>2</sup>
36	83106	29855	13379	11.119	3.994
7	76208	27893	14497	11.048	4.044
8	69844	26108	15712	10.974	4.102
9	63972	24459	17032	10.896	4.166
40	58557	22907	18466	10.813	4.230
1	53563	21433	20024	10.725	4.292
2	48959	20033	21718	10.633	4.351
3	44714	18705	23559	10.534	4.407
4	40802	17445	25563	10.430	4.459
5	37197	16253	27742	10.319	4.509
6	33877	15128	30116	10.202	4.556
7	30819	14069	32702	10.078	4.601
8	28003	13081	35514	9.945	4.646
9	25410	12166	38857	9.800	4.692
50	23023	11327	41894	9.645	4.745
1	20826	10560	45514	9.478	4.806
2	18804	98641	49448	9.298	4.878
3	16940	92288	53652	9.089	4.951
4	15229	86303	58440	8.900	5.044
5	13656	80807	63576	8.682	5.137
6	12212	75619	69251	8.457	5.237
7	10888	70690	75508	8.221	5.338
8	96752	65965	82488	7.981	5.441
9	85675	61408	90271	7.734	5.543
60	75579	56992	99053	7.486	5.645
1	66402	52698	10896	7.235	5.742
2	58088	48523	12028	6.987	5.836
3	50585	44486	13328	6.742	5.929
4	43837	40603	14818	6.496	6.017
5	37793	36889	16546	6.253	6.104
6	32401	33356	18547	6.009	6.187
7	27614	30017	20891	5.769	6.271
8	23385	26867	23642	5.529	6.352
9	19666	23907	26893	5.289	6.429
70	16416	21135	30764	5.050	6.502
1	13594	18552	35435	4.817	6.574
2	11160	16154	41090	4.586	6.638
3	90785	13941	48043	4.362	6.698
4	73130	11921	56640	4.142	6.752
5	58290	10074	67388	3.928	6.789
6	45941	84105	80979	3.720	6.811
7	35776	69276	98374	3.519	6.815
8	27505	56243	12090	3.325	6.800
9	20859	44960	15047	3.139	6.765
80	15589	35391	18977	2.958	6.716
1	11471	27375	24281		
2	83010	20800	31548		
3	59012	15512	41670		
4	41161	11343	56018		
5	28130	81240	76739		
6	18809	56892	10729		
7	12288	38891	15333		
8	78231	25967	22399		
9	48380	16912	33499		
90	28896	10747	51324		
1	16543	66519	80952		
2	89115	40285	13104		
3	44221	23310	22274		
4	19624	12563	40655		
5	75121	60887	82564		
6	23421	25483	19342		
7	54081	86997	55515		
8	95548	20725	22458		
9	00000	44154	10466		

## DIFFERENCE OF AGE Twenty-two YEARS.

(Male the elder.)

$x$	$N_{x'y}$	$N_{x'y}^{\frac{3}{2}}$	$D_{x'y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
$a_{x'y}$	$a_{x'y}^{\frac{3}{2}}$				
37	80648	29347	13737	11·079	4·031
8	73931	27429	14887	11·006	4·083
9	67734	25684	16136	10·930	4·144
40	62017	24073	17493	10·849	4·211
1	56745	22558	18967	10·763	4·279
2	51883	21119	20569	10·672	4·344
3	47401	19752	22311	10·576	4·407
4	43270	18454	24205	10·474	4·467
5	39462	17223	26266	10·365	4·524
6	35955	16057	28510	10·251	4·578
7	32724	14955	30955	10·130	4·629
8	29749	13925	33612	9·999	4·680
9	27009	12969	36496	9·857	4·733
50	24485	12091	39620	9·701	4·790
1	22160	11289	43014	9·532	4·856
2	20019	10560	46701	9·349	4·932
3	18047	98928	50717	9·153	5·017
4	16230	92757	55025	8·931	5·104
5	14562	86983	59945	8·729	5·214
6	13029	81525	65244	8·501	5·320
7	11623	76326	71121	8·266	5·428
8	10335	71332	77631	8·023	5·538
9	91576	66500	84931	7·778	5·648
60	80836	61806	93112	7·527	5·755
1	71070	57227	10239	7·277	5·859
2	62215	52761	11292	7·025	5·958
3	54215	48428	12500	6·777	6·054
4	47016	44250	13893	6·531	6·147
5	40562	40244	15494	6·285	6·235
6	34802	36427	17360	6·042	6·324
7	29682	32810	19531	5·797	6·408
8	25155	29394	22091	5·557	6·493
9	21173	26179	25113	5·317	6·574
70	17690	23168	28710	5·079	6·652
1	14662	20361	33024	4·842	6·724
2	12049	17760	38266	4·611	6·796
3	98104	15354	44671	4·382	6·859
4	79099	13145	52619	4·162	6·917
5	63112	11132	62548	3·948	6·963
6	49794	93156	75090	3·739	6·995
7	38821	76946	91128	3·538	7·012
8	29892	62667	11188	3·343	7·011
9	22692	50264	13907	3·156	6·990
80	16983	39670	17518	2·975	6·949
1	12516	30780	22383		
2	90723	23459	29040		
3	64613	17548	38298		
4	45156	12870	51398		
5	30928	92463	70280		
6	20730	64969	98063		
7	13579	44576	13983		
8	86712	29884	20378		
9	53811	19551	30393		
90	32271	12487	46427		
1	18546	77653	72858		
2	10033	47308	11747		
3	50020	27495	19876		
4	22310	14921	36088		
5	85816	72641	72841		
6	26940	30618	16985		
7	62597	10524	48356		
8	11132	25319	19431		
9	00000	54366	89834		

## DIFFERENCE OF AGE Twenty-three YEARS.

(Male the elder.)

$x$	$N_{x'y}$	$N_{x'y}^{\frac{3}{2}}$	$D_{x'y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
$a_{x'y}$	$a_{x'y}^{\frac{3}{2}}$				
38	78235	28870	14106	11·036	4·072
9	71694	26995	15288	10·961	4·127
40	65660	25291	16572	10·881	4·191
1	60094	23718	17967	10·797	4·261
2	54961	22239	19483	10·708	4·333
3	50229	20834	21130	10·613	4·402
4	45866	19498	22922	10·513	4·469
5	41845	18229	24871	10·407	4·554
6	38141	17025	26993	10·295	4·596
7	34728	15883	29304	10·177	4·654
8	31585	14812	31817	10·049	4·713
9	28690	13815	34542	9·910	4·771
50	26023	12898	37493	9·757	4·836
1	23565	12058	40680	9·586	4·905
2	21299	11297	44136	9·401	4·986
3	19211	10598	47900	9·202	5·076
4	17289	99493	52016	8·993	5·175
5	15517	93438	56762	8·808	5·304
6	13892	87703	61518	8·546	5·395
7	12399	82235	67006	8·308	5·510
8	11032	76968	72591	8·008	5·587
9	97806	71860	79932	7·818	5·744
60	86391	66882	87605	7·568	5·849
1	76001	62016	96253	7·315	5·969
2	66578	57254	10612	7·065	6·076
3	58056	52620	11735	6·813	6·175
4	50381	48134	13029	6·564	6·271
5	43497	43823	14526	6·318	6·366
6	37346	39706	16257	6·071	6·455
7	31876	35799	18281	5·827	6·544
8	27034	32097	20652	5·583	6·629
9	22772	28611	23465	5·343	6·714
70	19042	25341	26810	5·105	6·794
1	15798	22291	30819	4·869	6·870
2	12994	19465	35662	4·634	6·942
3	10590	16855	41601	4·406	7·012
4	85458	14454	48926	4·181	7·072
5	68249	12263	58108	3·966	7·126
6	53901	10284	69697	3·757	7·168
7	42067	85140	84502	3·555	7·195
8	32418	69531	10364	3·360	7·206
9	24647	55942	12869	3·172	7·199
80	18471	44297	16191	2·991	7·172
1	13631	34482	20662		
2	98960	26362	26771		
3	70555	19780	35255		
4	49426	14552	47239		
5	33918	10485	64484		
6	22783	73905	89809		
7	14959	50877	12781		
8	95777	34233	18584		
9	59611	22487	27650		
90	35871	14426	42123		
1	20698	90155	65906		
2	11239	55171	10572		
3	56268	32253	17817		
4	25214	17577	32202		
5	97482	86184	64657		
6	30746	36480	14984		
7	71952	12629	42461		
8	12866	30602	16924		
9	00000	66272	77722		

## DIFFERENCE OF AGE Twenty-four YEARS.

(Male the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub> <sup>2</sup>	D <sub>x'y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
				$a_{x'y}$	$a_{x'y}^2$
39	75863	28425	14487	10.990	4.118
40	69494	26595	15702	10.911	4.176
1	63619	24930	17022	10.829	4.244
2	58201	23835	18456	10.742	4.318
3	53205	21952	20015	10.649	4.394
4	48599	20579	21709	10.550	4.467
5	44353	19273	23553	10.446	4.539
6	40440	18031	25559	10.336	4.609
7	36836	16842	27744	10.220	4.673
8	33516	15732	30120	10.095	4.738
9	30457	14695	32696	9.958	4.805
50	27639	13738	35485	9.808	4.875
1	25042	12861	38497	9.640	4.951
2	22646	12065	41741	9.453	5.036
3	20437	11334	45270	9.252	5.131
4	18401	10655	49126	9.040	5.234
5	16527	10018	53354	8.818	5.345
6	14801	94170	57923	8.573	5.454
7	13218	88425	63179	8.351	5.587
8	11766	82885	68891	8.106	5.710
9	10438	77498	75288	7.859	5.835
60	92253	72236	82447	7.606	5.956
1	81211	67075	90560	7.354	6.074
2	71186	62014	99753	7.101	6.186
3	62118	57073	11028	6.850	6.294
4	53942	52275	12232	6.598	6.394
5	46602	47646	13624	6.349	6.491
6	40041	43216	15241	6.103	6.587
7	34200	39001	17120	5.855	6.677
8	29027	35004	19331	5.611	6.767
9	24468	31226	21938	5.368	6.850
70	20476	27680	25051	5.129	6.934
1	17002	24368	28780	4.893	7.013
2	13997	21297	33281	4.658	7.081
3	11418	18461	38770	4.427	7.157
4	92229	15856	45563	4.202	7.224
5	73721	13475	54030	3.983	7.281
6	58277	11321	64750	3.773	7.330
7	45528	93922	78433	3.571	7.367
8	35122	76881	96100	3.375	7.388
9	26783	62027	11921	3.187	7.394
80	20058	49269	14982	3.005	7.381
1	14822	38481	19097		
2	10775	29517	24713		
3	76983	22217	32500		
4	53987	16395	43484		
5	37118	11850	59266		
6	24978	83772	82401		
7	16434	57850	11705		
8	10547	39055	16985		
9	65809	25748	25216		
90	39714	16583	38321		
1	22991	10408	59796		
2	12534	63993	95636		
3	62983	37571	16036		
4	28341	20595	28867		
5	11008	10139	57696		
6	34900	43239	13301		
7	82059	15028	37461		
8	14771	36698	14861		
9	00000	79918	67698		

## DIFFERENCE OF AGE Twenty-five YEARS.

(Male the elder.)

x	N <sub>x'y</sub>	N <sub>x'y</sub> <sup>2</sup>	D <sub>x'y</sub> <sup>-1</sup>	Annuities.	
				Joint Lives.	Rever-sionary.
				$a_{x'y}$	$a_{x'y}^2$
40	73531	27985	14879	10.941	4.164
1	67331	26198	16128	10.859	4.225
2	61612	24574	17485	10.773	4.297
3	56337	23075	18960	10.681	4.375
4	51474	21664	20563	10.585	4.455
5	46991	20321	22307	10.482	4.533
6	42860	19044	24204	10.374	4.609
7	39053	17829	26271	10.260	4.684
8	35547	16681	28517	10.137	4.757
9	32316	15608-	30953	10.003	4.831
50	29339	14612	38589	9.855	4.908
1	26594	13698	36435	9.690	4.991
2	24063	12865	39501	9.505	5.082
3	21727	12101	42813	9.302	5.181
4	19573	11391	46429	9.088	5.289
5	17588	10724	50391	8.863	5.404
6	15762	10092	54756	8.631	5.526
7	14081	94898	59488	8.377	5.645
8	12542	89077	64956	8.147	5.766
9	11132	83410	70932	7.896	5.916
60	98441	77861	77658	7.645	6.047
1	86708	72406	85228	7.390	6.171
2	76053	67038	93853	7.138	6.292
3	66406	61787	10366	6.884	6.405
4	57706	56672	11494	6.633	6.514
5	49888	51721	12790	6.381	6.615
6	42892	46965	14294	6.131	6.713
7	38661	42430	16050	5.884	6.810
8	31137	38117	18103	5.637	6.900
9	26267	34037	20534	5.394	6.989
70	21997	30195	23420	5.152	7.072
1	18279	26603	26892	4.916	7.154
2	15061	23268	31079	4.681	7.231
3	12297	20187	36182	4.449	7.304
4	99421	17356	42463	4.222	7.370
5	79547	14773	50317	4.003	7.433
6	62937	12432	60205	3.789	7.485
7	49214	10333	72866	3.586	7.529
8	38003	84758	89199	3.390	7.560
9	28956	68541	11055	3.201	7.577
80	21751	54595	13878	3.019	7.577
1	16092	42775	17956		
2	11714	32923	22840		
3	83803	24862	30000		
4	58857	18405	40087		
5	40527	13344	54555		
6	27322	94625	75733		
7	18011	65538	10789		
8	11582	44382	15555		
9	72434	29356	23047		
90	43820	18974	34948		
1	25437	11956	54400		
2	13913	73811	86771		
3	70190	43536	14506		
4	31699	23964	25980		
5	12364	11868	51719		
6	39382	50803	11869		
7	93091	17798	33252		
8	16822	48642	13111		
9	00000	95686	59446		

## DIFFERENCE OF AGE Twenty-six YEARS.

(Male the elder.)

$x$	$N_{x'y}$	$N_{x'y}^{\frac{2}{3}}$	$D_{x'y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
41	71238	27579	15283	10·887	4·215
2	65202	25835	16567	10·802	4·280
3	59634	24249	17962	10·711	4·356
4	54501	22784	19479	10·616	4·438
5	49768	21405	21129	10·515	4·523
6	45406	20091	22924	10·409	4·606
7	41386	18841	24878	10·296	4·687
8	37683	17659	27002	10·175	4·768
9	34270	16550	29306	10·043	4·850
50	31125	15518	31798	9·897	4·934
1	28226	14567	34489	9·735	5·024
2	25551	13699	37386	9·553	5·122
3	23083	12900	40515	9·352	5·226
4	20805	12157	43909	9·135	5·338
5	18706	11460	47624	8·909	5·458
6	16772	10798	51713	8·673	5·584
7	14994	10165	56233	8·432	5·716
8	13359	95548	61161	8·170	5·844
9	11863	89594	66881	7·934	5·992
60	10497	83757	73164	7·680	6·028
1	92510	78004	80277	7·426	6·262
2	81188	72331	88328	7·171	6·389
3	70935	66761	97532	6·918	6·511
4	61680	61325	10805	6·665	6·626
5	53360	56046	12019	6·413	6·736
6	45908	50960	13419	6·160	6·838
7	39265	46090	15052	5·910	6·937
8	33372	41449	16971	5·664	7·034
9	28172	37048	19229	5·417	7·124
70	23610	32898	21922	5·176	7·212
1	19633	29007	25141	4·936	7·293
2	16189	25390	29039	4·701	7·373
3	13229	22044	33788	4·470	7·448
4	10706	18969	39629	4·243	7·517
5	85735	16162	46892	4·020	7·579
6	67899	13623	56068	3·807	7·638
7	53139	11341	67752	3·600	7·684
8	41072	93195	82868	3·404	7·723
9	31325	75517	10260	3·214	7·748
80	23555	60291	12869	3·031	7·759
1	17446	47370	16369		
2	12714	36574	21133		
3	91080	27715	27728		
4	64055	20587	37003		
5	44171	14974	50292		
6	29827	10651	69713		
7	19696	74000	98703		
8	12689	50260	14273		
9	79516	33346	21107		
90	48209	81623	81941		
1	28052	13672	49610		
2	15384	84712	78939		
3	77853	50163	13161		
4	53502	27737	23501		
5	13819	13792	46548		
6	44201	59410	10639		
7	10499	20884	29672		
8	19067	51659	11638		
9	00000	11358	52446		

## DIFFERENCE OF AGE Twenty-seven YEARS.

(Male the elder.)

$x$	$N_{x'y}$	$N_{x'y}^{\frac{2}{3}}$	$D_{x'y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
42	68981	27198	15698	10·829	4·270
3	63105	25495	17019	10·740	4·339
4	57686	23945	18454	10·645	4·419
5	52690	22513	20015	10·546	4·506
6	48085	21163	21714	10·441	4·595
7	43841	19878	23562	10·330	4·684
8	39930	18661	25571	10·211	4·772
9	36326	17518	27749	10·080	4·861
50	33005	16453	80105	9·936	4·953
1	29942	15467	82649	9·776	5·050
2	27116	14564	85488	9·623	5·168
3	24508	13731	88346	9·398	5·265
4	22101	12955	91552	9·183	5·383
5	19881	12226	94039	8·954	5·506
6	17835	11534	98874	8·717	5·637
7	15952	10871	10310	8·462	5·774
8	14223	10229	57815	8·123	5·914
9	12635	96051	62973	7·957	6·049
60	11185	89917	68985	7·716	6·203
1	98628	83866	75633	7·460	6·343
2	86608	77883	83197	7·206	6·480
3	75714	71996	91790	6·950	6·609
4	65877	66230	10166	6·697	6·733
5	57026	60620	11298	6·443	6·849
6	49096	55196	12610	6·191	6·960
7	42020	49989	14131	5·938	7·064
8	35737	45006	15916	5·688	7·163
9	30189	40270	18027	5·442	7·259
70	25318	35793	20528	5·197	7·348
1	21069	31590	23532	4·958	7·434
2	17385	27672	27149	4·720	7·513
3	14218	24043	31571	4·489	7·591
4	11516	20703	37006	4·262	7·661
5	92305	17654	43762	4·039	7·726
6	73167	14894	52252	3·823	7·782
7	57318	12419	63095	3·616	7·836
8	44340	10222	77051	3·416	7·876
9	33849	82984	95246	3·224	7·904
80	25477	66386	11945	3·043	7·930
1	18889	52280	15179		
2	13782	40479	19578		
3	98841	30772	25657		
4	69602	22937	34201		
5	48062	16740	46425		
6	32501	11946	64266		
7	21495	83261	90859		
8	13872	56725	13118		
9	87084	87745	19366		
90	52900	24549	29253		
1	30846	15571	45343		
2	16955	96795	71990		
3	86028	57519	11973		
4	39130	81927	21323		
5	15381	15949	42107		
6	49373	68967	95756		
7	11777	24405	26598		
8	21481	60587	10385		
9	00000	13434	46553		

## DIFFERENCE OF AGE Twenty-eight Years.

(Male the elder.)

$x$	$N_{x,y}$	$N_{x,y}^{-2}$	$D_{x,y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
$a_{x,y}$	$a_{x,y}^{-2}$	$D_{x,y}^{-1}$			
43	66759	26841	16127	10·766	4·329
4	61039	25176	17485	10·673	4·402
5	55766	23661	18962	10·574	4·487
6	50904	22260	20369	10·470	4·579
7	46423	20939	22318	10·361	4·673
8	42294	19688	24218	10·243	4·768
9	38489	18512	26278	10·115	4·865
50	34981	17414	28506	9·972	4·964
1	31746	16396	30912	9·813	5·068
2	28761	15460	33501	9·635	5·179
3	26006	14593	36296	9·439	5·297
4	23463	13784	39327	9·227	5·421
5	21117	13022	42622	9·000	5·550
6	18953	12299	46321	8·760	5·685
7	16961	11606	50193	8·513	5·825
8	15130	10934	54607	8·262	5·971
9	13450	10277	59528	8·007	6·118
60	11910	96343	64955	7·736	6·258
1	10308	89985	71313	7·494	6·417
2	92322	83691	78383	7·236	6·560
3	80756	77483	86453	6·982	6·699
4	70304	71388	95674	6·726	6·830
5	60896	65439	10630	6·473	6·956
6	52460	59675	11854	6·217	7·074
7	44930	54122	13280	5·967	7·187
8	38238	48793	14943	5·714	7·291
9	32323	43708	16908	5·465	7·390
70	27127	38890	19245	5·221	7·484
1	22589	34356	22037	4·978	7·571
2	18654	30124	25412	4·740	7·655
3	15266	26192	29515	4·506	7·731
4	12874	22570	34578	4·279	7·804
5	99269	19259	40866	4·057	7·870
6	78762	16260	48764	3·841	7·929
7	61755	13571	58801	3·631	7·980
8	47819	11187	71756	3·431	8·027
9	36536	90968	88628	3·238	8·062
80	27525	72909	11097	3·054	8·091
1	20427	57532	14089		
2	14919	44648	18155		
3	10712	34038	23768		
4	75518	25454	31647		
5	52213	18642	42907		
6	35356	13350	59324		
7	23417	93347	88758		
8	15135	63800	12075		
9	95172	42584	17799		
90	57914	27776	26840		
1	33833	17669	41527		
2	18635	11016	65797		
3	94764	65666	10919		
4	43213	36573	19398		
5	17037	18339	38203		
6	54922	79670	86619		
7	13149	28295	23939		
8	24073	70754	93094		
9	00000	15718	41540		

## DIFFERENCE OF AGE Twenty-nine Years.

(Male the elder.)

$x$	$N_{x,y}$	$N_{x,y}^{-2}$	$D_{x,y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
$a_{x,y}$	$a_{x,y}^{-2}$	$D_{x,y}^{-1}$			
44	64568	26504	16569	10·698	4·391
5	59002	24877	17966	10·600	4·469
6	53870	23395	19470	10·488	4·555
7	49140	22024	21142	10·389	4·636
8	44781	20739	22939	10·272	4·757
9	40763	19530	24888	10·145	4·861
50	87059	18399	26996	9·904	4·967
1	33642	17350	29270	9·847	5·078
2	30490	16384	31718	9·671	5·197
3	27579	15486	34361	9·476	5·321
4	24893	14644	37226	9·267	5·451
5	22414	13849	40340	9·042	5·587
6	20128	13093	43741	8·804	5·727
7	18021	12368	47470	8·555	5·871
8	16083	11666	51606	8·300	6·020
9	14305	10979	56221	8·042	6·173
60	12676	10303	61402	7·783	6·326
1	11187	96359	67146	7·512	6·470
2	98333	89747	73905	7·268	6·633
3	86071	83216	81456	7·011	6·778
4	74975	76788	90116	6·756	6·920
5	64979	70500	10004	6·500	7·053
6	56013	64386	11153	6·247	7·181
7	48002	58486	12483	5·993	7·301
8	40880	52804	14042	5·740	7·415
9	34580	47366	15873	5·489	7·518
70	29040	42194	18050	5·242	7·616
1	24199	37315	20659	4·999	7·709
2	19997	32749	23797	4·759	7·793
3	16377	28503	27627	4·524	7·875
4	13284	24579	32327	4·294	7·946
5	10665	20987	38185	4·072	8·014
6	84689	17731	45537	3·856	8·074
7	66467	14809	54877	3·648	8·127
8	51513	12219	66872	3·445	8·171
9	39397	99510	82537	3·252	8·213
80	29705	79883	10318	3·065	8·242
1	22065	63152	13089		
2	16131	49108	16851		
3	11594	37524	22040		
4	81826	28140	29316		
5	56640	20677	39704		
6	38401	14859	54830		
7	25468	10427	77317		
8	16484	71496	11131		
9	10381	47873	16385		
90	63271	31321	24668		
1	37026	19980	38101		
2	20431	12492	60259		
3	10410	74676	99798		
4	47577	41718	17690		
5	18804	20989	34755		
6	60800	91533	78589		
7	14621	32666	21655		
8	26854	82007	83786		
9	00000	18346	37238		

## DIFFERENCE OF AGE THIRTY YEARS.

(Male the elder.)

$x$	$N_{x'y}$	$N_{x'y}^{-\frac{1}{2}}$	$D_{x'y}^{-1}$	Annuities.	
				Joint Lives.	Rever-sionary.
45	62411	26190	17025	10·625	4·459
6	56995	24598	18464	10·524	4·542
7	52002	23147	20029	10·415	4·636
8	47400	21813	21730	10·300	4·740
9	43158	20571	23574	10·174	4·849
50	39247	19409	25567	10·034	4·962
1	35639	18329	27718	9·678	5·080
2	32310	17333	30034	9·704	5·206
3	29236	16405	32533	9·511	5·337
4	26398	15533	35240	9·303	5·474
5	23779	14707	38184	9·080	5·616
6	21364	13918	41398	8·844	5·762
7	19138	13160	44922	8·597	5·912
8	17089	12426	48805	8·340	6·065
9	15207	11707	53135	8·080	6·221
60	13482	10999	57991	7·818	6·378
1	11907	10299	63473	7·558	6·537
2	10470	96053	69587	7·286	6·684
3	91676	89191	76803	7·041	6·850
4	79898	82430	84903	6·784	6·999
5	69285	75798	94229	6·529	7·142
6	59758	69336	10496	6·272	7·278
7	51244	63077	11745	6·019	7·408
8	43668	57039	13200	5·764	7·529
9	36964	51240	14916	5·514	7·643
70	31062	45708	16945	5·263	7·745
1	25901	40470	19876	5·019	7·841
2	21419	35557	22309	4·778	7·932
3	17553	30976	25871	4·541	8·014
4	14248	26738	30258	4·311	8·090
5	11447	22847	35699	4·086	8·156
6	90971	19315	42549	3·871	8·218
7	71457	16142	51345	3·662	8·272
8	55433	13328	62409	3·460	8·318
9	42433	10864	76920	3·264	8·357
80	82026	87342	96093	3·077	8·393
1	23810	69158	12170		
2	17422	53877	15655		
3	12533	41250	20457		
4	88548	31005	27184		
5	61359	22847	36779		
6	41649	16473	50736		
7	27656	11601	71461		
8	17924	79828	10275		
9	11303	53628	15104		
90	68994	35198	22708		
1	40437	22521	35018		
2	22350	14118	55289		
3	11409	84623	91398		
4	52244	47406	16169		
5	20694	23923	31696		
6	67075	10467	71496		
7	16178	37493	19647		
8	29838	94614	75792		
9	00000	21220	33515		

## ANNUITIES. DAUGHTERS, UNMARRIED. 4½ PER CENT.

	$D_u$	$N_u$	$D_u^{-1}$	$a_u$		$D_u$	$N_u$	$D_u^{-1}$	$a_u$
0	1·000000	10924892	1·000000	10·925	60	53103	495549	18831	9·332
1	828029	10096863	12077	12·194	1	49350	446199	20263	9·041
2	743307	9353556	18458	12·583	2	45763	400437	21852	8·750
3	686181	8667425	14574	12·632	3	42849	358088	23613	8·456
4	640711	8026714	15608	12·528	4	39084	319004	25586	8·162
5	602480	7424434	16604	12·328	5	35971	283038	27800	7·868
6	568696	6855738	17584	12·055	6	33010	250023	30294	7·574
7	538460	6317278	18571	11·732	7	30184	219839	38130	7·283
8	510597	5806681	19585	11·372	8	27501	192338	36362	6·994
9	484855	5321826	20625	10·976	9	24954	167384	40074	6·708
10	460904	4860922	21696	10·546	70	22544	144840	44358	6·425
1	438475	4422447	22806	10·086	1	20264	124576	49349	6·148
2	417346	4005101	23961	9·597	2	18122	106434	55182	5·874
3	397332	3607769	25168	9·080	3	16111	90343	62069	5·607
4	378294	3229475	26434	8·537	4	14235	76108	70249	5·347
5	360113	2869362	27769	7·968	5	12491	63617	80058	5·098
6	336674	2532688	29703	7·523	6	10882	52735	91895	4·846
7	303718	2228970	32925	7·339	7	9405	43330	10688	4·607
8	266967	1962003	37458	7·849	8	8060	35270	12407	4·376
9	230625	1731378	43360	7·507	9	6845	28425	14609	4·153
20	197241	1584137	50699	7·778	80	5758	22667	17367	3·938
1	167996	1366141	59527	8·132	1	4792	17875	20868	3·730
2	143664	1222477	69607	8·509	2	3944	13931	25355	3·532
3	123466	1099011	80994	8·901	3	3209	10722	31162	3·341
4	106707	992304	93715	9·299	4	2578	8144	38790	3·159
5	92782	899522	10778	9·695	5	2045	6099	48900	2·982
6	81183	818339	12818	10·080	6	1598	4501	62578	2·817
7	71511	746828	13984	10·444	7	1229	32721	81367	2·663
8	63387	683441	15776	10·771	8	9333	23389	10715	2·506
9	56512	626929	17696	11·094	9	6962	16426	14364	2·359
30	50653	576276	19742	11·377	90	5101	11325	19604	2·220
1	45623	530653	21919	11·631	1	8661	7664	27815	2·093
2	41289	489364	24220	11·852	2	2580	5084	38760	1·971
3	37522	451842	26651	12·042	3	1785	3239	56022	1·848
4	34214	417628	29228	12·206	4	1213	2086	82440	1·720
5	31292	3863386	31957	12·346	5	794	1292	12594	1·627
6	28692	357644	34853	12·465	6	512	780	19581	1·523
7	26563	331281	37932	12·566	7	322	458	81056	1·422
8	24270	307011	41203	12·650	8	201	257	49751	1·279
9	22385	284626	44673	12·715	9	115	1418	86957	1·233
40	20683	268943	48349	12·761	100	735	683	18605	0·929
1	19144	244799	52236	12·787	1	852	831	28409	
2	17744	227055	56357	12·796	2	224	107	44643	
3	16470	210585	60716	12·786	3	107			
4	15313	195272	65304	12·752					
5	14257	181015	70141	12·697					
6	13293	167728	75228	12·617					
7	12411	155311	80574	12·514					
8	11600	143711	86207	12·389					
9	10854	132857	92132	12·240					
50	10163	1226987	98396	12·073					
1	95687	1181250	10451	11·823					
2	90036	1041214	11107	11·565					
3	84684	956530	11809	11·296					
4	79608	876922	12562	11·016					
5	74678	802244	13891	10·743					
6	69966	732278	14293	10·466					
7	65456	666822	15277	10·187					
8	61143	605679	16355	9·906					
9	57027	548652	17536	9·621					

## ANNUITIES. FATHERS AND DAUGHTERS. DIFF. 34. 4½ PER CENT.

Ages.		$\frac{x+u}{2}$	$l_x$	$l_{x+u}$	$D_{x+u}$	$N_{x+u}$	$D_{x+u}^{-1}$	$a_{x+u}$	$u$
$x$	$u$								
84	0	17	67780	677800	3207190	26283192	31180	8·195	0
5	1	18	66031	571360	2587120	23696072	38653	9·159	1
6	2	19	64317	522068	2262130	21433942	44206	9·475	2
7	3	20	62640	490465	203678	19400264	49172	9·539	3
8	4	21	61001	466084	1849363	17550901	54073	9·490	4
9	5	22	59399	445819	1692779	15858122	59074	9·368	5
40	6	23	57834	428313	1556726	14301396	64237	9·187	6
1	7	24	56306	412593	1434600	12866796	69706	8·969	7
2	8	25	54815	398023	1324344	11542452	75509	8·716	8
3	9	26	53359	384473	1224172	10318280	81688	8·429	9
4	10	27	51936	371742	1132666	9185614	88287	8·110	10
5	1	28	50545	359668	1048686	8136928	95357	7·759	1
6	2	29	49184	348110	971279	7165649	10296	7·378	2
7	3	30	47852	336950	899657	6265992	11117	6·966	3
8	4	31	46556	326162	833552	5432640	12000	6·519	4
9	5	32	45303	315726	771950	4660690	12954	6·037	5
50	16	33	44099	300261	702524	3958166	14234	5·634	6
1	7	34	42949	275677	617229	3340937	16201	5·413	7
2	8	35	41857	246785	528748	2812189	18913	5·319	8
3	9	36	40809	217206	445333	2366856	22455	5·315	9
4	20	37	39791	189282	371870	1995486	26927	5·373	20
5	1	38	38792	164241	308363	1687123	32429	5·471	1
6	2	39	37800	143020	256958	1430165	38917	5·566	2
7	3	40	36806	125067	215026	1215139	46506	5·651	3
8	4	41	35799	109864	180754	1034385	55324	5·723	4
9	5	42	34769	96953	152643	681742	65512	5·776	5
60	26	43	83708	85945	129485	752257	77229	5·810	6
1	7	44	82608	76531	110337	641920	90631	5·818	7
2	8	45	81464	68403	94372	547548	10696	5·857	8
3	9	46	80277	61823	80961	466587	12352	5·763	9
4	30	47	29048	55107	69621	396966	14363	5·702	30
5	1	48	27780	49604	59970	336996	16675	5·619	1
6	2	49	26477	44712	51728	285268	19332	5·515	2
7	3	50	25143	40322	44640	240628	22401	5·390	3
8	4	51	23778	36335	38494	202134	26039	5·263	4
9	5	52	22385	32693	33144	168990	30171	5·099	5
70	36	53	20968	29843	28467	140523	35128	4·936	6
1	7	54	19533	26246	24366	116157	41041	4·767	7
2	8	55	18088	23382	20772	95385	48142	4·592	8
3	9	56	16688	20729	17622	77763	56747	4·413	9
4	40	57	15191	18275	14867	62896	67263	4·230	40
5	1	58	13756	16006	12461	50435	80250	4·047	1
6	2	59	12345	13913	10365	40070	96479	3·866	2
7	3	60	10970	11992	8549	31521	11697	3·687	3
8	4	61	9646	10245	6989	24532	14308	3·510	4
9	5	62	8386	8686	5670	18862	17637	3·327	6
80	46	63	7203	7253	4531	14331	22070	3·163	6
1	7	64	6107	6000	3587	10744	27878	2·995	7
2	8	65	5106	4899	2803	7941	35676	2·833	8
3	9	66	4206	3946	2160	5781	46296	2·676	9
4	50	67	3410	3130	1640	4141	60976	2·525	50
5	1	68	2718	2455	1231	2910	81235	2·364	1
6	2	69	2127	1889	906·2	2003·8	11035	2·211	2
7	3	70	1633	1425	654·1	1349·7	15288	2·063	3
8	4	71	1228	1053	462·6	887·1	21617	1·918	4
9	5	72	905	761	319·9	567·2	31260	1·773	5
90	56	73	653	537	216·0	351·2	46296	1·626	6
1	7	74	460	370	142·4	208·79	70225	1·466	7
2	8	75	317	249	91·72	117·07	10903	1·276	8
3	9	76	209	160	56·40	60·67	17730	1·076	9
4	60	77	129	96	82·88	28·29	80883	·874	60
5	1	78	72	52	16·79	11·50	59559	·685	1
6	2	79	35	25	7·72	3·78	12953	·490	2
7	3	80	14	9	2·66	1·12	37594	·421	3
8	4	81	4	3	·85	·27	11765	·318	4
9	5	82	1	1	·27	·00		·000	5

ANNUITIES. DAUGHTERS WITH FATHERS LIVING.  $4\frac{1}{2}$  PER CENT.

	Ages.			Ages.			Life Reversionary $a_u - a_{x+u}$	
	x	u	$a_u - a_{x+u}$	x	u	$a_u - a_{x+u}$		
	34	0	2.730	70	36	7.529		
	5	1	3.035	1	7	7.799		
	6	2	3.108	2	8	6.058		
	7	3	3.093	3	9	8.802		
	8	4	3.038	4	40	8.581		
	9	5	2.960	5	1	8.740		
				6	2	8.930		
	40	6	2.868	7	3	9.099		
	1	7	2.763	8	4	9.242		
	2	8	2.656	9	5	9.370		
	3	9	2.547					
	4	10	2.436	80	46	9.454		
	5	1	2.327	1	7	9.519		
	6	2	2.219	2	8	9.556		
	7	3	2.114	3	9	9.564		
	8	4	2.018	4	50	9.548		
	9	5	1.931	5	1	9.459		
				6	2	9.854		
	50	16	1.889	7	3	9.933		
	1	7	1.926	8	4	9.098		
	2	8	2.030	9	5	8.970		
	3	9	2.192					
	4	20	2.405	90	56	8.840		
	5	1	2.661	1	7	8.721		
	6	2	2.943	2	8	8.630		
	7	3	3.250	3	9	8.545		
	8	4	3.576	4	60	8.458		
	9	5	3.919	5	1	8.356		
				6	2	8.260		
	60	26	4.270	7	3	8.035		
	1	7	4.626	8	4	7.844		
	2	8	4.914	9	5	7.868		
	3	9	5.331					
	4	30	5.675					
	5	1	6.012					
	6	2	6.337					
	7	3	6.652					
	8	4	6.943					
	9	5	7.247					

## THE FOREGOING ANNUITIES DEFERRED.

Age.	Single Life.			Joint Lives.			Reversionary.			Age. u
	u	Deferred till 6.	Deferred till 12.	Deferred till 21.	Deferred till 6.	Deferred till 12.	Deferred till 21.	Deferred till 6.	Deferred till 12.	Deferred till 21.
0	6.856	4.005	1.366	4.459	2.234	0.526	2.897	1.771	0.840	0
1	8.280	4.827	1.650	5.528	2.770	0.652	2.752	2.067	0.998	1
2	9.223	5.388	1.838	6.322	3.168	0.746	2.901	2.220	1.092	2
3	9.992	5.837	1.991	7.032	3.523	0.830	2.960	2.314	1.161	3
4	10.700	6.251	2.132	7.733	3.875	0.912	2.987	2.376	1.220	4
5	11.383	6.650	2.268	8.448	4.233	0.997	2.935	2.417	1.271	5
6	12.055	7.043	2.402	9.187	4.603	1.084	2.868	2.440	1.318	6
7		7.438	2.537		4.995	1.176		2.443	1.361	7
8		7.844	2.676		5.411	1.274		2.453	1.402	8
9		8.261	2.818		5.853	1.378		2.408	1.440	9
10		8.689	2.964		6.326	1.490		2.366	1.474	10
11		9.134	3.116		6.833	1.609		2.301	1.507	11
12		9.597	3.273		7.378	1.737		2.218	1.536	12
13			3.438			1.876			1.562	13
14			3.611			2.025			1.586	14
15			3.794			2.185			1.609	15
16			4.058			2.401			1.657	16
17			4.498			2.733			1.765	17
18			5.117			3.191			1.926	18
19			5.924			3.788			2.136	19
20			6.946			4.543			2.883	20
21			8.132			5.471			2.661	21

## SONS.

ENGLISH LIFE TABLE No. 3. 4½ PER CENT. TEMPORARY ANNUITIES.

s	$l_s$	$D_s$	$N_s$	$D_s^{-1}$	$a_s$	Deferred	
						till 6.	till 12.
0	511745	511745	4874695	19541	9·526	5·600	2·853
1	428026	409594	4465101	24414	10·901	6·997	3·564
2	400505	366754	4098347	27266	11·175	7·814	3·981
3	386290	338505	3759842	29543	11·107	8·467	4·313
4	377077	316202	3443640	31626	10·891	9·064	4·617
5	370358	297194	3146446	33648	10·587	9·643	4·912
6	365325	280531	2865915	35647	10·216	- - -	5·204
7	361372	265546	2600369	37658	9·792	- - -	5·498
8	358062	251784	2348585	39717	9·328	- - -	5·798
9	355328	239102	2109483	41948	8·849	- - -	6·124
0	353031	227326	1882157	43990	8·280	- - -	6·422
1	351048	216315	1665842	46229	7·701	- - -	6·749
2	349272	205952	1459890	48555	7·088	- - -	-
3	347606	196143	1263747	50983	6·443	- - -	-
4	345969	186814	1076933	53529	5·765	- - -	-
5	344290	177902	899031	56211	5·054	- - -	-
6	342509	169360	729671	59046	4·308	- - -	-
7	340581	161155	568516	62052	3·528	- - -	-
8	338469	153259	415257	65249	2·710	- - -	-
9	336149	145654	269603	68656	1·851	- - -	-
20	333608	188328	181275	72292	0·949	- - -	-
1	330844	181275	000000	-	-	- - -	-

## FATHERS AND SONS.

s	x	$l_x$	$D_{x's}$	$N_{x's}$	$D_{x's}^{-1}$	$a_{x's}$	Deferred	
							till 6.	till 12.
0	4	67780	346861	2628740	28830	7·579	3·975	1·830
1	5	66081	270459	2358281	36974	8·720	5·097	2·347
2	6	64317	235885	2122396	42393	8·997	5·844	2·691
3	7	62640	2120389	1910357	47163	9·010	6·502	2·994
4	8	61001	192887	1717470	51846	8·904	7·148	3·292
5	9	59399	176530	1540940	56648	8·728	7·810	3·596
6	40	57884	1622443	1378697	61637	8·498	- - -	3·913
7	1	56306	149519	1229178	66881	8·221	- - -	4·246
8	2	54815	138015	1091163	72453	7·906	- - -	4·600
9	3	53359	127582	963581	78616	7·575	- - -	4·991
10	4	51936	118064	845514	84703	7·162	- - -	5·378
1	5	50545	109337	736177	91458	6·733	- - -	5·806
2	6	49184	101295	634882	98717	6·267	- - -	-
3	7	47852	93858	541024	10654	5·764	- - -	-
4	8	46556	86973	454051	11498	5·221	- - -	-
5	9	45303	80595	373456	12408	4·634	- - -	-
6	50	44099	74686	298770	13389	4·000	- - -	-
7	1	42949	69214	229556	14448	3·317	- - -	-
8	2	41857	64150	165406	15588	2·578	- - -	-
9	3	40809	59440	105966	16824	1·783	- - -	-
20	4	39791	55042	50924	18168	0·925	- - -	-
1	5	38792	50924	00000	-	-	- - -	-

## SONS. REVERSIONARY ANNUITIES.

Commencing on Decease of the Father, and continuing till the Age of 21.

s	till 21.	Deferred till 6.	Deferred till 12.		
				0	1·947
				1·947	1·625
				2·181	1·900
				2·178	1·970
				2·097	1·965
				1·987	1·916
				1·859	1·833
				1·718	- - -
				1·571	- - -
				1·423	- - -
				1·274	- - -
				1·118	- - -
				0·968	- - -
				0·821	- - -
				0·679	- - -
				0·544	- - -
				0·420	- - -
				0·308	- - -
				0·211	- - -
				0·132	- - -
				0·068	- - -
				0·024	- - -

**COMPUTATION OF THE PAYMENTS**

**TO BE REQUIRED ON**

**MARRIAGE AND PROMOTION, AND FOR CHILDREN.**

**COMPUTATION of the requisite DONATIONS on MARRIAGE and on subsequent PROMOTION to each RANK.**

Ranks.	Present Ages.		Advanced Ages.		Present Ages. $D_{x'y}^{-1}$	Advanced Ages. $D_{(x'y)+n}$	Advanced Ages. $a_{(x'y)+n}$	Half Product of the Three preceding Columns.	Present Ages. $a_{x'y}$	Differences of the Two preceding Columns.	Present Ages. $a_{x'y}^{\frac{1}{2}}$
	H.	W.	H.	W.							
Lieutenant - - -	25	20	49	44	13330	98560	9.233	0.606	11.767	11.161	3.752
Captain - - -	30	24	49	43	18687	105247	9.315	0.916	11.379	10.463	3.902
Major - - -	38	31	49	42	33929	112266	9.389	1.788	10.659	8.871	3.928
Lieut.-Colonel - - -	44	36	49	41	53511	119703	9.458	3.029	10.086	7.057	3.880
Colonel - - -	49	39	49	39	73701	135684	9.600	4.800	9.600	4.800	3.932

Ranks.	Yearly Subscriptions.		Pensions.			
	Of each Rank.	Increase in each Rank.	Of each Rank.	Increase in each Rank.	The same exchanged.	
	Rs.	Rs.	£	£	Rs.	Rs.
Lieutenant - - -	120	0	40		417.39	
Captain - - -	240	120	70	30	730.43	313.04
Major - - -	360	120	100	30	1043.48	313.04
Lieut.-Colonel - - -	480	120	130	30	1356.52	313.04
Colonel - - -	600	120	160	30	1669.57	313.04

Ranks.	Present Values of the				Differences, being the requisite Donations.	
	Yearly Subscriptions.	Increase in each Rank.	Pensions.	Increase.	On Marriage.	On Promotion.
	Rs.	Rs.	Rs.	Rs.	Rs.	Rs.
Lieutenant - - -	1339.32		1566.05		236.73	
Captain - - -	2511.12	1255.56	2850.14	1221.51	339.02	
Major - - -	3193.56	1064.52	4098.79	1229.64	905.23	165.12
Lieut.-Colonel - - -	3387.36	846.84	5263.81	1214.61	1875.95	367.77
Colonel - - -	2880.00	578.00	6564.79	1231.83	3684.79	655.83

## COMPUTATION of the MARRIAGE DONATIONS for DISPARITY of AGES.

Difference of Ages.	Age of Husband.	$\alpha_{x-y}$ Half Rates after Age 49.	Rank and Rates and Values of Subscription.					$\alpha_{x-y}^2$ Exchanged into Rupees.	Rank, and Amounts and Values of Pensions.					
			Lieut. Rs. 120.	Captain. Rs. 240.	Major. Rs. 360.	Lt.-Col. Rs. 480.	Colonel. Rs. 600.		Lieut. £40.	Captain. £70.	Major. £100.	Lt.-Col. £130.	Colonel. £160.	
15	{ 80 35 40 45 50 55 60	10·748 9·875 8·662 6·848 4·885 4·415 3·839	1290 1185 1039 822 586 530 461	2580 2370 2079 1644 1759 1589 921	3869 3555 3118 2465 2345 2119 1382	5159 5225 5197 5109 2931 2649 1843	6449 5276 43·910 44·744 46·437 51·443	39·663 42·198 43·910 44·744 46·437 51·443	1587 1688 1756 1790 1857 2058	2776 2954 3074 3132 3251 3601	3966 4220 4391 4474 4644 5144	5156 5486 5708 5817 6037 6688	6346 6752 7026 7159 7430 8231	
		9·985 8·794 7·062 5·024 4·546 3·950	1198 1055 847 603 546 474	2396 2111 1695 1206 1091 948	3595 3166 2542 1809 1637 1422	4793 4221 3890 3014 2182 1896	5991 5276 4237 3014 2728 2370	41·301 44·243 45·779 51·214 52·769 57·725	1652 1770 1871 1892 2111 2309	2891 3097 3275 3424 3694 4041	4130 4424 4678 4892 5277 5773	5369 5752 6081 6359 6860 7504	6608 7079 7485 7827 8443 9236	
		8·885 7·170 5·156 4·660 4·051	1066 860 619 559 486	2132 1721 1237 1118 972	3199 2581 1856 1678 1458	4265 3442 2475 2237 1944	5331 4302 3094 2796 2431	43·450 47·301 51·214 56·390 63·099	1738 1892 2049 2256 2524	3042 3311 3585 3947 4417	4345 4730 5121 5639 6310	5649 6149 6658 7381 8203	6952 7568 8194 9022 10096	
		7·194 5·246 4·769 4·138	863 630 572 497	1727 1259 1145 993	2590 1889 1717 1490	3453 2518 2289 1986	4316 3148 2861 2483	46·529 51·777 58·602 66·553	1861 2071 2344 2662	3257 3624 4102 4659	4653 5178 5860 6655	6049 6731 7618 8652	7445 8284 9376 10648	
		45	1086	1101	1409	1428								
		50	1180	1218	1551	1601								

Note.—The differences of the corresponding values show the requisite marriage donations. For example, at age 50 the donation of a colonel for a disparity of 20 years is 7827 - 3014 = Rs. 4813, which amount is entered in the scale. The intermediate values have been interpolated.

## SCALE of MARRIAGE DONATIONS. Increased for Disparity of Age.

Age.	Captains.		Majors.		Lieut.-Colonels.			Colonels.				
	15.	20.	15.	20.	15.	20.	25.	15.	20.	25.	30.	
34	533											
35	600											
36	671	543										
37	746	651										
38	825	761										
39	908	872	1143	1091								
40	995	986	1273	1258								
41	1086	1101	1409	1428								
42	1180	1218	1551	1601								
43	1279	1337	1698	1777	2110							
44	1382	1458	1850	1995	2305	2377						
45	1488	1580	2009	2136	2530	2691	2707					
46	-	-	2173	2320	2824	2984	3047					
47	-	-	2343	2507	3087	3256	3365					
48	-	-	2518	2696	3320	3508	3660					
49	-	-	-	-	3521	3737	3933					
50	-	-	-	-	3692	3947	4183	4499	4813	5100	5136	
51	-	-	-	-	3832	4135	4410	4559	4973	5300	5390	
52	-	-	-	-	3941	4302	4615	4638	5144	5513	5655	
53	-	-	-	-	-	-	-	4735	5324	5738	5931	
54	-	-	-	-	-	-	-	4850	5515	5976	6218	
55	-	-	-	-	-	-	-	4984	5715	6226	6515	
56	-	-	-	-	-	-	-	5136	5925	6489	6823	
57	-	-	-	-	-	-	-	5307	6146	6764	7142	
58	-	-	-	-	-	-	-	5495	6376	7052	7472	
59	-	-	-	-	-	-	-	5702	6616	7352	7813	
60	-	-	-	-	-	-	-	5928	6866	7665	8165	

Example. A captain aged 37 marries a lady aged 22. The difference of age is 15. The marriage donation is Rs. 746, to be paid instead of the ordinary donation.

In like manner, a colonel aged 54 marries a lady aged 29. The difference of age is 25, and the corresponding marriage donation is Rs. 5976.

It will be observed that the amounts depend much more on the age of the husband than on that of the wife, a circumstance which, in the present case, is caused by the re-marriage of young widows being an element in the calculation. It follows that the table will serve for all cases, nearly enough.

## COMPUTATION of the FAMILY CONTRIBUTION for SONS.

Son's Age.	Reversionary Pensions.			
	Deferred			
	Immediate.		Deferred	
			till 6.	till 12.
0 to 1	2.064		1.762	1.120

Sum of the above values - 4.946.

$$4.946 \times 10 = £49.46 = \text{Rs. } 516.1$$

Deduct birth donation - 156.0

Balance - - 360.1

The value of the joint life annuity till age 21 is - 8.608.

$$\text{Hence } \frac{360.1}{8.608 \times 12} = \text{Rs. } 3.500 \text{ monthly.}$$

Deduct the rate in aid 2.500 " (See Report, Art. 20.)

Balance family contribution - Rs. 1.000 "

## COMPUTATION of the FAMILY CONTRIBUTION for DAUGHTERS.

Daughter's Age.	Reversionary Pensions.			
	Deferred.			
	Immediate.		Deferred.	
			till 6.	till 12.
0 to 1	2.883		2.575	1.919
Add for £5 after the age of 21		-	-	-
				0.919
				0.460
				1.379

Sum of the values - 8.756.

$$8.756 \times 10 = £87.56 = \text{Rs. } 913.67$$

Deduct birth donation - 250.

663.67

The value of the joint life annuity is - 9.135.

$$\text{Hence } \frac{663.67}{9.135 \times 12} = \text{Rs. } 6.054 \text{ monthly.}$$

Deduct the rate in aid 3.500 " (See Report, Art. 20.)

Balance family contribution - Rs. 2.554 "

In accordance with the results herein set forth, the family contributions have been assigned as follows :—  
(See Report, Art. 22.)

Donation on Birth. Monthly Subscription.

	Rs.	R.	A.	P.
For Sons -	156	1	0	0
For Daughters -	250	2	8	0

F O R M S

FOR THE

REGISTRY OF MARRIAGES, BIRTHS, AND DEATHS.

M

FORM of Register for Officers.

No.	Names.	MEMBERS.					WIVES.		CHILDREN.										Reference to the Page or Folio of the Children's Register.					
		Present Rank.					Dates of					Dates of		This is to be filled up by merely inserting under the proper number the letter <i>m</i> or <i>f</i> , to denote the sex of the child.										
		Lieutenant.	Captain.	Major.	Lieut.-Colonel.	Colonel.	Entry.	Birth.	Marriage.	Death.	Exit by any other Cause.	Birth.	Death.	1	2	3	4	5	6	7	8	9	10	
39	Anderson, John F.	-	-	-	-	-	71·353	46·238	76·441	87·682	-	53·523	-	m	f	f	m							12

NOTE.—The above entries indicate that the officer named, whose reference number is A 39, entered as a Lieutenant on the 10th May 1871, that he was born on the 29th March 1846, was married on the 11th June 1876, and died, being then a Captain, on the 7th September 1887, leaving a widow and three children him surviving; a fourth child having died in the father's lifetime. For the purposes of any intermediate valuation it would have appeared that this officer was seven years older than his wife; his then present rank, and the number of his children would have also been obtained.

The dates are most briefly and conveniently entered as *decimals of the year*, for which end a table is annexed.

FORM of Register for Children and Widows.

12	Names.	Reference.	Dates of				Remarks.
			Birth.	Marriage.	Death.	Exit.	
	Anderson, John F. - - - -	A. 39.			87·682		
	Children.						
	" John - - - -		78·510				
	" Anne - - - -		80·164				
	" Emily - - - -		81·677				
	" Edward - - - -		83·786		84·033		
	Widow.						
	" Matilda - - - -		53·523				Pension £70.

NOTE.—On the marriage of an officer, his name and the reference number should be entered in this Register, and the dates of births of children, and of any casualties be recorded as they occur. On his decease, the date of that event should be entered, as indicating the time at which the children became wards. The christian name and birth date of the widow should be entered at the close, and any further events respecting her will have place in this Register. Any particulars, other than dates, may be entered in the column of Remarks.

DATES expressed in Decimals of the Year.

Day of the Month.	Jan.	Feb.	March.	April.	May.	June.	July.	August.	Sept.	Oct.	Nov.	Dec.	Day of the Month.
1	.000	.085	.162	.247	.329	.414	.496	.581	.666	.748	.833	.915	1
2	.003	.088	.164	.249	.332	.416	.499	.584	.668	.751	.836	.918	2
3	.005	.090	.167	.252	.334	.419	.501	.586	.671	.753	.838	.921	3
4	.008	.093	.170	.255	.337	.422	.504	.589	.674	.756	.841	.923	4
5	.011	.096	.173	.258	.340	.425	.507	.592	.677	.759	.844	.926	5
6	.014	.099	.175	.260	.342	.427	.510	.595	.679	.762	.847	.929	6
7	.016	.101	.178	.263	.345	.430	.512	.597	.682	.764	.849	.932	7
8	.019	.104	.181	.266	.348	.433	.515	.600	.685	.767	.852	.934	8
9	.022	.107	.184	.268	.351	.436	.518	.603	.688	.770	.855	.937	9
10	.025	.110	.186	.271	.353	.438	.521	.605	.690	.773	.858	.940	10
11	.027	.112	.189	.274	.356	.441	.523	.608	.693	.775	.860	.942	11
12	.030	.115	.192	.277	.359	.444	.526	.611	.696	.778	.863	.945	12
13	.033	.118	.195	.279	.362	.447	.529	.614	.699	.781	.866	.948	13
14	.036	.121	.197	.282	.364	.449	.532	.616	.701	.784	.868	.951	14
15	.038	.123	.200	.285	.367	.452	.534	.619	.704	.786	.871	.953	15
16	.041	.126	.203	.288	.370	.455	.537	.622	.707	.789	.874	.956	16
17	.044	.129	.205	.290	.373	.458	.540	.625	.710	.792	.877	.959	17
18	.047	.132	.208	.293	.375	.460	.542	.627	.712	.795	.879	.962	18
19	.049	.134	.211	.296	.378	.463	.545	.630	.715	.797	.882	.964	19
20	.052	.137	.214	.299	.381	.466	.548	.633	.718	.800	.885	.967	20
21	.055	.140	.216	.301	.384	.468	.551	.636	.721	.803	.888	.970	21
22	.058	.142	.219	.304	.386	.471	.553	.638	.723	.805	.890	.973	22
23	.060	.145	.222	.307	.389	.474	.556	.641	.726	.808	.893	.975	23
24	.063	.148	.225	.310	.392	.477	.559	.644	.729	.811	.896	.978	24
25	.066	.151	.227	.312	.395	.479	.562	.647	.732	.814	.899	.981	25
26	.068	.153	.230	.315	.397	.482	.564	.649	.734	.816	.901	.984	26
27	.071	.156	.233	.318	.400	.485	.567	.652	.737	.819	.904	.986	27
28	.074	.159	.236	.321	.403	.488	.570	.655	.740	.822	.907	.989	28
29	.077		.238	.323	.405	.490	.573	.658	.742	.825	.910	.992	29
30	.079		.241	.326	.408	.493	.575	.660	.745	.827	.912	.995	30
31	.082		.244		.411		.578	.663		.830		.997	31

Example.—The decimal part of the year corresponding to the 22d June is .471.

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R E P O R T  
ON THE  
FOREGOING CALCULATIONS,

BY

SAMUEL BROWN, F.S.S.,  
ACTUARY OF THE GUARDIAN ASSURANCE COMPANY, AND LATE PRESIDENT OF THE  
INSTITUTE OF ACTUARIES.

To the Under Secretary of State for India, India Office, S.W.

Guardian Assurance Office,  
11, Lombard Street, E.C.,  
25th February 1871.

Sir,

Para. 1. In accordance with the instructions which I received in Letter No. 3529, dated 6th September 1870, I have carefully examined Major-General Hannyngton's report on the scheme for granting pensions to the widows and orphans of Officers entering the Staff Corps, and of Chaplains and Medical Officers on the Indian Establishment.

2. In my previous Reports on the Indian Military Funds for widows and orphans, I have had occasion to follow General Hannyngton's calculations and methods of dealing with the complicated contingencies which, in such Funds, present themselves in what appears, at first sight, simple questions. I can fully appreciate the ability and scientific skill with which he treats these subjects, and the caution and prudence with which he meets those doubtful points which may affect the future safety or prosperity of the Fund.

3. The object of Colonel Norman's proposition appears to be, by taking the leading features of the former Military Pension Funds, to make some additions to the benefits granted to widows and orphans of Officers in the British Army, bringing up the scale to what was formerly the average rate in the three Presidencies, and requiring from the members such contributions as would make the Fund self-supporting, without causing any additional charge on the Government.

4. As it is not proposed to have different rates, as formerly, for each Presidency, it is of great importance that we should be able to form some clear idea of what would be safe data for the computations of the benefits and the equivalent contributions applicable to the whole of India.

5. General Hannyngton judiciously points out that the bases of his tables must be the rates of mortality amongst military Officers in India, their wives, widows, sons, and daughters; the rates of marriage among widows and unmarried daughters; the rate of interest and the rate of exchange.

6. The two last points have been settled by the letter of the 23d April 1869, from the Military Secretary, authorizing the rate of interest to be taken at  $4\frac{1}{2}$  per cent., and the rate of exchange at 1s. 11d. the rupee.

7. I should have been inclined to propose that the rupee should be taken = 2s., as having been offered in the settlement of some of the existing Pension Funds now winding up, and as being nearer the average of exchange of late years. The facilities in the accounts and computations would have been very great. The Exchange Table, however, given in p. 31, contains in small compass the ready means of computing when the exchange is 1s. 11d. the rupee, and it is essential to the scheme as agreed on.

8. One of the most important questions is the tables of mortality, on which the calculations are made, especially that of subscribers and their wives whilst resident in India.

9. The table for the former, adopted by General Hannyngton is taken from Mr. Neison's report on the Bengal Military Fund, 1849, Table XI. The data for this table were collected from the records of the India Office, and include observations on mortality amongst Officers after they had retired from the service.

10. This table, it must be admitted, is a very important one, but in the twenty years which have since elapsed other observations of considerable value have been gathered, and are now available for use or comparison.

11. In my Report of 31st January 1863, on the Madras Military Fund, will be found the complete experience of the Fund collected for 50 years, 1808 to 1858, and the summaries of the tables, as still further corrected in the course of the investigation, may be examined in the "Journal of the Institute of Actuaries," Vol. XI., pp. 139, &c.

12. These observations throw light, not merely on the differences in the rate of mortality amongst married and unmarried Indian Officers, whether on active

Report on General Hannyngton's calculations as to the scheme for granting pensions to the widows and orphans of Officers entering the Staff Corps, and of Chaplains and Medical Officers on the Indian establishment.

Objects of the Scheme.

Basis of the Tables.

Rate of interest.  
Rate of exchange.

Mortality of Indian military Officers.

service or retired, but amongst their wives and sons and daughters, as well as the rates of marriage amongst their widows and daughters. They show, also, the marked improvement in the rate of mortality in India in recent years, as compared with the earlier periods of the present century.

13. The total number of lives accounted for was 5,104 (of whom 117 had entered as married). Of the total number, 2,400 had died, 473 withdrew, and 2,231 were living at the close of the observations.

14. In my Report on the Bengal Military Fund, of 16th March 1869, further observations are given, as deduced from the experience of the Bombay Military Fund in an investigation of that Fund then proceeding. The totals have been combined with those of the Madras Military Fund, and the rates per cent. of death, withdrawal, retirement, and marriage computed and shown in Abstract H, p. 43. The numbers were, 3,332 who entered as bachelors, besides 257 who entered as married, total 3,589. Of these, 1,501 died, 431 withdrew, 211 had retired as bachelors, and were not further traced, and 1,446 were living on 31st December 1865.

15. The more detailed observations on the Bombay Military Fund from 1816 to 31st December 1865, in my Report on that Fund in the present year, may be compared with Mr. Davies's data from the same Fund from 1825 to 1849. The effect of the addition of 15 recent years of observation is to show clearly in the middle periods of life a still-diminishing rate of mortality at the same ages.

16. It was hoped that the experience of the Bengal Military Fund would have enabled the observations to be continued from 1849 to the present time. But the documents only allowed of comparisons at the average ages in the different ranks, and not of grouping the facts in quinquennial or decennial periods of age.

17. But if we add to the above recent observations in Madras and Bombay, the facts for the Bengal Army up to 1847, from Mr. Neison's Table XI., it will probably afford in the combination the best general Table of Mortality for all India which has ever yet been obtained.

18. The number of Officers who entered from 1800 to 1847, by Mr. Neison's Table XI., were 5,199. Of these, 2,019 died, 75 discontinued, and 3,105 were living at the close of the observations.

19. By taking for the number exposed to risk the number living in the middle of any year of age, the following Table shows the effect of bringing together these three Tables and the mortality per cent. resulting therefrom.

TABLE A.

OBSERVATIONS of Mortality amongst Indian Military Officers, deduced from the combined experience of the Bengal, Madras, and Bombay Military Funds.

Ages.	Exposed to Risk.	Died.	Mortality per Cent.		
			By Ditto.	Hannyngton.	
15 and under 20	18038	271	1·50	1·20	
20 " 25	49883·5	1342	2·69	2·22	
25 " 30	42612	1181	2·77	2·37	
30 " 35	33303	956	2·87	2·65	
35 " 40	24956	706	2·83	2·67	
40 " 45	17488·5	504	2·88	2·58	
45 " 50	11805·5	361	3·06	2·97	
50 " 55	8221·5	211	2·57	3·25	
55 " 60	5180·5	151	2·92	2·57	
60 " 65	2521·5	92	3·65	3·08	
65 " 70	1180	68	5·76	1·53	
70 " 75	531·5	39	7·34		
75 " 80	200	27	13·50		
80 " 85	64	8	12·50		
85 " 90	11·5	3	26·09		
	215997	5920	2·76		

20. From the large number of lives exposed to risk, 215,997, and deaths, 5,920; and also from the fact that the observations in the three Presidencies are combined, showing the rates of mortality at quinquennial periods of age, this Table is the most complete and authentic which has yet been obtained, and may be safely used as a basis, if any correction of the monetary tables should be required hereafter.

21. It indicates at most ages, and particularly the younger ages, a somewhat higher rate of mortality than that selected by General Hannington; but inasmuch as all observations show that there is a marked difference of mortality in favour of married life, and the risks under the proposed new scheme almost entirely depend on that class, I feel confident that the table on which his calculations are based may be safely and judiciously adopted.

22. It would be very desirable, however, to carry out the proposed registers for the collection of original data from the experience of the New Fund, both for the sake of checking or confirming the accuracy of the above Table, as well as to fill up the deficiencies which we find in the other tables required.

23. The mortality amongst the wives of Officers is a subject on which more Mortality of the information is much desired. wives of Officers.

24. General Hannington has used the table of mortality deduced by Mr. Davies from the records of the Madras Military Fund, and somewhat modified for use in the Bengal Military Fund.

25. It must be admitted, that the larger collection of facts which I made from the records of the Madras Military Fund presents results which in the middle and older periods of life seem to indicate a too favourable rate of mortality and require cautious use.

26. Most of the observations as to mortality amongst adult female European lives in India are liable to the objection, that in former days their ages were not accurately recorded till they became widows, and thus the effect of climate during the earlier years of married female life has not been accurately ascertained. Amongst widows the observations at the younger ages are comparatively few. But it is probable on the one hand, that the younger widows do not generally return immediately to Europe; and on the other hand, after the middle periods of life, the retirement of the husbands would lead to the greater portion of married females or widows after these ages being no longer exposed to the risks of a tropical climate.

27. I am disposed to think, therefore, that by combining the observations for female lives, whether wives or widows, both in the Military and Civil Funds, a sufficient number of facts may be obtained to give confidence in the comparison, except as to the middle periods of life, ages 45 to 60, when from some cause or other the per-cent-age of mortality shown is so small as to be scarcely admissible without further evidence.

28. The following Tables comprise all the recent collection of facts.

		Exposed to Risk.	Died.	Married.	
Madras Military Fund :					
1808 to 1807 -	Wives -	22274·5	300		
(S. Brown.)	Widows	8273·5	140	145	
Bengal Military Fund :					
1800 to 1847 -	Widows	6094·5	92	119	
(Neison.)					
Bengal Civil Fund :					
1850 to 1862 -	Wives -	4135	54		
(S. Brown.)	Widows	1170	18	8	
Total (Wives and Widows)		41947·5	604		
" (Widows only)		15538	250	272	

29. The observations in quinquennial periods of age, and the rates per cent. of mortality and marriage, computed on 100 living in the middle of the year, by these combined Tables, may be compared as follows with the Table deduced by Mr. Davies, slightly corrected by him at the younger ages for the Bengal Military Fund, which General Hannyngton has used.

TABLE B.

Rates of Mortality amongst the Wives and Widows, and Rates of Marriage amongst the Widows of Indian Military Officers and Civil Servants.

Wives and Widows.				Widows only.			Hannyngton.		
Ages.	Exposed to Risk.	Died.	Mortality per Cent.	Exposed to Risk.	Married.	Married per Cent.	Wives.	Widows.	
							Mortality per Cent.	Mortality per Cent.	Married per Cent.
15-20	1011·5	19	1·88	61·5	7	11·38	·61	·79	6·85
20-25	5198·5	85	1·64	551	41	7·44	·82	·88	5·50
25-30	7329	93	1·27	1354	67	4·95	1·11	·97	3·51
30-35	7199·5	93	1·29	2006	67	3·34	1·45	1·07	3·05
35-40	6246·5	82	1·31	2386	36	1·51	1·68	1·15	1·88
40-45	4951	56	1·13	2421	19	·78	2·03	1·23	·88
45-50	3680	42	1·14	2064·5	18	·87	2·42	1·37	·79
50-55	2562	37	1·44	1645	10	·61	2·92	1·62	1·32
55-60	1746·5	24	1·37	1315	6	·46	3·42	2·10	·79
60-65	1067	34	3·19	881	1	·11	4·12	2·80	
65-70	570·5	16	2·80	493·5	—	—	5·19	4·07	
70-75	253	11	4·35	230·5	—	—	7·24	6·02	
75-80	91	4	4·40	87·5	—	—	10·30	9·10	
80-85	39·5	6	15·19	39·5	—	—	15·70	13·59	
85-90	2	2	100	2	—	—	23·83	19·71	
	41947·5	604	1·44	15538	272	1·75			

30. The table of mortality which General Hannyngton has used for wives is the same, after age 27, as Mr. Davies gives in his report on the Madras Military Fund, dated June 1839, but which he afterwards corrected by making the deaths an equal number at each of the ages 13 to 27. But it will be found, by Appendix 20 (Mr. Davies), that it was deduced from only 21 deaths of daughters and 41 deaths of widows of members of the Fund, and that of the latter only 11 had the ages at death recorded, so that it would evidently be desirable to continue to collect the facts, since the recent experience with the larger numbers shows a much lighter mortality amongst female lives returned from India than has generally been supposed.

31. As Mr. Davies' Table, however, does not begin to show the excess of mortality to any great extent until after the age of 40, at which age the widows, whose pensions are valued by a different table, begin to bear a larger proportion to the wives, I am not prepared to recommend that General Hannyngton's Joint Life Tables of Husband and Wife should be recomputed until some better observations shall have been collected, by which the tables may be corrected.

Mortality amongst children of Indian Officers.

32. In regard to the mortality under 20 years of age of sons and daughters of Officers, there have been considerable additions to the facts of late years, and the observations on the mortality and rate of marriage of daughters after that age have also been extended. General Hannyngton has himself given the data which were furnished to Mr. Griffith Davies and Mr. Peter Hardy in 1852, from the Register of the Bengal Military Fund up to 1850, and if these be combined with those contained in my Report for the Madras Military Fund and in some of the Reports of the Civil Funds, they may fairly be made the basis of comparison for the mortality amongst children born of European parents in India.

33. They will then comprise the following numbers for the mortality of sons and daughters under 20 years of age:—

	Sons.		Daughters.	
	Exposed to Risk.	Died.	Exposed to Risk.	Died.
Madras Military Fund, 1808 to 1857 - - -	26770·5	445	25364	434
" Annuitants, 1808 to 1857 - - -	5829	42	5778·5	35
Bengal Military Fund, - - - to 1850	10887	393	10320·5	370
" Civil Fund, 1850 to 1863 - - -	7588·5	102	6644·5	84
Madras Medical Fund, 1824 to 1855 - - -	5323·5	66	4603·5	71
	56398·5	1048	52711	994

34. The combination of these tables affords sufficient materials for trustworthy results under age 20, except, perhaps, for the first year of life, when, from the very light mortality which is observable, it is probable that some of the deaths which take place soon after birth have escaped registration.

35. General Hannyngton has adopted Dr. Farr's English Life Table No. 3, which includes the deaths for 17 years, 1838 to 1854, compared with the living at the two censuses in 1841 and 1851, and the following comparison of the above Indian tables may be made with it:—

TABLE C.

MORTALITY amongst Children born of European Parents in India.

Age.	Males.		Females.		Indian Table.		Hannyngton, Farr No. 3. Annual Mortality per Cent. at Mean Age.	
	Exposed to Risk.	Died.	Exposed to Risk.	Died.	Male.	Female.	Male.	Female.
0	3552	306	3404	261	8·62	7·67	18·33	14·75
1	4781	346	4526	306	7·24	6·76	6·68	6·44
2	4292	136	4071	150	3·17	3·68	3·62	3·60
3	4011	64	3740·5	70	1·60	1·87	2·42	2·45
4	3778·5	30	3495	40	·79	1·14	1·80	1·79
0·5	20414·5	882	19236·5	827	4·32	4·30	6·57	5·80
5·10	16024·5	82	14926·5	87	·51	·58	·92	·91
10·15	12107·	39	11112·5	39	·32	·35	·48	·51
15·20	7852·5	45	7435·5	41	·57	·55	·62	·66
—	56398·5	1048	52711	994	—	—	—	—

36. It will thus be seen that Farr's English Life Table No. 3, exhibits a much higher rate of mortality in the first year of life and generally in and after the third year, indicating that a smaller number would survive to obtain the benefits than according to the Indian rates. I think, therefore, it would be prudent to collect further observations to check the above tables, and, if found necessary, the contributions for the contingent benefits to children might be modified hereafter.

37. Assuming that the mortality of daughters, after the age of 20, may be fairly represented by the English Life Table No. 3, the only remaining point is their rate of marriage.

38. In the proportions given for 1851 in England, in the Registrar General's 14th Report, the rates of marriage amongst spinsters are much lower at all ages than amongst widows, and, being computed on 140,331 marriages of spinsters and 13,875 marriages of widows, may be supposed to fairly exhibit the ratios in the general population of this country. The rates amongst spinsters in 1851 are also confirmed by recent observations of a similar kind in 1868.

39. But General Hannyngham has prudently thought that allowance should be made for what, in this case, must be considered a special class, and has accordingly formed a table by reducing the full English rates by one-fifth, a course in which he is strengthened by the opinion of Dr. Farr.

40. By collecting my own observations for the Indian services a few more facts have been put together, which show that at the younger marriageable ages the daughters of Indian Officers marry in rather higher proportions than their widows do, but at the subsequent ages less. They are principally derived from the Madras tables, but include also the Bengal Civil Fund.

TABLE E.  
Proportion of Marriages amongst Spinsters.

Age.	Daughters of Indian Officers.			England, 1851, less one-fifth.	England.	
	At Risk.	Married.	Per Cent.		1851.	1868.
15-20	6675·	209	3·13	1·74	2·18	2·70
20-25	2966·	238	8·02	10·14	12·67	13·20
25-30	1267·	69	5·45	7·60	9·50	9·77
30-35	679·5	19	2·80	4·82	6·03	5·76
35-40	373·	3	·80	3·02	3·78	4·01
40-45	99·5	2	1·00	2·00	2·50	2·93
45-50	93·5	—	—	1·14	1·42	2·09
50-55	39·	—	—	·48	·60	1·26
55-60	19·	—	—	·25	·31	·72
60-65	7·	—	—	·07	·09	·35
	12318·5	540				

41. Even the reduced table of General Hannyngham still considerably exceeds the rates of marriage by actual observations amongst the daughters of Indian Officers. As, however, they are combined with the rates of mortality amongst the same class, and affect mostly the earlier periods of the marriageable ages, they will probably be safe enough for practical use.

42. On the whole, I come to the conclusion that the bases of the various tables which General Hannyngham has taken have been selected with great care and judgment, and that they will only require that the registers which he suggests should be kept with accuracy and the results compared from time to time, so that any alteration which may be necessary in the subscriptions or benefits may be effected on good authority. They are, as far as our experience extends at present, sufficient to preserve the Fund financially in a sound condition and render it free from the need of any extraneous aid.

43. As to the other questions discussed, the amount of the pensions to be paid to widows and children, the amount of donations on promotion and marriage, the increase of the subscriptions on promotion, and their reduction after retirement, the corresponding contributions appear to have been very judiciously and carefully computed by General Hannyngham so as to place the new benefits proposed, when added to the scale of pensions in the British Army, in accordance with the average of the total benefits which have hitherto been found sufficient and convenient in the Indian Pension Funds.

44. I also agree in the view which General Hannyngham takes as to the proportion of the rate in aid which may be expected from the unmarried members, and their effect upon the family contributions for sons and daughters, as shown in p. 82.

45. I have carefully examined the methods adopted, and tables given, for computing the various benefits, and need only say that General Hannyngham has shown the greatest mathematical skill in simplifying the processes and arriving at accurate results.

46. On the whole, I beg to report that in my judgment the scheme has been well devised, and with the collection of facts from the actual experience of the

Funds, as recommended by General Hannyneton, to correct, from time to time, some of the data on which at present more precise information is required, I believe it may be worked out with perfect safety to the Government. Reasoning from the success of the Pension Funds, which have been so long tried in the three Presidencies, there is every reason to think that it will prove the greatest boon and advantage to the families of Military Officers in India.

I have the honour to be,  
Sir,  
Your most obedient Servant,  
(Signed) SAMUEL BROWN, Actuary.

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