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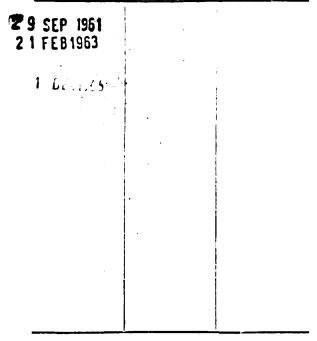
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Quality

of
Manufactured Product

By

W. A. SHEWHART, Ph.D.

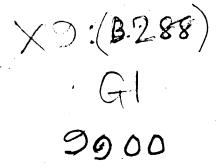
Member of the Technical Staff
BELL TELEPHONE LABORATORIES, INC.

MACMILLAN AND CO., LIMITED ST. MARTIN'S STREET, LONDON

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# 9900

"When numbers are large, chance is the best warrant for certainty."

A. S. Eddington,

The Nature of the Physical World

"A situation like this merely means that those details which determine the future in terms of the past may be so deep in the structure that at present we have no immediate experimental knowledge of them and we may for the present be compelled to give a treatment from a statistical point of view based on considerations of probability."

P. W. BRIDGMAN,
The Logic of Modern Physics

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#### **PREFACE**

Broadly speaking, the object of industry is to set up economic ways and means of satisfying human wants and in so doing to reduce everything possible to routines requiring a minimum amount of human effort. Through the use of the scientific method, extended to take account of modern statistical concepts, it has been found possible to set up limits within which the results of routine efforts must lie if they are to be economical. Deviations in the results of a routine process outside such limits indicate that the routine has broken down and will no longer be economical until the cause of trouble is removed.

This book is the natural outgrowth of an investigation started some six years ago to develop a scientific basis for attaining economic control of quality of manufactured product through the establishment of control limits to indicate at every stage in the production process from raw materials to finished product when the quality of product is varying more than is economically desirable. As such, this book constitutes a record of progress and an indication of the direction in which future developments may be expected to take place. To get as quickly as possible a picture of the way control works, the reader may find it desirable, after going through Part I, to consider next the various practical illustrations given in Parts VI and VII and in Appendix I.

The material in this text was originally organized for presentation in one of the Out-of-Hour Courses in Bell Telephone Laboratories. Since then it has undergone revision for use in a course of lectures presented at the request of Stevens Institute of Technology in its Department of Economics of Engineering. Much of the work recorded herein is the result of the cooperative effort of many individuals. To a

considerable extent the experimental data are such as could have been accumulated only in a large industry.

On the theoretical side the author wishes to acknowledge the very helpful and suggestive criticisms of his colleague Dr. T. C. Fry and of Mr. E. C. Molina of the American Telephone and Telegraph Company. On the practical side he owes a great debt to another colleague, Mr. H. F. Dodge.

The task of accumulating and analyzing the large amount of data and of putting the manuscript in final form was borne by Miss Marion B. Cater and Miss Miriam S. Harold, assisted by Miss Fina E. Giraldi. Mr. F. W. Winters contributed to the development of the theory. The Bureau of Publication of the Laboratories cooperated in preparing the manuscript for publication. To each of these the author is deeply indebted.

The author is particularly indebted to R. L. Jones, Director of Apparatus Development, and to G. D. Edwards, Inspection Engineer, under whose helpful guidance the present basis for economic control of quality of manufactured product has been developed.

W. A. SHEWHART.

BELL TELEPHONE LABORATORIES, INC. New York, N. Y. April, 1931.

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#### APPENDIX I

### RESULTANT EFFECTS OF CONSTANT CAUSE SYSTEMS

#### 1. Introductory Remarks

Our discussion of the problem of establishing the necessary and sufficient conditions for maximum control was based upon the following three assumptions:

- A. The resultant effect X of the operation of the m causes is the sum of the effects of the separate causes.
  - B. The number m of causes is large.
- C. The effect of any one cause is finite and is not greater than the resultant effect of all the others.

It was stated that under these conditions the distribution of resultant effects of a cause system approached normality as the number m of causes was increased indefinitely, at least in the sense that the skewness  $\sqrt{\beta_{1zx}}$  and the flatness  $\beta_{2zx}$  of this distribution approach o and 3 respectively. We shall now consider the basis for this statement in more detail.

To start with it will be found helpful in trying to get an appreciation of the significance of the three limitations to carry through the details of finding the distribution of resultant effects of a few simple systems. For this purpose we shall consider eight such systems characterized as follows:

(a) 
$$\begin{cases} m = 5 \\ x: & \text{o i; o i; o i; o i; o i.} \\ p: & \frac{5}{6} \frac{1}{6}; \frac{5}{6} \frac{1}{6}; \frac{5}{6} \frac{1}{6}; \frac{5}{6} \frac{1}{6}; \frac{5}{6} \frac{1}{6}. \end{cases}$$
(b) 
$$\begin{cases} m = 5 \\ x: & \text{o i; o 2; o 3; o 4; o 5.} \\ p: & \frac{1}{6} \frac{5}{6}; \frac{3}{6} \frac{4}{6}; \frac{3}{6} \frac{3}{6}; \frac{5}{6} \frac{1}{6}. \end{cases}$$

The notation used in describing the cause systems can be made clear by considering only the first one. Here we have a system of m = 5 causes. Each of these five causes may produce an effect of either 0 or 1. For each cause the probability of zero effect is  $\frac{5}{6}$  and that of unit effect is  $\frac{1}{6}$ .

Using this cause system we may illustrate the method of finding the distribution of resultant effects. Obviously the magnitude of this effect may take on values 0, 1, 2, 3, 4, 5. The probability that the resultant effect will be zero is the compound probability of each component cause producing zero effect or  $(\frac{5}{6})^5$ . In a similar way the probabilities of getting a resultant effect equal to 1, 2, 3, 4, or 5 are respectively  $5(\frac{1}{6})(\frac{5}{6})^4$ ,  $10(\frac{1}{6})^2(\frac{5}{6})^3$ ,  $10(\frac{1}{6})^3(\frac{5}{6})^2$ ,  $5(\frac{1}{6})^4(\frac{5}{6})^1$ , and  $(\frac{1}{6})^5$ . In this way we get the following distribution:

Resultant Effect X	0	1	2	3	4	5
Probability	0.401878	0.401878	0.160751	0.032150	0.003215	0.000129

This is shown graphically in Fig. 1-a. The distributions of the resultant effects of the seven other systems are also shown in Fig. 1. What significance do these results have?

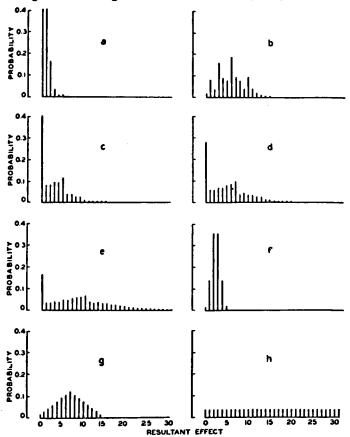


FIG. 1.—DISTRIBUTION OF RESULTANT EFFECTS OF SIMPLE CAUSE SYSTEMS.

In the first case we see that the distribution of resultant effects will always be characterized by the point binomial. Hence it will always monotonically decrease on either side of

the mode—in other words, it is a *smooth* distribution. Distributions b, c, d, and e indicate the effect of lack of uniformity among the component causes. From this viewpoint smoothness is a necessary condition. That it is not, however, a sufficient condition is evidenced by systems f, g, and h.

As long as the component causes are the same, we have already seen (Fig. 53) that the distribution of resultant effects approaches normality as the number of causes is increased. The condition that there shall be an indefinitely large number of causes is, however, certainly not sufficient as is shown by systems g and h, for in these cases the shapes of the distributions will always be those shown in Fig. 1-g and h. Of course, if we admit that the effect of any cause must be finite, systems such as g and h with an indefinitely large number m of causes are ruled out.

#### 2. Practical Significance of Results

In practice one is confronted with an observed distribution and from its nature must often decide whether or not it is worth while looking for assignable causes of either Type I or Type II. We shall concern ourselves here only with the problem of deciding whether or not an observed distribution

1			
1,391	1,318	1,203	1,291
1,416	1,268	1,380	1,273
1,367	1,294	1,349	1,242
1,258	1,368	1,360	1,231
1,289	1,330	1,313	1,320
1,199	1,254	1,351	r,340
1,275	1,226	1,289	1,420

TABLE I.—THERMAL UNITS PER CU. Ft. OF GAS

gives evidence of the presence of a predominating cause, that is, an assignable cause of Type II.

Let us consider a typical problem. The operation data for a certain gas plant for one month expressed in terms of arbitrary thermal units per cubic foot of gas produced from oil by cracking are those given below in Table 1. The data are tabulated in the order in which they were taken. Ideal operation calls for as high and as nearly constant value as can economically be attained.

The following question was raised by the Director of Research of the large organization interested in these results:

If I understand the methods of statistics correctly, it should be possible to determine from these data whether or not there is a predominating cause of variation, and hence to determine whether or not it should be reasonable to expect that a marked improvement in product can be made by controlling one or at least a few causes of variation. Am I right in this interpretation of the possibilities of statistical methods?

In answer to such a question we can at least say something like the following. If we divide the data into subgroups of four in the order in which they were taken and apply Criterion I of Part VI, we get no evidence of lack of control, as may easily be verified by the reader. Assuming that the quality is controlled, we may now consider the evidence for the presence of a predominating effect. An examination of these data shows that they are more or less uniformly distributed over the range of variation as one might expect with a cause system such as (h). In other words, the observed results are consistent with the hypothesis that a predominating cause was present. Needless to say such evidence is not conclusive: it is suggestive.

#### 3. Analytical Results

and

Let us now find expressions for the skewness  $\sqrt{\beta_{12x}}$  and flatness  $\beta_{22x}$  of the distribution of resultant effects under simplifying assumptions.

If we let  $\mu_i$ , represent the *i*th moment of the effects of the *j*th cause about their expected value, it may be shown 1 that

$$\sigma^{2} = \mu_{2} = \sigma_{1}^{2} + \sigma_{2}^{2} + \ldots + \sigma_{J}^{2} + \ldots + \sigma_{m}^{2},$$

$$\mu_{3} = \mu_{3_{1}} + \mu_{3_{2}} + \ldots + \mu_{3_{J}} + \ldots + \mu_{3_{m}},$$

$$\mu_{4} = \sum_{j=1}^{m} (\mu_{4_{j}} - 3\sigma_{J}^{4}) + 3\mu_{2}^{2},$$

<sup>1</sup> See for example *Elements of Statistics*, by A. L. Bowley, published by P. S. King & Son, Ltd., 1920, pp. 291-292.

where  $\mu_i$  is the *i*th moment of the resultant effect of the *m* causes about the expected value of the resultant effect.

From these results we get

$$\beta_{1_{\Sigma X}} = \frac{\mu_3^2}{\mu_2^3} = \frac{\left(\sum_{j=1}^m \mu_{3j}\right)^2}{\mu_2^3} \tag{1}$$

and

$$\beta_{2_{\Sigma X}} = \frac{\mu_4}{\mu_2^2} = \frac{\sum_{j=1}^{m} (\mu_{4j} - 3\sigma_j^4) + 3\mu_2^2}{\mu_2^2} = \frac{\sum_{j=1}^{m} (\mu_{4j} - 3\sigma_j^4)}{\mu_2^2} + 3. \quad (2)$$

As a simple case let us assume that the distribution of effects of (m-1) of the component causes are the same, at least in respect to their second, third and fourth moments, all of which are assumed to be finite, which we shall denote by  $M_2$ ,  $M_3$ , and  $M_4$ . Let us assume that the remaining cause is predominating in the sense that the corresponding three moments of its effects are  $b_2M_2$ ,  $b_3M_3$ , and  $b_4M_4$ , where  $b_2$ ,  $b_3$ , and  $b_4$  are all positive and greater than unity. Under these conditions, we get

$$\beta_{1_{2X}} = \frac{(m-1+b_3)^2}{(m-1+b_2)^3} \frac{\mathbf{M}_3^2}{\mathbf{M}_2^3}$$

and

$$\beta_{2\Sigma X} = \frac{(m-1+b_4)M_4 - 3(m-1+b_2^2)M_2^2}{(m-1+b_2)^2M_2^2} + 3.$$

Evidently these two expressions approach o and 3 respectively as the number m of causes becomes indefinitely large, assuming that  $b_2$ ,  $b_3$ , and  $b_4$  are finite. In this way we come to see that the skewness and flatness of a distribution of resultant effects will, in general, be approximately 0 and 3 if the number m of causes is *very* large.

### 4. Economic Significance of Control from a Design Viewpoint

In Chapter III of Part I we called attention to the fact that as a result of control we attain maximum benefits from quantity production. Only general statements as to obtaining these benefits were given at that time. In Part III, however, we developed the theoretical basis for control, making it now possible to show specifically how control enables us to attain these benefits. We shall consider here only the simplest kind of examples.

A. Example 1.—Suppose that an assembly is to be made in which two washers are to be used, one brass and the other mica. Assume that it is desirable to maintain as closely as possible a uniform overall thickness of these two washers. This could be done, of course, by selecting the pairs of brass and mica washers to give the desired thickness. Such a process, however, would tend to counterbalance the benefits of quantity production, since the economies rising from assembly processes result from interchangeability of piece-parts.

Table 2 gives the results of measurements of thickness on one hundred tool-made samples each of mica and brass washers to be used in the manner previously indicated in the assembly of an important piece of telephone equipment. The reader may easily satisfy himself that both of these distributions are sufficiently near normal to indicate that each of the piece-parts was controlled, and we shall therefore assume this to be the case. For this size of sample we are perhaps justified in assuming that the observed standard deviations of these two distributions may reasonably be taken as the standard deviations  $\sigma_1$  and  $\sigma_2$  of the objective controlled distributions of mica and brass washers respectively. The theory of the previous section shows that under these conditions the standard deviation of a random assembly of two washers, one of each kind, is

$$\sigma = \sqrt{\sigma_1^2 + \sigma_2^2}.$$

Furthermore, it follows that the distribution of the sum of the thickness in such a random assembly will be normally distributed about a mean value which is the sum of the mean values of the two objective distributions.

Upon this basis, therefore, the design engineer is justified

TABLE 2.—Typical Distribution Requisite for Efficient Design

Thickness of Mica in Inches	Number of Washers	Thickness of Brass in Inches	Number of Washers
0.0088	I	0.0182	ı
0.0089	1	0.0185	I
0.0092	1	0.0186	2
0.0093	1	0.0187	2
0.0094	I	0.0188	2
0.0095	1	0,0190	2
0.0098	2	0.0191	3
0.0099	1	0.0192	3
0.0100	2	0.0193	3
0.0101	5	0.0195	5 6
0.0102	2	0.0196	
0.0103	3	0.0197	5
0.0104	7	0.0198	4
0.0105	5 8	0.0199	ı
0.0106	I	0.0200	3
0.0107	10	0.0201	8
0.0108	10	0.0202	4
0.0109	7	0.0203	5
0.0110	5	0.0204	7
0.0111	3	0.0205	4
0.0112	5 6	0.0206	3
0.0113		0.0207	3 6
0.0114	. <b>6</b> 3	0.0208	1
0.0115	3	0.0210	3
0.0116	3	0.0211	. 1
0.0119	I	0.0212	I
		0.0213	3
		0.0214	2
		0.0215	3
		0.0216	2.
		0.0220	I
		0.0222	I

in predicting that the overall thickness of random assemblies of mica and brass washers will be distributed as shown in Fig. 2. The dots in this figure show how closely the first one hundred assemblies made from manufactured product check the prediction. Furthermore, if the observed average thickness of

each distribution is taken as the expected value of the distribution, the design engineer can easily calculate the percentage of assemblies that will be defective in respect to overall thickness subject to the assumptions that have been made.

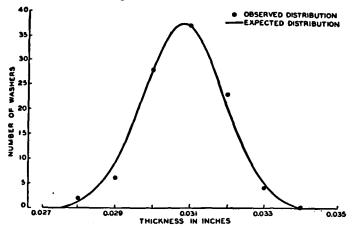


Fig. 2.—Statistical Method Makes Prediction in Design Possible.

B. Example 2.—For a shaft to operate in a bearing it is, of course, necessary to have a certain clearance. Thus, if  $\rho_1$  and  $\rho_2$  represent the radii of the bearing and shaft respectively, then the specification will, in general, state that the difference  $\rho_1 - \rho_2$  must satisfy the inequality

$$d_1 \leq \rho_1 - \rho_2 \leq d_2,$$

where  $d_1$  and  $d_2$  are both positive. This situation is represented schematically in Fig. 3.

In most instances the shaft and bearing are fitted. Sometimes, however, it is of economic importance to be able to product shafts and bearings separately and to assemble these on the job. The question, of course, that is always raised is: What will be the expected rejection of such assemblies because of failure to satisfy the clearance specification?

From the theory of the previous section we see that this question can be answered readily, at least if we assume that radii of bearings and shafts are normally controlled with standard deviations  $\sigma_1$  and  $\sigma_2$  respectively. Under these conditions the difference  $\rho_1 - \rho_2$  between any bearing and shaft chosen at random will be distributed normally about a mean value  $\bar{\rho}_1 - \bar{\rho}_2$  with standard deviation

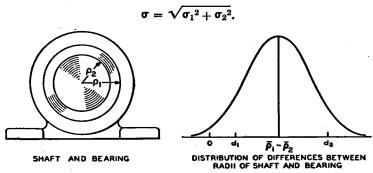


Fig. 3.—How Many Rejections Should We Expect in Assembly?

Hence, the probability of a random assembly being rejected because the clearance fails to come within the required limits is given by

where 
$$z = \frac{(\rho_1 - \rho_2) - (\bar{\rho}_1 - \bar{\rho}_2)}{\sigma}$$

$$z_1 = \frac{d_1 - (\bar{\rho}_1 - \bar{\rho}_2)}{\sigma}$$

$$z_2 = \frac{d_2 - (\bar{\rho}_1 - \bar{\rho}_2)}{\sigma}$$

and the value of the integral can be read directly from Table A.

C. Example 3.—We shall now consider a problem involving maximum control. Many instances arise in production where

materials must be covered with protective coatings. Of such are the various kinds of platings, nickel, chromium, zinc, etc. In other instances we have coatings of paper or lead.

In practically every instance of this kind it is very desirable to maintain a uniform coating that is never less in thickness than some prescribed value. It is obviously desirable from the viewpoint of saving to reduce the variability to a minimum. Table 3 gives an observed distribution of one such kind of

TABLE 3DO THE	VARIATIONS IN	THICKNESS	INDICATE A	Possible Saving?
---------------	---------------	-----------	------------	------------------

Thickness in Inches	Number of Observations	Thickness in Inches	Number of Observations
0.125	2	0.131	20
0.126	12	0.132	5
0.127	21	0.133	3
0.128	18	0.134	0
0.129	33	0.135	3
0.130	33		1

coating supposed always to be more than 0.124 inch in thickness. The histogram in Fig. 4 shows this distribution. What

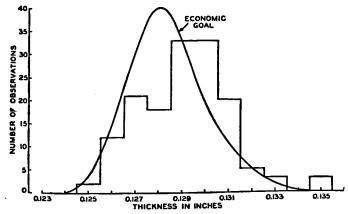


Fig. 4.—How Maximum Control Saves Money.

does the theory of maximum control tell us about the uniformity of coating? In the light of the previous section the lack of smoothness in this distribution is indicative of the presence of assignable causes of variation which can be removed. In fact, an investigation revealed assignable causes of variation, and on removing these, the resulting quality approached the distribution shown by the smooth curve of Fig. 4, representing the state of maximum control for this particular kind of coating. By attaining this state of maximum control, it is apparent that the average thickness of coating is materially reduced without increasing the probability of obtaining a defective thickness.

Not only does control lead to a saving of material in such cases but it also leads to a more uniform product because as shown in Chapter XXIV of Part VII, it is practically impossible to sample for protective purposes unless the quality is controlled.

#### APPENDIX II

PRESENTATION OF ORIGINAL EXPERIMENTAL RESULTS USEFUL IN OBTAINING AN UNDERSTANDING OF THE FUNDAMENTAL PRINCIPLES UNDERLYING THE THEORY OF QUALITY CONTROL

The six tables in this appendix give in detail the results of 4,000 drawings from each of the three experimental universes referred to in the text. Tables A, B, and C give the original drawings divided into groups of four in the order in which they occurred. Tables D, E, and F give various statistics for these samples of four. It should not be inferred that these statistics are arranged to correspond to the samples as this is not always the case. We have made extensive use of these data in our discussions of the theory of quality control, and it is advisable to reproduce these data if for no other reason than that the reader may wish to carry out for himself computations similar to those referred to throughout the text.

There is, however, a far more important reason for presenting these experimental results. It will have become apparent by this time that statistical theory rests upon a fundamental natural law—the law of large numbers. In the last analysis we must always appeal to experimental evidence to justify our belief in such a law and to give us a feeling for its physical significance. For example, in the discussion of the theory of statistics, we always have to talk about doing something again and again under the same essential conditions; or, as we have said, under a controlled condition where the chance cause system is constant.

· We have used these data in various places throughout the book to illustrate a controlled phenomenon. In particular we

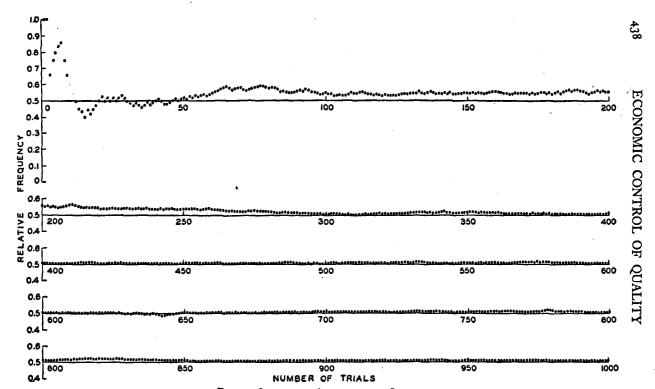


Fig. 1.—Statistical Approach to a Limit.

have shown how they can be used in checking the results of the mathematical theory of distribution, and in certain other instances, in indicating the probable character of some distribution function not yet determined a priori. Most of this discussion was limited to the statistics of samples of four. Often, of course, we wish to investigate in a similar way the nature of the distribution functions for sample sizes other than four. This can readily be done for the three types of universes through the use of the data in Tables A, B, and C.

These data have been used in many ways other than those mentioned in the text. For example, they have been found to be of great use in the experimental determination of the correlation between the average and range, which correlation is sometimes required in the establishment of an efficient inspection method where it is not feasible for one reason or another to calculate the standard deviation.

In this connection it is perhaps worthwhile to illustrate the use of these data in indicating in a somewhat more concrete manner than was done in the text the nature of the statistical limit involved in the statement of the law of large numbers. For example, suppose we consider a thousand drawings from any one of the universes, let us say the normal one. It will be recalled that half of the 998 chips were of one color  $^1$  and half of another. If we let p represent the ratio of the number of chips observed to be of one color in a series of n drawings to the number n of drawings, then this fraction p should obey the law of large numbers and approach  $\frac{1}{2}$  as a statistical limit; that is,

 $\underset{\mathbf{z} \to \mathbf{w}}{Ls} \ p = \frac{1}{2}.$ 

Fig. 1 shows the statistical approach of the fraction p in one such series of 1,000 drawings.

Obviously, as a result of the first drawing, p will be either zero or unity. In fact, p will continue to remain zero or unity until a chip is drawn which is of a color different from that of

<sup>&</sup>lt;sup>1</sup> Colors used instead of plus and minus.

#### ECONOMIC CONTROL OF QUALITY

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the first one drawn. Thereafter p will never become equal to o or 1, but will always lie somewhere within this range. In the definition of a statistical limit, it was pointed out that there is no value of n such that for n greater than this value, the absolute value of p always becomes and remains less than some preassigned quantity—characteristics which belong to a mathematical limit.

The experimental results shown in Fig. 1 illustrate how the fraction p oscillates back and forth. A student of the theory of control can well afford to carry out similar tests of this nature until he has gained a clear picture of the significance of the statistical limit.

#### **TABLES**

- Table A-4,000 drawings from a normal universe consisting of 998 approximately identical chips marked as indicated in Table 22 of the text.
- TABLE B-4,000 drawings from a rectangular universe of 122 approximately identical chips marked as indicated in Table 28 of the text.
- Table C-4,000 drawings from a right triangular universe made up of 820 approximately identical chips marked as indicated in Table 28 of the text.
- Table D-Observed distribution of arithmetic mean  $\overline{X}$ , median,  $\frac{\text{Max.} + \text{Min.}}{2}$ , mean deviation  $\mu$ , standard deviation  $\sigma$ , and ratio  $z = \frac{\overline{X}}{\sigma}$  for 1,000 samples of four from the normal universe.
- Table E—Observed distribution of arithmetic mean  $\overline{X}$ , standard deviation  $\sigma$ , and ratio  $z = \frac{\overline{X}}{\sigma}$  for 1,000 samples of four from the rectangular universe.
- Table F—Observed distribution of arithmetic mean  $\overline{X}$ , standard deviation  $\sigma$ , and ratio  $z = \frac{\overline{X}}{\sigma}$  for 1,000 samples of four drawn from the right triangular universe.

#### TABLE A.—DRAWINGS FROM NORMAL UNIVERSE

1.7 .8 1.4 .5	P. 19. 4. 4.	4414	-1.8 9 6 1.7	.5 7 .8 1.0	-1.1 .7 .1 5	7 1.5 4	-1.6 1 1.3	5 8 .7	1 .2 0 -1.7	1.0 -1,2 0 -1.9	9 -1.8 .6	4 .0 .1	2.2 1 9 -1.2	4 -1.0 0 -1.0	-1.1 -2.9 0	8 .4 .9 -1.8	1 5 6	9 .7 .8 5	6 8 -1.4	2 .9 7 9	1.1 .2 1.6 -1.8	-1.6 7 1.1 1.2	.2 1.6 8	1
1.0	-1.6 .7 1.5	÷ ; ; ;		2.1 -1.7 1.5 2.5	.4 -1.1 -1.9 -1.4	.2 2 1.1 1.0	-1.6 .1 -1.0	5 1.4 1 8	-1.2 8 -1.0	9 .1 .9	-1.5 1.4 8.4 -1.7	.6 1.8 -1.1 1.1	-,5 .1 .8 0	9 -1.0 -4	9 8 1.4 -1.1	.9 6 6	1.0 1.4 6 -1.2	7 6 1.6 1	7 .7 1.4	.6 2.2 0	.5 7 -1.9 -2.5	.8 -1.5 1.0 1	-1.2 0 8 5	-1 -1
.s. .s .6 .8	1 0 .9	-1.8 -4 5	.6 .7 .9	.8 -2.1 5	-1.9 1.4 1 1	.1 -1.2 .1 6	8 1.7 -1.8 5	1 6 .8 1.4	1.8 4 .2 5	1 1.0 1.8	7 8 7	.4 5 8.2 2	1.0 7 6	.8 -1.4 2	.9 -1,1 .9	1.2 5 5 1.8	·	1.5 8 -2.0	-1.5 .1 -8.0 -1.4	1.0 1.9 .8	8 .9 4 -1.2	0 .6 .4 -1.2	1.1 .7 3	-1
.8 4 5	5 .8 1.0	-1.0 7 2 .5	-,1 -,1 -,1	5 .5 .7	1.2 2.9 .8	6 8 8	.8 1.0 .1 8.8	6 2.3 .5	1.6 .2 -1.0 8,0	5 1 6 -1.5	.1 4 .4	1.6 0	.5 -1.0 .4 1.6	2.5 8 .5 3.4	8 1.6 2.2 1.8	-1.6 6 -8.8 1.5	.6 2.8 -1.1 2.0	1 9 -1.5 -2.1	.5 .1 .2 -1.8	2.2 .4 -1.5 -2.5	7 1.1 9 1	2 8 1.5	.2 3 -1.4 0	
.5 4 .1 8	2.0 1.5	.5 4 1 0	1.2 4 1.0	8 -1.4 1.4 .9	-1.8 1.5 .6	.7 -1.1 1.7 -1.6	1.8 8.2 6 5	5 9 0	-1.9 -2.7 5 1	-1.5 8.5 -8.2 -1.0	1.4 .5 7	7 .5 .6 1.9	-1.8 .8 .1	2.3 .8 .7	.1 .6 .5	4 -1.0 0 1.7	5 1.4 .4 1.7	4 .6 7 -1.0	.7 1 .6	.4 5 1.0	.9 .2 .1	1.0 -1.5 -1.1	1.8 .4 6 6	
.4 9 5	6 7 1.0 5	1.5 6 5	.1 8 -1.5 -5	0 1.8 -1.0	1.0 .8 -1.9	.7 ,2 -1.8	-1.6 .1 -1.5 -2.7	-1.9 4 .5 1,2	.5 .2 .8	0 -1.6 -1.5	9 5 .6	5 1.1 -1.5 4	-1.5 8 8 7	-1.5 .3 9	.1 4 .9	-2.6 -5.0 7	.7 -2.2 0 7	-1.0 1.7 .7	8 -1.5 -7 7	2 .7 1.9	5 2	1.5 1.4 1.5 8	.5 -1.7 -1.2 -1.5	:
1.1 1.1 1.8	.5 2 4	.8 .5 6 1.0	1.5 -8.6 8 9	-1.6 .4 -1.0	.5 -1.5 0 -1.6	0 5 1.0	2 1 1.7 1.1	.7 6 -1.6	2.8 -1.6 -1.5 8	1.5	.6 7 -1.5 -1.8	1.1 .2 .5	.1 5 -1.1 2.5	1.1 .1 6 0	1.9 1.5 -1.1	-1.8 6 4 1	1.1 .8 -2.0	.6 2 .5 2.1		1.5 0 8 1	5 1.1 1.8 7	.5 2 1.1 1.8	1.8 1.7 5 1.5	:
	7.4 1.5 .1 1	.8 .1 5	9 1 .5 -2.1	-1.0 -1.0 .1 1.4	.5 4 .5 1.4	2.0 -1.1 -2.3	.9 2 5	.7 1 5	2 7 1 -1.8	2.1 .6 1.5 1.1	-1.5 .5 -1.6	1.1 -1.1 .0		.5 .2 .1	1.1 -1.8 1.5	.5 1 8 -1.1	1.0 .6 -1.1	1.5 1.2 1.7	1.8 .4 3 -1.0	.5 6 1.9 9	.1 .2 .5	9 .5 1 1.4	-2.1 3.0 .8 1	-3
1.1 1.8 1.8	a.0 1 9	.4 .9 .2	9 1.0 -1.0 -1.8	-,7 .1 .9	.1.9 .0	7 -1.2 .2	8 .2 2.4 1.8	5 6 0 1.1	1.4 .7 1.7	.4 5 1.8 1.1	-1.0 6 6	9 8 4	-1.4 .5 .2	-1.4 -4 -1.4 1.1	.5 -1.8 -1.0	0 -1.0 -1.0 9	.4 4 1 1.5	5 6 1.1	9.5.5.4	1 .3 .1 1.0	2 9 6	2 -1.0 1.5	-1.0 1 .1	-7
.1 5 8	.8 .4 1.6	-1.8 1.1 -2.8 -2.0	.5 .9 1.9	.1 7 1.1 8	.7 4 -1.0	-8.0 1.1 1.0	-1.5 1 1	.7 1 6	-1.4 .6 0 -1.7	.7 1.6 .9	.6 .6 -1.1 8.8	.6 .8 .2	1.7 5 1.3	.8 8 1.1	8 6 -8.0	.1 -1.5 .2 .5	8 8 5	.7 6 .5	6 .8 -1.7 -1.8	.8 1.4 5 -1.1	-1.0 -1.0 1	.4 9 2 1.8	1.0 .1 -1.0 .5	3

6 -1.4 -1.4 0		.9 .B 0	.6 0 8 -1.4	-1.0 -4 5	1.8 8 6 5	8 .4 1.8 -1.1	.9 .8 0	.7 2 .5	9 0 .8 1.6	.\$ .\$ .8		.8 .9 2	-1.1 0 -1.1	1.4 .8 .8	1.8 .6 .7 -1.1	-8.0 .6 1.8 5	 -1.5 1	8 -1.7 -4.7	.7 4 4	1.4 8 -1.4	-:0	8 -1.6	-1.8 -1.8 -1.8	.1 .8 -1.6 1.8
0.000	4 -1.1 -3	1 -1.1 -2.7 -1.0	-1.0 .7 .6 -1.0	0 4 4 1.8	-1.8 -1.0 .2 .5	.1 4 1.1 -1.8	.8 -1.1 .2 .5	1.9 4 .8	8 3 -1.7 2.0	7 .4 .8	1111	1.8 1 1.4	5 .1 1.7	1.8 8 1.7	* 9 9 7	4.0.0	1.1 1.1 1.1	<b>?</b> ???	7 1.0	777.	.7 .7 2.0	8.8 -1.4 .1 1.7	.4 1.8 -1.8	777
-1.3 -1.3 0	10.84	1.5.9.9	-2.5 1.0 -1.8 3.8	2.8 0 7	-,2 1.3 -,1 8.1	8 6 -1.0 .4	-1.8 -1.0 8 -1.0	2.5 .8 1.3 1.6	.4 4 .5	.1 1.8 .5	0 .6 -,1	8 0 -1.1 3	-1.0 1 -1.1 1.1	.8 .8 1.7	2.0 .9 .8 -1.1	8.1 8.1 1 6	-1.0 -:: -:4	7.8 7.6 7.8 8.8	6 1.3 .4 -1.0	7.44	-2.8 8 1.1	8.5 .8 1.6	.7 1.0 -1.4 1	
-,4 -0 -1,5 -1,5	4777	4 1.3 5 7	5 -1.0 2	****	1.7 2.7 .4 .8	.4 2 5	8 8 1.1	-2.0 -1.1 -2.5 1.0	9 .8 .1 0		4 8.8 .6	.6 4 6 3.0	1.6 .8 0 .8	8 3 0 1.1	-1.0 -1.7 1.6	2.2 .5 1.1 7	21 2.1 1.2 •.1	••••••••••••••••••••••••••••••••••••••	8794 1171	1,8 1,1 2,0	-1.4 .8 -2.3	6 4 1	7	# 7 ° °
-0 -1.8 -1.4 -1.1	0 1 4	.6 4 .8	1.8 .5 -1.0 -2.6	.1 2 4 1.8	1.5 4 -1.6 1.7	.9 -1.0 1.9	-1.3 .6 .8 8	.6 -1.1 3	8 -1.1 -1.1 1.6	1.0 -1.9 1.1	8 1.7 .8 1	4 -1.0 5 1.2	-1.1 1.0 .5 -1.2	.8 .0 .8 1.4	1:45. 1:45. 1:45.	.0 .5 -1.8	1000	.1 7 0 1.5	 	.1 -1.7 1.0	1.0 -1.0 1.6	1.5 1.8 4 .1	4 -2.0 1 5	-1.0 0 1.1
.9 .4 1.8 0	6 .6 .4	-1.4 1 1.4 -1.0	1.8 -1.8 1.0	6 1 1.2 .3	5 0 .7 1.1	1 8 .2	1 2.1 .6 .2	.0 1 -1.6 7	.6 .9 1.9 1.7	.8 0 2 1	-1.0 .1 -1.2	1.4 3 .8 .1	1.4 0 6 :	.6 -1.1 7 .7	2.2 .6 -1.7 5	0 8 .2 1.7	.7 -2.4 -1.7 -1	-1.5 2 1.2	9 -1.6 3	7 -1.3 .0	-1.4 .1 3 5	.7 .1 .8 4	1.4 5 4 5	1.0 -1.0 -1.1 -4
7 .8	1.5 -6 -1.1	.6 .5 0	1.0 5 1.4 1	6 .5 .9	-1.5 4 9	.6 .9 .5 6	.9 1 7 1	8 1.3 8 6	-2.0 -,2 -,9 -,2	6 .4 1.1	.1 -1.4 -2.0 0	.0 .2 -1.4 3	1 1.4 0 1.3	1.0 3 -1.0 1.1	3 6 6	2 .9 .8 .0	.1 9 0	5 -1.2 1.5	2.7 -1.1 4	.3 3 .3 -1.1	-1.1 1.5 -1.1	.2 6 .1 .0	1.7 .7 -1.8 -1.8	1.5 -2.6 -,4 -1.2
0 1 1	1::	1.8	1.0 -1.1 .2 4	.2 .1 1.8 .7	1.5 1.8 9 1.6	.6 7 8	2.3 1.2 0	-1.6 -1.5 -1.5	3 -5 -1.4	5 8 8 2.6	-1.3 -1.2 -1.6		-1.0 1.4 .8	1.0 .6 1.7	.1 .5 .5		.6 .1 1.5	-2.1 1.8 .9 5	.5 .8	.1 -,2 -,8 -,4	.0 -1.9 1.9 .0	2 .2 1.5 1.0	1.0 2 8 1.0	
::	1:1	1.0	1.8	1 2 8	:	1.5		-1.1 4 .9	5 1 1.5 .3	3.5 5 -2.3	-1.8 3 1.5 .9	.8 2 .3 9	1.4 1.4 4 .9		 .; 1.6	-1.0 1 .0	5	-1.0 -1.0 .0 -1.8	.1 .8 0 1	.0 .1 -2.5 1.1	1.0 6 .2 8	4 1 7	4 -2.2 1.5 0	- 1
		:-	3.8	6	1.8		:	.2 1 .6 3	1.6 -1.2 6	.1 .9 2 .3	-1.8 -1.5 4 -1.1	1.7 -1.3 -1.6	6 .8 1.1 1.3	8 4 -1.7	8 2.4 8	.8 9 1.0 4	4 3 7 3	1.8 -1.1 0 .7	.6 1.1 1.8 4	4 3 1.8 1	5 -1.6 4 1.1	.8 -2.4 3 6	-1.0 1.1 2 .8	 1.1 1.4

TABLE	A.—Drawings	FROM	Normal	Universe-	(Continued)	

.9 .5 9	1.4 2.7 .8 -1.0	9 -1.6 0	-1.2 -2.3 -1.0 1.1	7 .4 1.1 1.4	.4 1	3.3 -1.3 .4	6 1 5 -1.1	9 5	1.6 -1.1 1.0	.0 4 2	.1 1.2 .8	.6 .1 0	.1 1.2 7	2.7 8 1.7	.4 0 .1	.5 5 6	1.9 1.6 7 -1.5	1.5 .6 .8	1.5 .6 8 -1.7	.\$ 8 8	-8.0 5 4	.1 .2 1.9 -1.3	.1 -2.5 8 -1.0	1 8 8.6
-1.5 5 -1.8 1.4	.8 5 .6	.7 8 .9	1.4 -1.1 1	0 .8 -1.5 -1.8	2.0 8 1.7	1.1 .1 .9	6 1.1 1.0	.5 8 5	.7 6 7	-1.1 .6 -1.2 1.7	4 .6 1.0	.2 4 -1.5	4 0 5 -1.7	.6 2.3 .7	-1.4 -2.3 -1.5	-1.5 .8 1.1	2.2	.7 -2.4 1.2 1.5	.6 1.3 1.3	1.4 .9 3	.7 .6 -1.0	4 .8 -1.5	-1.6 1.6 1.5	3 .3 8
	9 6 4	1.5 .8 1.8 0	9 -1.5 -1.8	8 8 -1.4	4 .6 -1.8	2.0 8 9 1.5	.6 .4 -1.0	.5 .4 -1.9 .8	.1 9 0 3	3 2.1 7	7 1.4 7 -1.8	1.6 1.1 -1.1 0	1.8 4 2	.3 .1 4 -1.5	5 5 -2.0 -1.0	6 -1.3 .5 -1.2	1 .7 -2.1 -2.1	1.6 .2 1.6 1.3	5 8 9 -2.4	8 6 6 1	1.6 .2 -1.2 9	1.7 2.8 -1.6	.1 0 5 -2.4	4 7 -1.4 .5
77.50	1 5 -1.5	-1.1 .7 5	.8 -1.7	.: 4 1.0	.5 5 .6 1.1	<b>440</b>	1.8 .5 .7 1.5	0 1.0 1.6	.1 4 -1.8	.7 .5 5 -1.4	2 -1.5 .9	-2.0 .2 .7	2 -1.4 .2	-1.0 1 -2.6 7	0 8 6	-1.5 6 5	-1.4 -1.1 1.0 -1.8	0 -,6 .9 1.1	9 .1 1.1 5	-1.6 2 1	8 9 0 4	.2 1.5 5	3.0 3.0 4	1.1 .4 1.5
1.3 8 4 6	- 7 9 5	2 1.1 1.4	5 1.8 1.2	7		1943	11.8	5 7 -1.4 .8	5 5 -1.5 1.2	6 8 .9	5 7 5	-1.9 -6 8	-1.7 .5 2.0 -1.8	-1.0 1.7 1	4 7:8 9	9 .5 -1.5 1.5	-1.2 .3 -1.3	.7	1.5 3 5 2	4 .7 -3.6		-1.5 -2.2 7 1	7 -5 -2.1 0	5 4 2.8
.9 .5 .5 -1.1	6 1.1 1.4 8	1.8 1.8 -1.0	.7 1.8 7 -1.6	4 2 1.6	6 2 .5	91.0	1 -2.9 2.1	.6 .7 -1.1 0	4 8 6 -1.5	6 5	2.5 1.1	.7 .6 7	3 0 .5 1	0 ,7 .2	.9 7 -1.6 -2.5	.6 8.1 .9	.7 .6 2.2	1.7 -1.9 .4	4 7 -1.6 4	.5 -1.2 -1.3 5	1.0 -1.6 4	6 -1.8 -1.0	7 -2.1 .4	2.0 4 2
1.5 5 .4 -1.0	1.7 5 .9 -1.4	.7 8 1.0 5	-1.1 2.5 6 8	.5 1.8 .6 1.1	-1.1 -2.2 4	1.0	8 .4 9	1.0 -1.6 -1.0 -1.2	0 -1.6 5.0	8 8 1.1 -2.0	2.1 .1 .1 2.5	.2 1.1 7 1.7	-1.7 1.7 -1.8	.1 .5 7	7 3 1.4 5	.5 .7 7	1 -1.0 1.4	5 .1 -1.4 1.8	.9 .6 9	.4 .3 6	.1 2.7 9.	-:1 -:5 1:1	* ?	-1.8 9 .9
1.1	-:0 ::	.6 .2 1.0 2.5	1.0	.1 1.0 1.8 -1.4	-1.4 1 1.1 7	1.5 .8 4	8 .6 .3	1.5 .5 .6 -1.4	1.0 .9	5 -1.5 6 7	5 .6 1.8 8	.1 1.6 .7	.8 .7 .7	.8 -2.2 1.2	.5 .4 8.0 -1.3	.7 .7 7	1 0 .2	.8 .2 1 1.9	.6 5 -1.1 6	-1.1 5 7 1.2	1.0 1.0 8.	9 2 2	8 5 5 5	9 -1.0 .1 -1.9
-,1 -4 -1.5	.2 .5 1.8	.7 -1.3 1.6	-1.2 1.2 1 -1.7	.8 8.6 1.0	5	1.5 .3 -1.4	8 1.1 -1.2 -1.4	7 4 .6	6 5 6	.8 6	1.0 7 5	1 9 .9	2 .1 .1 -1.5	-1.8 5 4 -1.8	6 -1.6 -1.4 9	1.0 4 .8 -1.5	.4 9	2.7 1 .5	-1.5 1.1	-1.5 .6 -1.8 1.4	.9	1.1 1.9 .8 -1.5	1.7 4 1.9 7	.8 -1.0 1.7
-1.0 1 .1	-2.2 4 .1 1.5	.6 .5 5	7 -1.8 1.6	.1 -4 -1.8	6 9	.7 -1.5 .2	9 .4 2	.6 .7 .8	0 1.6 -1.2 0	.4 -1.4 9 1.8	9 8 6 -1.1	-1.5 -1	1.4 1.0 .4	-1.1 1.3 7 -1.8	1.8 8.0 -1.7 1.5	.8 7 1.6 3	.7 .2 8	.8 .1 1.6 -1.2	.3 -1.8 -2.5 -1.4	2 -1.6 4 .8	4 -1.1 -1.1		.6 -1.6 1.5 -1.9	6 3 .8 1.1

4:- 6:- 9:- 7:8	8, 1, 6,	0 ·-	9.1- 0 0	0 f.s 0.	8°1	8'- 8'-	-"7 -7"0 1"8 3"1	1 1 1 1	0°1-		9 7.0		8 4 6 6 1 7 7 9	4404	8 4 6 B	0	6 6 6. 1-		6. 3	9°E 8°e 4°		8 6	8"- "T"- ""-	6 8.1. 8.4.
9°7-	9.1 8.1 0.1-	6. 6.	8.4-	7°7 8°7- 8°-	9. 0 1	9: 6: 0:T	9°7 9°-	9. 7. 7. 7. 8. 7. 7.	12.1	 	g:	8.1- 7.5 7.5	8°T 6° 8°T	7°0 • • • • • •	8. 8. 8. 8. 8.		1.1.	1885	7: <b>•</b> 7: <b>•</b> 1:0	g g g g	8. 2.1. 6	9°-	4" 8"T- 9"	a. a. a.
4°. 0'8- 4'. 1'0	0°T- 0°T- 0°T-	0'. 0'. 1'.1	8°T-	e:- C'-	₽: 4: 0:1	6 7. 8.s-		-7:8 -8 7:8	9 9	1 4 4 7	4°T-	7°9 7°0 7°	 6. 1.1.	3 6 6		0 0 0		9 2.0 4	· · · · ·	0°- 8'- 1'- 1'-	-7°0 -°0 -°2 7°8	g:-	8. 6. 0.	9 9 4
6° 6°7 8°7-	8°7- 4°-	0.8 0.1 8.8-	9°T- 8° 1°T	9 4 4	4: 9:7 9:-	0.1- 0.1-	4°E- 4°E- 8°	4° 8° 1° 7°8-	-:3 -:8 1:1 1:0	7.0 7.0		8 8. £	8 8	7°5 7°5 7°8 7°8	8.1- 8.	8. 6.	4. T 0 0.t-	9'- 6' 7'T-	8°t	8, 8, 8, 8-1	9.1- 9.8 9.8	9'- -7'4 -7'0	8°T 1° 9°T 9°	9
9°T- 9°T 1°T- 0	8°T- 9° 1°T- 1°T	8'T- 8' 7'	T'- 0'T- 0	4 - 8 - 4 - 8 -	0°T 4°- 1°-	€: 7: 7: •:7-	1161	9°2 e 7°2 0		÷0 00	ù à ē ù	g. T 6.1	8.8 4	\$ 5 5 T	9 % 6 4	t. f. e.	4*- 0*T 8* 7*T-	9 4 T	8 6 8	7°7 7°4 9°-		8 8. 1.1	9°7 9°7 9°7	
9*T	1,1,1	8.1- 9. 7-	7'8 7'6 	1.0 8. 1.0	8 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	8°7- 8°7- 8°8-	0 1. 9.	7.0 -1.0	4 4 5 5	9.5 8.8 9.8	9°- 9°- 9°-	\$*T- \$*T- \$*T-	1.1-	4° 0°- 1°-	444	\$ 8	8*- 0 9*T-	8 8 8	9.4 9.4 8.	8.1- 8.1-	8° T'T- 9°	0°t-	8. 2.4 8.	100
0.1 0.1 0.	7°8 7°8 7°6	8.6- 8.6-	8°7 7°8 7°9 7°0	3°0 7°9 3°0	::7:	9 · · · · · · · · · · · · · · · · · · ·	91- 91 91 91	7.1 7.1	12 12	4 5 5 5	8. 1.1- 8.	9:- U 0: 0:T	8.8- 0 0.1	g. 4 8	1°4 -1°4 -1°7	9°-	3. 0.	9°7- 9°7-	9°°°	0°7-	8. 0.1	# T . 4 . 9 . 4 . 9 .	9.	
*** *** **-	***	4°E 9° 4°- 9°E-	8'- 8' 9't	6. 6.	T*8- T*- T*-		  0 7-2	1 : : :	1111		9.1- 9	0.8- 8. 8.	8 8	0' E'E-	8 6.8 7.	6 6 6	6 6 5	6. 9.	1.1-	4. 1 0	0°T-	9.1	8°1-	8
4°E	7 7 7	F- 8' 8'-	0"T T 0"T	8.4 0 1.1	4 1 1	9°T 0°T	7.0	- 1 - B	10 1	7.0 7.0	1.1 1.1	1	#:- #:- #:-	6:- 6:1 8:1	\$*- T*T 0	6.1-	9 9 7.4	0 ·	6.1- 6.1- 6.4-	9°7- 1°7- 9°7-	9. 9 4 9.T-	9°8 7'8 8'8		1000
9°-	0°1	8"8 1"1 8"1-	177	:	7° 8°7 9°7-	111	1:- 0:T	81- 61- 61- 71-	1.0		8.f-	7:-	8:- 0:7	7°1	8°- 1'8 9'-	9: 1: 1: 0:T-	9°7	1°7 9°7- 9°	***	\$:- 4:-	6:- 6:- 7:- 4:-	9°T-	***	

						TAB	LE ]	B.—ì	Drav	VING	S FR	ом :	Rect	ANG	ULAR	Un	IVER	SE						
7 -1.4 .5 1.5	-2.5 8.2 8.7	1.7 8.1 1.6 1.5	.8 -2.7 3.0	.0 5 -1.2	-1.9 1.0 8.4 1.7	-2.5 5 -2.6	-1.8 1.8 -1.5	-5.0 2.5 1.6	-8.1 1.1 2 6	1.8 1 6 2.6	-2.7 -1.2 -1.5 -1.2	8 -1.1 -2.8 -1.5	2.7 1.2 -2.6 3	-1.2 -2.4 1.2 -1.6	1 -2.6 -1.5 2.7	-2.9 .7 .8 -1.0	2.1 1.0 .8	.2 2.2 1 -2.5	1.7 6 5 -1.5	7 .5 4	3.4 1.2 3.7	-1.6 2 1.1 2.5	1.5 1.7 -2.5	5.0 -1.0 .6 -1.7
8 5.0 1.1 8	2.5 -2.7 6	-2.0 -1.2 5 -2.6	1.4 6 4 1.0	5.0 7 2.0 1.7	2.7 3.1 -1.0 -1.6	-1.7 2.4 -\$.5 -1.4	.7 1.7 9 -1.4	1 6 -2.2 1.5	-2.1 2.1 4 -2.2	-1.8 2.6 3.0	-2.2 -2 7 1.0	.5 1.5 .3	-2.5 1.6 -1.1 1.8	-1.2 -1.0 .1 1.4	-2,6 .6 -1.1 1.9	5.0 6 1.0	-2.5 1.4 -1.2 .8	-1.4 2.6 2.1 2.5	2.0 -1.8 .1 -2.8	5	1.4 -1.1 -2.1 -2.9	1.5 1.7 -2.9 1.5	1.5 -2.0 1.6	1 .9 1.1 2.7
2.2 1.8 7	1.1 1.5 1.0	6 -1.7 8.6 -8.9	.7 .0 0	7 -2.0 -2.6 -1.5	-1.7 2.9 1.5 9	.5 .2 -1.5	2.4 1.1 -2.6 2.7	1.8 .7 1.5 1.8	-1.2 2.8 1.5	2.2 -2.5 -2.9	3 1 -2.7 -2.5	-1.4 1.5 -2.4 1.9	2 -2.1 1.8 1	8 -2.7 9 2.8	-1.2 2.5 2.3 3	5.0 8 .5 -1.5	-2.8 -1.1 -3.0 2.1	.8 1.9 2 -1.7	.4 -1.6 5 5	1.0 1.1 .8 1.6	8 2.2 .8	2 -2.3 1.3 2.8	1.2 2.2 -2.8 -2.5	-1.1 -2.6 -1.4 1.0
2.2 1.6 5.0 -1.8	8.0 8.5 4	-1.8 2.9 -2.8 2.5	8.4 8.0 -1.1 1.1	-2.9 8.6 -1.0 -1.5	1.0 -1.1 -2.0 -1.7	2.5 -8.0 1.1 5	-#.0 .6 .8 -1.0	1.6 1.1 .6 -2.6	2.9 -2.6 2.9	-2.8 -1.8 -1.5	-1.8 -2.6 -2.2 -2.4	-2.0 2 -2.4	1.9 1 -1.7	1.5 5.0 2.2 1.2	.7 1.0 .9 2.7	-1.5 -1.8 -2.0 2.3	-1.5 -2.5 .9	9799	2.2 2.7 5	-2.5 -2.9 -2.5	-2.6 -1.5 .6 -2.7	1.7 9 1.5 -2.5	2.8 2.4 -1.1	2.2 2.2 1 2.3
1.7 6 5 -1.8	7 .5 4 2.9	2.4 1.2 2.7	-1.6 8 1.1 2.5	1.5 1.7 -2.5	3.0 -1.0 .6 -1.7	8 5.0 1.1 8	2.1 2.5 -2.7 5	.8 2.7 2.1 9	-1.9 1.8 .6 9	.1 7 1.1 -2.2	-1.7 2.2 1.1 .1	.7 1.1 2.8 .1	-1.5 8 -1.8 8	2.0 2.2 .7 -3.0	5 1.0 -8.5 1.7	1.7 .6 1.8 2.1	-2.9 .1 2.6 1.1	1.0 2.0 -1.6 -2.5	4 -1.9 2.7 -5.0	7 .7 -1.7 -2.1	1 .4 2.5 1.9	.5 1.6 -2.2 -1.6	5 2.8 -1.9 1.7	6 -1.9 4 8.7
7 -2.5 4 5	-1.6 2.0 6 2.0	2.1 2.1 2.2 2.8	.6 -1.9 -5 2.5	5.0 -3.5 2 3.1	-2.5 .1 1.5	-1.1 1.5 5 8	-2.8 2.1 -1.6 2.7	-2.1 -9 -8.9 -1	.2 -1.5 1.5 2.4	.4 .1 2.5 -1.8	1.8 -1.8 -8.5	2.1 1.0 .4 1.7	3.0 4 .4 1.6	2.4 1.9 -2.5 -3.0	-2,0 -1.1 -1.6 1.5	-3.0 1.7 -1.4 5	2.8 1.2 -2.6 -2.7	1.8 .7 8 2.6	.6 1.0 9 2.2	-2.4 1 1.7 2.8	1.5 9 -1.9 8	75.25	2.1 1.0 1.8 1.1	.5 7 -8.9 .5
-2.7 1.5 -2.5 1.5	1.7 -8.0 2.7 -1.1	1.7 -2.1 2.5	9 15 4 15	2.5 1.5 -3.0	-1.0 -1.5 2.2 -3.4	2.0 1.2 .6	4548	5.0 1.5 .4 1.5	-8,6 ? 2,5 -2,4	1.4 .7 8 1.8	1.4 2.7 -8.5 2.9	-1.9 2.7 -2.5	-1.9 5 1.5 -1.7	-2.8 -2.9 2.0 2.7	-2.7 1.8 8.9 -2.6	-1.1 -2.2 3.7 -2.0	.6 2.5 6	2.0 .1 2.1	8 2.7 -2.9 1.5	1.1 8.5 -2.4 -1.5	5 -1.0 -3.0 1.5	.5 .8 2.2 -1.0	2.8 -3.2 -2.2	.8 7 .8 9
2.1 1.7 1 8	-2.6 -1 -1.9	2.8 8 2.9	-1.6 1.5 -1.1 -1.8	.8 .9 1.5 -2.4	2.0 1 -2.8 -2.7	-1,8 -1.6 1.8 .8	7.5.7.9 -2.5 -2.9	-8.6 -1.0 1.5 6	-1.8 -1.4 2.7	-1.0 -2.9 -1.9 5	8 -5.0 -1.2 6	5 1.0 1.7 8.5	-1.5 -8.4 7 .8	2.2 2.5 5.5	1.8 -2.7 2.4 2.1	1.4 .5 .1	8 1.8 1.1 2.9	5.0 2.2 -1.2 2.5	.4 -2.6 9 -2.5	7 -2.9 8	-1.0 1 .8 -1.6	-1.6 -2.0 .9 1.5	1.2 -2.1 -2.1 1.4	-8.8 9 2 5
-2.6 -6 -1.9 5	-2.2 2 1.5	-1.5 2.2 9 2.5	1 2.0 .7 8	.5 -2.7 .2 9.0	-5.0 2.2 1.4 2.0	2.5 -5.0 2.0 -1.7	-1.1 .5 9 -8.0	8 -1.2 -2.4 -1.6	-1.1 -1.0 -2.4 .8	2 1.5 2.5 2	7 2.8 -1.1 -1.4	9 -1.9 -8.4 8.9	5 .4 .7 2.1	1.6 2.4 2.5 1.6	.9 -1.5 5.0 -1.8	.1 .9 2.9 -2.8	1.7 -2.6 2.8 -1.5	2.7 1 .5	- 6 2.8 -5.0	2.5 5 2.7	2.7 1.5 -2.5 2.6	2.9 2.8 2.8	1.5 5.0 4	-1.0 -1.8 -2.5 .3
5 2 .5 -1.3		4 -2.9 -2.1 -5	2.0 2.1 1.0 .B	.9 1.8 2.4 .7	.2 7 1.7	-1.7 -1.8 .4 1.6	1.6 -2.9 8 -1.9	1.1 8.1 5.0 8.5	1.6 .8 -1.5	1.8 1.0 6	2.6 1.4 -1.8 -8	7 8 5	-8.5 1.1 1 -8.6	2.5 -1.1 -8.8 -8.8	-2.0 1 -1.0 5.0	2.9 2.8 8	2.7 1.5 .8 7	-1.6 -3 6	6 1.8 -2.4 2.9	1.8 -3.0 -1.9 -2.2	-2.1 -1.2 1.6 1.8	8 -1.6 5 -2.5	-1.0 8.8 -1.9 1.1	-3.0 1.1 2.0 -2.1

1,2 -4 -1.9 2.9	-1.1 1.5 8	8,5 -2,7 8,0	1 .7 4 -2.1	-2.2 -1.0 -2.2 -9.2	2.0 8.0 8.0	2.7 1.6 -1.8	2.1 2.9 7 5	2.7 1 3	.4 -2.8 1.0 -2.0	-1.2 B -2.4 -2.7	-1.4 4 1.0	-1.1 -1.6 1.3 9	-1.0 -1.5 -8.1	-1.1 1.2 .7	1.7	.1 -1.8 -9 2.8	2.3 1.1 5 6	9 0 8 4 2 2 8 8	.5 1.5 -1.5 0	3377	-8.8 8 8 2.0	-1.0 8.8 -2.9 8.0	4 -1.1 -8.8 -2.6	.0 0 1.0 2.0
.9 -2.7 8.0 2.7	8.8 6 1 1.1	1.6 -1.8 8.1 1.0	1.6 -1.5 7 -8.7	-1.4 .5 .8 -2.5	-1.3 9 9		5 -2.0 -2.3 1	8.5 1.8 ~.9 1.4	-2.8 -2.8 -2.0 8.0	=_8 8.1 8.6 4	2.0 .1 .6 1.4	1.4 1.8 2.6 -3.0	2.9 2.0 3.0	2.5 .5 1.9	.6 8.3 .6 -1.8	1.9 8.0 8.8	2.6 6 .8 1.0	1.2 .8 8.4 .8	2.6 .6 1.5 2.2	1.0 .0 -1.8 -2.0	1.8 1 -8.8 -1.4	1.7 -2.3 8.5 8.6	1.8 -8.6 1.4 -1.0	-2.6 -1.6 -8.1 1.6
.9 -1.8 -2 2.4	.8 2.0 -2.1 1.0	8.1 .4 8.5 1.7	.2 1.0 3.9 5.0	-1.0 4 2.6 1.5	2.5 7 1.1	.0 2.6 2.6	6 1.4 1.0	4 1.5 2.5 -1.0	.2 7 -4 -2.0	9 -1.6 8.0 6	-1.8 1.0 2.6	-1.5 -1.5 8.0 -1.0	-1.2 .9 3.0 2.7	7 .7 .0	2.7 2.1 2.6 1.8	.4 -1.9 8.8 8.6	.1 1.6 9 -1.6	-1.0 8 1.7 8.0	-8,7 8,6 ,2 -4	1.0 .9 -2.8	1 0 -1.5	.: -:: 1:3	2.1 1.0 -2.0 -,8	8 -2.5 -1.0 -8.0
-1.6 8 8.5 -2.7	-2.3 .2 1 2.6	1.0 1.2 -2.7	1.7 -8.6 1.0	-1.9 -8.2 2.8 1.3	-2.7 2.9 2.9 1.1	-1.6 1.5 -1.1 8.4	.9 -1.3 8.1 -1.0	.2 -1.5 -2.0	2.0 -2.0 3.5	-2.9 4 1.4 -2.7	-8.0 1.9 -1.6 1.6	-2.8 -1.5 -2.8 1.9	1.8 .9 -8.4	2.2 1.5 -1.2 -2.2	2 2.0 1.0 6	\$.0 -8.0 .1	2.8 -2.8 -1.9 -1.7	1.8 -8.4 -2.9 1.7	-1.6 -2.8 2.7 2.1	-1.4 -2.9 9 -8.1	7 -1.8 -1.8	-2.7 2.0 1.1	1.7 -2.5 1.8 8.0	1.8 8.4 1 -1.4
-1.8 -2.5 8.7 2.4	1 -1.4 -1.9 2.7	8 2.0 .2	1.0 9.3 .4	8 1.4 .8 -1.6	2.6 1.1 1.1	-1.7 1.6 2.6 -1.1	1.6 -1.9 1.8	-2.9 2.7 -2.9 2.8	-8.0 8.0 -1.7	5 -1.2 2.6 -1.1	-2.2 .6 2.2	-2.6 8.5 2.5 -2.4	-8.8 -3.0 -1.9	8.5 8.2 -1.5 -1.0	.3 -:1 -2:1 2:6	2.6 3 -1.8 2.3	1.8 -8.6 1 1	-1.8 2.4 -1.5 -1.8	1.5 8 -1.6 -1.0	-3.0 -8.6 5 2.6	1.7 -8.4 1 2.0	8.0 -1.5 -4 -2.5	.7 -8.4 .8 1.6	.8 .8.6 .8.8
8 -2.9 1.1	2.0 1.8 -1.6	-2.8 -1.8 1.9	-1.0 -2.5 -2.7	-:5	.1 .2 2.2	8.3 6 -1.6 1.7	-1.5 .6 -8.7	.7 .2 9	.2 6 4 -2.1	1.8 1 2.8 -2.0	2.3 8.0 2.9 2.1	3.0 -1.3 -2.6	2.0 4 2.7	-2.2 .4 -2.5 -2.6	-1.0 -1.2 .7	.6 -1.9 8 6	8 6 1 1.6	2.0 -2.1 .9	3 2.7 -2.0	.6 -1.9 -1.8 1.8	1.6 1.8 6	8.8 -1.7 -8.9 8	: 4 : .	1.7 1.8 1.8
1.9	-3.7	2.0	2.6 1.9 -2.9	4 1.9 -8.7	-1.4 -2.3 0 -2.1	2.4 1.1 -1.8	-8.7 .2 -2.1	1.8 1.6 1.4	.5 1.6 -2.0	-2.2 -8.0 -2.6	2 -1.5 1.5	8 .5 1.0	1.8 2.5 2.9	2.9 2.9 -1.6	8.7 -1.8 -8.8 -2.0	1.6 .3 6	1.8 2.0 1.1	2.0 -2.6 -1.8	2.0 1.7 1.5	7 7 4	-8.9 -1.0 .0	4 8.4 .6 1.8	-1.6 1.1 .8	-8.0 8 1.8 1.6
-2.1	-1.0	-1.8 -1.8 -3.4	-1.5	1.8	8 -1.8 8.1	1.9	1.1 .3 -2.5	8 8 6	3.0 1.9 2.4	-8.6 1.8 3.0	2.2 -2.8 -1.7	-2.8 -1.6 -8.7	0 8.5 -2.1	.; .; 1.7	-1.6 8.5 -2.6 2.5	1.6 -8.8 1.4 8.0	-8.1 -8.4 4 -1.6	1.6 7 8.7 -1.6	1.0 1.8 2.6	-1.8 -1.1 -8.0 8.7	8 1.7 .4 -1.7	9 -8.4 -1.0 1	-1.6 8.7 .8	2.0 1.0 -2.9 -1.2
a. 2.	-2.	-2.0	1	2.9	2.0	.8 8.8 -3.0	-2.4 1.7 6	-3.1 -2.8 2.6	.4 3 2.9 -2.8	-8.0 -2.2 2.2	.1 1.2 -1.7	-2.6 1.4 -2.6 -2.0	-8.3	1.0 2.0 -3.8 3.7	2.0 -1.0 -2.0	2.5 -1.8 .9	-8.0 -1.9 -3.0 2.2	-1.1 6 .3	-2.4 -2.8 -1.5 -2.1	-8.8 -1.6 -1.1 8.1	-2.0 .8 1.8 3.0	1.9 -1.7 -6 -1.0	1.1 8.8 8 1.6	-8.7 8.8 -1.4 .1
1:	5 1. 6 1.	-8.		1.0	8.0	-3.7	2.1 -3.0 -2.4 -1.8	1.9 1.5	-1.5 1.2 1.7	1.5	1.8 2.0 3.0	-:}	.2	.5 1.8 1.0 8.6	-1.7 -1.9 1.0	.8 -2.2 1.1 -1.1	1.8 -1.5 1.6 .5	8 -1.9 9	-8.0 1.8 8.8 -1.6	2.2 -1.0 .5 2.0	1.3 -2.0 .9 -3.8	-1.8 8 1.1 1.9	.7 -1.8 -2.8	.4 1 1.8 7

Table B.—Drawings from Rectangular Universe—(Continued)

						,																		
-2.0 1 -6 -2.5	2.0 -1.8 -2.9	-2.4 1.9 5	-1.7 2.2 .6 2.9	4 -2.7 1 -1.7	2.8 -2.9 1.7	2.8 -1.5 2.0 2.2	-1.2 1 -2.7	-3.0 -1.2 1 3.0	1.5 -2.2 1.5	-1.4 9 7 -1.1	-2.0 .8 -2.7 2.5	.3 2.3 .7 -1.4	1.5 -2.7 1.5 2	-2.7 -:4 -3.0 -1.1	-1.4 1.7 .1 1.0	1.3 -2.6 -1.2	1.7 -1.2 -3.0	1.2 -2.3 .9 2.1	1.1 -1.0 -1.1 2.0	2.9 2.4 -1.1 4	1.0 2.2 1 4	-1.9 1.9 2.7 1.7	-3.0 3 1.4 1.6	-2.6 -2.8 -1.3
1.4 5.0 1.3 3.0	-3.0 -2.4 -2.0	6 -2.4 -1.7 -3.0	-1.4 5 0 -2.5	1.3 1.5 .2 -2.0	-2.9 2.0 2.5 -2.0	-1.0 -1.3 -1.6 2.7	1.3 1.9 -1.3 1.7	-1.0 -1.3 1.1	6 1.8 2.6	8 1.9 1.3 -1.2	9 2.1 1.9 1.6	2.8 2.9 -1.9 2.4	7 .3 .5 -1.3	2.0 .7 0	1.6 -2.1 2.8	8	1.8 2.2 	-1.1 2 9 2.6	2.9 1.6 1.6	2.4 -2.4 .2	6 -1.1 1.4	2.8 .6 1.8 1.7	5 -2.1 7 -2.6	2.7 -2.9 -1.1 2.0
0 2 -1.6 1.7	-1.5 2.1 1.5 -1.4	-1.1 .6 -1.2 7	-2.4 -1.0 9 2.9	1.7 0 -2.9 3.0	1 2 1	.6 2.3 3.0 1.3	.9 .1 -2.5 9	1.1 -2.8 -2.3 2.2	1.7 -2.7 -1.8	1.9 -1.3 1.0 -2.4	-1.6 7 -2.5 -2.4	-3.9 4 1.5 2.2	2.0 1 1.2 7	2.5 2.5 8	-1.7 3 -1.2 1	-1.3 6 2.9	2.7 1.2 .3	-1.6 2.5 -1.8 1.4	2.1 1.1 9 1.8	2.1 -1.5 -2.9 -1.5	2.9 -1.5 .8 £	2.5 1.4 .9	8 -2.5 1.6 2.5	-2.7 .5 1.2 4
-1.7 1.2 .7 1.7	6 2.1 .8 -1.4	-2.0	-2.1 3 1.8 2.7	3 -2.1 .1 3	-2.2 -2.5 -2.4 -3.0	1.9 3 .9 2	8 -1.9 2.0 -2.7	.9 .3 2.5 3.0	3.0 2.7 -2.4 -1.3	7 5 -1.3 9	1.6 2.6 -2.4 -1.6	9 .6 1.4 1.3	-1.7 2.5 1.8 2.0	.9 -2.5 3.7 2.5	2.6 .4 2.2 -1.1	1.6 -1.0 -1.7 2.6	2.6 -1.5 2.3 -1.1	.5 -1.0 .8	2.1 1.7 -1.0	2.8 4 3	-2.5 1.9 -1.3 8	5 1.3 .1 1.7	-2.9 1 2.8 -1.4	2.5 2.3 1.8 -2.9
-1.0 -2.1 -1.1 1.2	2.1 1.3 2.5	7 -1.4 .5 1.9	2.8 .4 1.9 -1.7	-1.9 -2.8 1.3 2.7	1.6 -1.2 .6 -2.6	-1.3 3 -1.3 1.4	1.5 .8 -2.5 -2.4	.5 -2.1 -2.3 7	3 .6 -2.7 2.9	.1 .4 2.6 1.3	2.9 1.1 .7 2.3	0 1.6 -1.1	7 -2.8 2.2 -1.6	4 5 -2.3	5 1 -1.1	7 .4 -2.9 -1.4	-2.8 -2.9 -0 -2.6	.4 2.6 .4 2.2	-2.5 -1.0 1.1	-2.8 2 .3	-2.2 -2.5 -2.0	1.0 1.7 1.3 2.9	5 -1.7 1.4 1.6	-3.0 4 1.5 2.4
1.8 -2.7 2.2 2.2	2.0 2.9 -1.0 -2.3	.5 -2.1 -2.6 7	-1.4 7 8 -2.9	2.7 8 7 -2.1	-1.4 2 -1.9 -2.2	-1.7 2.1 6 -2,6	-1.3 6 -2.9 1.4	-5.0 .9 -1.8 6	1.6 5 -2.3	.5 7 -1.9 -2.1	-1.8 -1.4 -2.6 -1.3	5 8 .6	-2.7 1 2.5 2.6	1.9 2.7 1.3 -2.8	2.7 2.8 -2.4 -1.9	1.2 1.2 -2.8 -1.9	-2.7 2.5 -2.5 8	2.8 -2.3 1.5 3.0	1.9 1.6 2.2	2.5 -2.1 -1.9 -7.4	1.7 1.6 3.0 -2.1	1 -2.0 1.2 -2.2	-1.6 .9 -2.8 -2.1	-2.1 -1.4 .9 2.5
.2 5 2.4 1.4	1.6 .7 1.5 -1.3	2.5 -1.5 .4 -2.2	1.2 .1 .9 8	0 -2.9 1 3	7 9 2.1	-2.1 2.4 .7 2.6	2.9 -2.7 2.9 2.1	-2.6 1.6 1 -2.9	-2.0 -1.4 1.4 -2.5	.5 .1 1.8	-3.0 2.6 1.9 1.7	.6 -2.6 1.3 -1.9	2.6 -2.1 9	-1.3 -1.0 -2.1 2.7	-1.9 1.6 -2.5	-1.5 2.0 2.6 2.6	-2.1 9 2.1 2.5	2.0 2.6 2.1	-1.2 1.5 -2.1 2.2	.3 -1.1 -2.8 .3	.1 2 2.3	-1.8 8 3 -2.7	-1.4 -2.0 2.3	2.6 2 -2.3 -1.4
7 1.4 -2.5 -1.0	-2.5 .6 2.5 -1.5		4 -1.4 1.2 5	8 4 -1.4 -2.2	2.1 .5 -2.6 -1.4	7 2.0 -2.6 2.8	.2 2 -2.7 -2.6	-1.5 .5 2.0 1.9	-3.0 -2.1 1.8 -2.6	2.8 6 -2.6 1.6	-2.1 4 -2.2 -1.1	-1.4 -1.0 .2 1.7	-1.1 -2.1 -1.1	-2.5 1.2 -1.1 -1.9	-1.7 2.6 -2.2	.2 .8 -2.6 -1.8	.2 1.8 8	4 2.4 -2.3 1.2	2.5 -1.0 -3.0 1.0	2.5 -2.5 9 2.0	.5 1.7 1.5 -1.6	9 .2 9	-1.9 -2.4 .2 -1.6	2.5 1.1 -3.0 2.4
.6 2.2 5	-2.6 -2.7 6 -1.0	-2.2 -2.7 1 -2.5	-2.0 7 -2.2 3	.7 -3.0 0 -1.4	.5 -1.1 -2.2 .7	1.5 -1.1 1.2 -1.1	.6 -1.6 1.8 2.2	2.2 -2.9 1.5	-1.0 .6 -2.1 2.4	-2.0 -1.5 -1.0 -2.1	1.4 2.6 -0.4 -2.4	.4 4 .5 1.5	2.7 -1.5 3.0 2.8	.1 1.7 .4 -1.6	.9 .8 -1.4	-1.4 1.6 1.7 1.3	2 9 -6 -3.0	-2.0 .1 .7 1.8	2.4 2.6 1.3 2.4	-1.7 2.9 3 1.2	-1.9 1.5 2.8 -1.7	2.0 -2.5 2.5 1.9	4 -1.6 2.0	.2 1.9 .2 2.9
1.0 -1.4 2 -2.9	.6 2.1 1.7 4	5 -3.0 1.9 ~1.6	2.5 2.6 1.7 -1.1	2.3 -1.9 1.6 2	.4 -1.5 2.5 1.9	1.0 2.1 1.3 1.0	1.9 -2.6 -2.7 -2.3	2,4 -2.0 5	1.5 -1.9 .5 1.5	2 -1.0 1.2 1.5	1.7 -1.4 -1.9 -1.6	8 9 1.3 1.7	1.7 9 -1.6 1.8	-3.0 -1.1 -2.£ 1.2	-1.6 1.8 3.0 1.2	-2.2 1.7 -1.5 2.3	.7 -2.4 2.7	-1.8 9 -2.6 -1.3	-2.0 3 1.7 -£.7	2.0 1.1 3.0 -2.9	-2.5 -6 -1.0 -2.8	2.7 1.0 -1.5 1.1	-1.0 -3.0 2.9 1	1.1 2 .5

2.0	1.0	1.4	8.1	1.4	1	8.8	1.8	-8.8	8.8	1.6	4	-8.0	-8.1	8.3	-2.2	8.8	1.0	-1.6	-1.6	-4	.,	6	8.0	8
1::	-1.8 -8.0	8 8	.0	-3.2 3 8	2 .4 3.5	.5 -1.6	-1.0 0 -0.1	-1.0 8	1.0 -1.0	-1.6 3 8.8	1.2	2.7 -1.1	2 <b>?</b> ?	-1.8 1.6 0	.6 .9 -1.2	-1.4 -1.4 -1.4	-8.0 8.2 8.7	1.6 -1.4 8.7	4.5	-8.6	-8.4 -1.6	-8.8 -8.8 -1.1	1.1	1.8
-2.6 4 -3.7 -1.9	-1.4 -1.9 8 -1.8	-2.7 -2.1 1.0	-1.6 -1.8 -1.2	1.3 1.1 -1.5 8.1	-8.0 2.5 2.1 -1.6	8 0 4	-8.4 .5 -1.9	6 1.7 -8.9	-2.5 -2.9 2.0 -2.1	-1.8 1.2 .9	-1.4 .3 .3 -2.7	.0 1.0 -1.5 -1.7	2.0 8 -8.8 -8.9	1.8 8.8 -1.6 8.1	1.4 -2.1 1.9	-1.6 1.5 -1.8 8,1	-:1 8:4 -1:1 -1:0	-3.0 -1.9 1.4	8.0 -8.6 4	9 3 7 3	-9.5 -5.5 -8.1	1.0 -8.1 -1.0	-2.0 8.0 -1.8	-1.9 -2.0 -1.8 -1.6
0 -1.0 -2.3	6 2.1 .7 5.0	2.6 8.0 -1.4	1.1 .4 -1.2	2.1 2.6 1.1	1.9 4 -8.6	.8 -8.0 1.8	8.5 8.0 .2 -1.7	8 1.8 -1.9	-1.4 .8 1.7	-1.8 -8.1 -1.6	\$.1 -1.9 -1.1	8 .5	-8.2 9 -2.6	.8 1.7 2 2.0	0 2.5 1.4	1.4 -2.5 -8.0	-8.0 -1.4 -8.0	3	1 -8.1 8.2	8.8 -8.9 -1.0	-1.0 2.0	.0 4 -1.1	1.8	2.0 .8 1.3
-2.6 -2.6 .2 -2.8	8 -1.8 -1.8 1.8	1.0 .8 8	.6 -8.5 -8.0 -2.5	2.5 -2.7 2.3 3.0	.1 1.9 -8.8 -1.9	2.5 1.0 -8.0 -2.5	1.0 -1.6 -2.9 -2.4	-8.2 -1.9 -8.7	2.5 -1.5 1.0	6 .7 a.7	-1.1 0 .3 -8.0	1.4 -2.8 -1.4 1.8	2.5 -2.5 -1.6	.9 1.4 .6 1.8	1.1 8 -1.0	5 -1.6 -1.0	-2.1 2.6 2.3	-1.8 -1.1 .1	1.8 -1.6 -1.1 -1.8	2.0 -1.1 1.6	1.3 -1.2 -2.5 2.3	7 -8.8 -2.4	-1.3 2.4 2.8 2.4	1.6 8 6
6 2.0 .9	-8.4 -2,1 8.0	2.2 .1 1.8 1.2	-2.6 -2.7 -1.1	-8.7 9 8.9	1.8 -3.9 -2.8 -2.3	2.8 2 2.9 -2.0	-1.6 -2.3 -8.6	1.4 -1.6 .6	-1.6 1.1 3.9 8.4	2 2.0 -2.6	1.6 1 -1.1 5	.7 -8.0 -1.0	.3 -1 -3.0	-1.7 5 .0	-2.9 -1.1 1.7 -1.6	8.0 -8.8 -2.5	-1.8 8.6 .3 -2.9	2.8 7 1.8 -2.6	.6 2.0 -1.2 -2.7	8 9 -1.8	-1.8 0 1.7 -8.7	-2.0 .4 -1.8	2.5 1.0 2.6	2.8 3.6 8
-2.5 1.8 1.6 1.1	1.2	1 -1.0 -1.1	.7 .5 0	.6 -8.9 .9 1.0	2.7 2.4 2.6 -2.0	1 1.5 1.0	.6 .3 -1.6 -1.3	-1.9 -8.0 2.3	-8.5 4 -1.2 -1.5	.2 -2.7 1.8 1.1	-8.6 8 -1.5	1.1 -2.6 1.4	-1.7 -1.8 1.9 2.5	1.2 -1.2 7 -8.6	8,0 8.0 1.3	-1.3 2.7 -1.3 -2.8	2.0 2.0 1.6 -8.7	8 -1.1 -1.4 .8	-1.1 -1.9 1	-1.4 -2.4 .6	.6 1.1 -1.8 1.0	0 -1.8 -8.2 -2.0	-1.9 -8.0 -8.7	-1.0 1.4 1.8 3.0
.8 8.9 .6 1.9	-1.0	2.0 1.4 1.0	1.7 8.0 2.2 -2.1	-1.1 1.3 -1.0	1.0 1.4 2.7	-1.6 -2.5 8 -2.6	1.4 -1.6 -2.4 7	-2.9 1.8 1.3	-1.1 2.9 1.6 3.6	-2.7 -1.6 7 -1.6	8.4 2.2 .0	-1.6 3 -2.6 -2.2	-1.8 -5.0 -2.4 -2.9	-1.2 -2.9 .8	-2.1 1.0 1.1 -8.1	8.0 1.9 -2.0 2.7	.8 8 -2.3 -2.5	1.4 -2.9 .8 -8.0	1 -2.9 -1.6	.6 2.5 2.8	.5 .7 2.2 2.5	-1.7 -2.0 -1.4 5	8 -2.9 -2.6 -1.7	1.7 -2.0 1.0 1.0
6 -1.0 .8		1.8	2.5 2 2.5		-1.5 -2.9 -1.0 2.0	.6 -1.1 -1.6 8	-1.5 1.2 6 8.0	-2.5 1.4 7 8.0	5 1 1.2 1.5	2.7 -3.0 9 -3.0	-2.6 -1.9 2.1 -1.1	0 1.1 ,6	-2.5 1.2 -2.5 -2.9	3 2.8 -2.0 -2.4	-1.8 -1.8 3.0 -1.8	.6 -2.4 -1.2 2.4	-1.0 -1.3 2 2	-1.0 .8 1.1 8	2.7 8 -2.2 -1.0	2.9 1.7 1.4 1.5	-3.0 2 3.0 -1.2	.5 4 2 -8.0	-8.9 8.0 1.6 8	.4 9 -3.0
1.1	2.8	-8.8	2.2	-2.0	8 2 1.4	1.0 -1.6 2.0 -1.6	2.6 4 -1.0	.1 1.2 2 1.2	-2.3 2.8 -1.5 0	4 -1.6 -1.6	2.9 1.8 -1.5 -2.5	1.0 1 .4 8	.5 1.8 1.2	2.8 -1.6 2.1	2.7 3 -2.1 -1.6	-2.0 .1 -1.6 3.0	-2.0 -1.7 8.1 -1.4	-1.8 .6 4	1.0 1 -1.6	6 -1.5 6 E.4	1.8 -1.8 8.7	-2.4 -1.0 1.5 1.5	-1.8 -1.6 -2.0 -8.6	-2.6 3.0 1.6 9
-1. -1. -2.	1	-2.5	1.5	-2.0	-2.4	-1.8 3.0 2.4 -2.4	-1.7	1.8 1.4 1.4	-2.7	1.8 -1.1 3 .6	3.9 -1.0 7 .3	5.0 .0 8.7 3	-1.6 1.4 -1.6 -1.0	3.0 -1.8 -1.4 8	1.2 4 -2.1 -1.1	-3.0 5 .1 2.6	.1 -2.2 8.9 8.4	.2 4 -8.4 2.7	-1.8 8.6 -1.4 1	1.1 1.4 1.2 9	-1.8 .1 -1.4 1	1.0 -1.1 1.5 -8.5	-1.8 -1.8 .8 8	0 .9 -1.9

TABLE C.—DRAWINGS FROM RIGHT TRIANGULAR UNIVERSE

						LABL	E C,	ע	KA W	INGS	FRO	M K	GHT	I RI	ANG	ULAR	Un	IVER	SE					
-1.1 1 2 1.4	1.7 8 0	.1 4 6 1.9	.1 -1.1 1.4 7	.7 5 .6 2.0	8 1.7 3	.8 8 1 -1.7	1.4 .6 -1.1 7	-1.1 7 1.4 .2	1.3 -1.3 4 1.2	2 -1.2 .5 1.4	6 .5 1.4 -1.2	1.5 .6 -1.0 -1.1	1 .5 3 1.6	-1.0 1.4 -1.2	-1.0 8 .3 1.6	-1.0 1.5 .2 -1.1	-1.1 .3 6	.1 .5 -1.0	7 .9 .9	.4 .7 8	.2 2 .4 -1.1	.6 .5 .7	.3 .2 .4 -1.1	1.2 1.0 2 1.3
.5 0 .4 -1.0	.1 .7 .6 8	.5 8 -1.0 0	0 .5 1.0 1.5	.2 -1.2 -1.3 3	.5 1.3 .9	1.2 .5 3	.5 6 .2 .9	7 .4 .8	0 0 .4 -1.1	7 .4 -1.1 0	.7 -1.1 1.4 6	1.9 6 .5	.1 .3 1.7 8	-1.3 1.2 2 -1.E	-1.5 .7 1.1 1.3	1.3 1.5 5 -1.1	.3 1.4 .9 -1.2	1.8 1.5 8 7	-1.1 1.3 .8 -1.5	1.8 6 1.5	1.9 1.4 .6 7	1 1.0 -1.1 1.5	0 1.5 2.0 6	-1.0 1.3 1.6 -1.0
1.6 -1.0 3 1.3	1.5 -1.1 -5	-1.5 .3 1.3 .3	.1 -1.0 .6 1.6	1.2 1.7 1.4	.6 -1.2 4 4	-1.1 -1.1 -1.0 1.5	- 3 a 4 a	-1.5 -1.1 1.3 -1.5	6 1.4 8 -1.2	1.6 -1.0 5 8	.3 1 1.2	9 -1.2 1 8	1.0 .1 5 0	-1.0 9 5	-1.1 .9 -1.1 1.5	2.3 1.7 3 .2	-1.1 1.5 .4 6	2.2 1.1 .2 4	-1.2 1 1.4 .7	.7 5 1.4 -1.2	? .7 1.4 -1.2	-1.3 -1.1 1 1.5	1.5 0 6 -1.1	-1.0 -1.3 -,2 1.3
6 .8 -1.5 1.4	.1 8 1.5 2.1	6 1.2 .4 2.5	2.0 9 .7 1.3	1.0	1.0 -1.2 1.7	3 1.4 2.1 8	2.3 5 0 1.6	-1.1 1.8 .8 3	.1 6 -1.2 1.7	.7 -1.0 1.1 1.9	2.0	8 -1.2 1.7	6 4 -1.1 1.8	6 -1.3 1.6	1.9 6 -1.0	4 6 2.3 1	2.2	1 -1.1 4 1.8	-1.0 5 1.9 0	-1.2 -1.2 1.7	1.7 -1.2 6	1.0 1.8 -1.1	-1.3 1.6 -1.0 5	1.9 2 -1.0 -1.0
1.5 .1 .1	.5 .5 .3 -1.1	.2 1 -1.2 .2	.6 6 8	1.0 9 0	.7 .8 6 4	9.000	3 22 7 -1.0	0585	1 1 i	2 .7 8 6	1.9 .4 -1.0	4.00	6 .1 -1.3 3	1.0	-1.1 -4 -3	.5 -1.1 .1 .2	1 .1 -1.5	1.6 .4 1.3 1.8	.1 1 5 -1.5	5450	.6 9 7 4	1.0055	.1 .5 -1.0	.1 1.4 .4
-1.0 -1.2 -1.0	-1.0 7 9 .3	7 4 .6	0 -1.1 6 -1.5	.1 1.4 .5	5 .4 1.0 2	-1.1 2 8	-1.1 -1.3 9	.5 6 4 -1.8		-1.0 3 -1.1	8 8 7	.5 6 -1.2	-1.0 .2 1 5		1 1.2 1 0	2.1 .4 5	-1.0 1 7 1.6	-1.1 1.5 6	1.6 2 -1.0	-1.2 -1.5 -1.5	4 1.4 -1.1 -1.8	-1.8 1.4 4	1.4 -1.2 -1.1	E -1.7 6 9
.6 -1.8 8 -1.1	.7 0 1.2 .5	1 -1.3 6	.2 .5 9	.5 8 .4 1	4 -1.5 2 1	7 5 6	5 -1.5 1 -1.0	.9 .2 1.1 1	4 7 -1.0 -3	9 .8 1.2	2 2 2	1.4 1.1 .5	.4 -1.8 -1.2 4	-1.2 5 1	-1.1 0 4	1 7 1 -1.8	40.5	1 -1.2 5 7	7 .4 1	1.1 1 6	-1.5 2 -1.0 4	-,7 -,3 -,8	4 2 -1.2 -1.3	0 -,2 -1.1 -1.0
1 -1.1 5 -1.8	.2 0 6	.8 .5 4	-1.0 5 8	1 6 6 -1.3	8 4 1	.2 .5 1.2 8.2	1.0 1.1 .5 -1.2	-1.5 -1.5 .7 1.5	-1.0 1 1.5 -1.1	-1.2 8 .6 1.5	6 -1.3 1.6 1.0	.8 1.7 1.1 -1.0	-1.5 -4 8 -2	8 8 2	1 .6 7 2	.3 1 -1.0 2	1.7 2.5 1.0 7	8 -1.1 1.9 -1.0	-1.5 8 -1.1 -1.0	-1.2 2.3 -1.1 9	4 5 7	-1.1 1.3 0 8	1 1.9 4 2	1.5 -1.0 8 1.1
4 .3 .6 1.5	4 -1.0 .9	-1.0 4 4	1 3 1.4 .5	4 9 .5 -1.2	6 1.1 1.2 0	-1.0 4 .8	.9 9 8	.9 9 5	8 2 1.0	1.0 9 .2 .7	.1 1.0 9 .1	-1.3 -1.2 3	-1.5 8 7 .6	.5 .4 1.8	.5 -1.1 -1.3 -1.1	8 7 .9 9	2 3 3 1.5	6 -8 -1.0 -1.2	.9 9 7 3	6 3 0 1.2	1.1 3 8 1	2 1 -1.2 -7	2.0 1.0 .1 1.2	5 1 -1.2 -7
.2 9 1.0 4	.8 9 1.0 7	.8 9 0 -1.1	2 -1.0 0	1.0 9 .1 5	.4 5 .9 -1.0	-1.2 .7 -1.2 .2	-1.0 -1.2 -2	4 .6 -1.3	1.1 .3 1.5 4	2 -1.0 .5	.6 1.7 .2 2.1	.8 -1.1 7 4	0 1.4 5 1.0	.9 5 -1.0	-1.3 .4 .3 .2	-1.2 -5	-1.1 .5 .5	\$ 9 0 C	-1.0 2 .7	7 1 .4 -1.3	.4 -1.5 7 1	7 -1.2 .5 0	9 8 8	.4 8 6
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	_								_												•		_	
	4.5.5	90.00	-1.0 .1 .8	1.8 1.7 -,1	1.4 .8 1.9	1.1 .6 7	.8 -1.5 8 -1	.6 .2 -1.8 6	-1.1 -1.1	.6 6 -1.1	-; -; -; -;	., ., ., .,	-1.0 .9 1	-1.1 -2.1	5 -1.8 -4 -6	-1.3 -1.3 -1.6	-1.0 .a .9	1.0 .8 1	.4 8 1.7 1.8	1.3	1.0 7 8	3 .9 6	1-1 0 ,7	1556
	.1 .6 5 1.8	0 1 -1.8	9 -1.1 -7	1.1 .4 6	-1.1 .7 6 -1.0	4 4 5 6		1.6 3 .0	.6 1.8 1.8	.6 -1.8 -:4	* 1 -8 -1.0	4 -1.8 -1.1	.9 4 5	.8 1.6 1.6	-1.8 -0.0 -0.0	.9 6 .5 1.8	1.8 1.5 1.2	1.0 4		1.9 8.2 .8	1.4 1.1 4 2	-1.1 8 4	1.8 .8 6 1	4 6 6 6
.8 8 1	-1.8 8 -4 -1.0	4 .7 0 1.8	7 .9 .3	-1.0 -5 -1.2	8 .1 5	3 .4 6 -1.8	9.54.5	.8 2 0 1.5	5 .2 6		9 .8 .1 8	4 4 1.0	5 1 1.4 8	.8 -1.2 -1.0 -1.0	-1.0 7 -1.8	.6 6 -1.1	-1.8 .4 -1.1 0	6 -1.1 6	-1.8 4 5	.8 -:4 :3 1.8	1 8 -1.8	3 1 -1.1	.4 .4 .1 -1.2	:::::
1.8 .5 4 1.8	.4 -1.3 .4 -1.1	-1.0 .4 .4 -1.8	-1.1 .5 .5		.5 .5 -1.1	.8 .4 -1.1 \$	.5 -1.8 -4 -,8	.1 1 -1.0	6 1 .5 1.0	.7 -:4 1:8 -:8	.5 1.0 .5 1.4	1 .4 -1.8 -1.0	.7 0 1.6 1.8	.3 1 6 -1.5	.6 .8 5 -1.0	.6 -1.0 4	.8 4 4	9 7 .3 -1.8	-:8	4 -6 -1.0	.7 .1 9	1.1 1.7 .1	-1.0 -1.0 8	-1.3 -2.4
.8 .7 -1.0	-1.8 .8 .1 8	.5 2 -1.8 -1	.7 3 -1.0	8 .7 .3 -1.0	1.8 1.0 8	6 -1.2 8	-1.8 6 7	-1.2 -1.1 .5 5	.8 8 1.2 5	1 6 5	.2 .5 7	.8 1 7	-:0	1.8 .8 1.8	5 -1.0 8	1 6 3 -1.1	6 8,- 0	.1 4 7	.1 9 2	8 1.1 5	1.7 .2 .4	1.0 5 6	1.8 2 .1 3	-:8 :0 :1 1:6
-1.1 .5 4	0	1.5 1	.5 1.8 1.6	1.1 .8 1.1	.4 .5 1	4 -1.0 0 1	5 9 -1.5 4	.2 8 7	1 4 6	.6 1.6 1.1	.4 .8 1.0	-1.2 6 2 -1.0	.1 1.1 .4	.8 1 .6 4	.8 0 	.8 1.3 .8	-:1 -:7 -1:1	5 -1.1 -1.5 9	-: 6 -: 9	.6 1.4 .5	-1.1 0 -1.0 1	3 -1.3 -1.2 -1.8	-1.1 1 -1.0	1 .0 1.0
2.5 5 5	8 2.3 1 1.9	5 4 1.5 2.6	1.8 0 -1.8	.0 4 1.7 -1.5	1.8 -1.8 -4	1.0 .4 -1.8	.8 -1.1 1.9 9	-1.3 6 1.7	5 4 1.6 2.6	-1.0 -1.1 -1.3 -1.1	6 6 6	6 7 5	.8	8.E 6 1.0 2.4	1 -1.8 1.7 1.6	-1.0 3 1.5	.1 2.0 -1.0 1.6	1.7 .5 8.1 9	2.0 1.5 8.4		8 4 7 4	1 3 4 5	.4 .1 .8	7 -1.1 -1.1
1.0 .8 1.8		8 -1.0 6 8	1 0 3	8 9 7	.9 -1.2 .6 8.0	7.0 -1.2 1.3 3	.2 -1.2 2.0	8 1.6 7 8.4	5 6 6	8 6 6	-1.0 -1.0 8	.1 2 3 3	8 4 9	8 7 3 6	5 0 1.9 -1.2	8 .4 2.3 2	-1.1 6 8.0	1.9 1 6 -1.8	2.5 -: 5 -: 5	-1.3 -1.2 1.8 2	-1.8 -1.3 5 1.8	2.1 .2 .8 -1.0	6 -1.3 1.7 1.9	8.1 1.9 1.0 -1.1
.6 .5 1.8	1	9 .1 7 -1.0	-1.5 8 -1.0 -1.1	8 8 6	3 2 1 .8	-1.1 -,8 .1	1.8 1.8 .1	.4 8 7	1 -1.3 -1.5 1	1.8 1.8 .7	8 4 1	7 -1.1 5 8	6 1 8	0 7 -1.8 -1.2	-1.1 8 -1.1 -1.2	4 -1.0 9	9 -1.0 7 4	9 6 -1.2 -1.2	.2 6 .6 3	2 -1.0 8 6	.4 1.1 .8 1.1	6 .1 5	.8 .6 .6	3 7 1 0
1.5 1.5 1.1	:	:	-:8	1.0		-1.0 6 8 -1.0	8 1 0	1 0 5 8	9 2 8 1	.7 .5 0	.1 .8 .3	6 -1.1 4 -1.2	6 3 8 -1.1	.4 1	5	1 .5 4 2	7 6 8	0 7 7 9	-1.1 -1.0 5 -1.2	4 3 4 .5	6 4	.5 5	4 4 -1.2 -1.8	2 6 -1.0 6

Table C.—Drawings from Right Triangular Universe.—(Continued)

1.1 1.2 4 -1,2	1.8 -1.0 -1.1 1.8	1.7 1 1.6 6	1.8 1.5 6 4	1.8 1.3 .6 6	8 1.6 .5 1.2	1.1 9 .7 -1.5	2.0 .2 1.6 4	1.4 -1.0 3 1.0	9 6 1.2 1.5	-1.8 1.1 8	8 0 1.6 1.3	.8 1.5 9 .8	6 -1.3 1.1	0 1.1 5 -1.3	.5 -1.8 1.1	.5 -1.8 5 1.2	.5 -1.2 1.2 6	-1.0 1.4 .7 8	0 2.4 1.0	1.2 .2 .4 2.6	-1.0 1 2 1.4	-1.2 9 5 1.8	1.5 0 9 5	8 1.6 7
1.1 -1.5 7 5	5 1.2 -1.8 9	1.4 .2 4 -1.0	0 1.2 -1.8 -1.1	-1.1 -1.1 .1 1.5	1.2 2.0 1.2	7 1.5 9 7	6 1.5 -1.1 -1.1	1.4 -1.0 5 6	2.0 0 4 3	1.2 9 -1.2 8	8 6 5 1.6	.2 5 -1.5 1.1	-1.1 .4 -1.0 1.3	-1.2 1.2 .5	6 1.8 .5	.5 1 1.8 6	-1.5 1.1 8 2	-1.8 7 .9 1.1	2.0 0 8 2.1	.4 .5 1.0 -1.5	5 -1.5 -5 0	1.1 6 .6 -1.2	1.0 1.4 9	1.2 8 .8 -1.1
.7 1.5 1.0 -1.0	1.0 -1.0 .4 1.8	1.6 8 7 1.5	-1.0 7 1.3	1.8 -1.1 -1.0	-1.0 .2 -1.1 1.2	9 .8 .1 1.4	-1.2 0 -2.3 -1.1	3 -1.3 1.0 1	5 .5 1.6 7	-1.3 1 1.0 1	1.1 .4 -1.8 0	.4 -1.8 .4 1.1	1.0 .3 5 -1.5	5 1.1 .4 -1.8	1.2 .5 9 -1.1	-1.3 1.0 7	9 6 0 1.4	8 1.4 1 9	1.4 1 4 9	5 -1.1 1.2 9	6 5 1.1 -1.2	-1.0 1.5 5	5 1.8 .2 5	-1.0 -1.0 1.3 4
-1.1 6 -1.0 1.8	1.7 6 8 1	5 6 1.5 4	1.6 .4 2 7	-1.0 1.3 -1.0	1.2 -1.0 -1.0 -1.1	-1.5 9 -1.1 1.0	1.0 1.5 5 7	.9 1.4 4 8	.4 -1.0 .8 1.2	.6 -1.2 1.0 6	.9 .6 -1.3 5	.6 -1.5 4	1.5 1 1.8 4	1.0 1 1.1 2.1	6 .6 .2 1.6	1.1 1 0 2.1	6 6 1.6	1 1.6 5 1.0	.5 1.8 4 1.8	1.1 1.7 3 5	1.5	8 .5 1.4 5	.5 1.0 .1 -1.2	7 .6 1.5 .8
-1.0 1 2 5	2 1 -1.0 5	5 .4 .5	6 -1.1 2.0 1.2	2.5 6 8 6	2.0 -1.1 8 5	.5 -1.2 1.8 1.0	1.7 +1.1 -1.0 -1.5	.5 4 .8	-1.1 1 .1 7	.8 4 .1	7 .5 5	5 5 .5 .7	1.1 -1.5 6 1.8	2.1 -1.0 -8	1 2.2 9	7 5 2.4	8 .6 2.3	0 1.8 -1.5	1.2 4 2.4 7	1.8 .8 1.0	1.9 -1.2 .7 1.1	-1.1 1.1 1.9 -1.2	1.7 5 .7	.8 1.8 .5 -1.0
1.4 8 .7	1.6 .9 1 6	5 1.1 -1.1 6	8 8 1.4 7	-1.1 5 1.1 6	.8 .1 .6 2.5	7 5 7 1.5	7 1.1 7 -1.1	8 -1.1 .6 -1.5	.6 2.4 .5	1.5 4 1 2	9 -1.3 -1.0	.1 3 5 1.6	8 -1.0 5	-1.1 -1.3 1.0 -1.1	-1.2 1.1 -1.0 2	.1 -1.0 1.0 -1.5	1.1 .8 -1.2 .1	-1.5 .9 .8	5 4 B Q	.6 1 4	8 2.1 6 1.2	1 6 8	-1.2 -1.2 1 5	4 0 8 .5
1.1 8 7 8	6 2.1 -1.0 1.4	5 .1 7 1	7 1 5	.1 .5 .7 1.5	-1.0 7 .5	5 2 7 -1.5	8 .5 .2 1	2 7 .4	5 0 7 -1.1	0 2 6 .5	1 -1.2 -1.1 6	: ::::::::::::::::::::::::::::::::::::	2 -1.1 -1.3 -1	.9 2.3 1.5	-1.0 6 -1.0	5 1 .9 4	8 7 .7	-1.0 -,2 .4 -1.0	-1.0 -1.0 -4 7	B 6 5 6	-1.0 5 7	-1.1 -1.0 -5	.2 .5 2 4	-1.0 4 9 1
6 .1 5 8	5 9 4 5 -	.1 4 2 -1.5	5 .6 .9	-,2 -1.0 .1	.5 .5 8	2 .1 -1.5 -1.0	.6 8 .3	4 -1.1 3 -1.8	1.2 .5 .7	7 .2 3 7	-1.0 8 4 -1.5	.1 5 4	* \$ -! a	5 -1.0 8 1	1.1 1.0 .0 1.5	-1.0 5 1 6	.1 4 5 8	-1.5 4 -1.2. -1.5	2 -1.1 8 2	2 -1.1 5 4	-1.2 3 5	1.6 1.4 1.4	.1 7 1 8	0 2.6 5
8 3 -1.2 1.0	9 1.4 1.4 2	1.8 1.8 3 -1.1	5 8 1.4 1.5	9 .9 .5 -1.2	1.1 0 -1.0 1	5 -1.1 1 1.0	-1.2 6 .0 2	4 .6 .2 1.7	.9 -1.2 5 2	0 -1.0 8 1.1	.6 8 1.5	.7 1.4 7 1	-1.5 .1 .8 -1.2	1.3 1 7 8	.5 1.8 3 1	1.5 0 5 6	-1.2 -1.5 8	9 1.2 4 8	.1 1.8 3 .2	1.5 0 .1 8	4 7 .2 1.4	4 .5 2 1.7	2.5 .4 1.3	5 5 .4 1.6
0 5 -1.5 .8	1.0 -1.0 .2 -1.1	-1.1 -1.3 -1.1 .8	8 1.6 3	.2 1.4 .7 0	0 7 1.4 .5	.1 1.0 -1.1 6	1 -1.5 .8 -1.0	7 5 .8 -1.5	-1.0 4 .9 -1.8	1.1 2 -1.0 8	1.3 5 9 1.1	1.5 1.3 6 1.5	1.4 1 2.0	2 .1.0 ^ 0 -1.1	1.6 1.0 5 1.3	.9 -1.2 9 .5	-1.2 .5 -1.2	2 -1.0 .7 1.1	1.7 1.3 1.8	-1.1 -5 5 1.0	1.1 1.2 .4 9	1.1 -1.0 1.0 .6	9 .6 .8 -1.5	5 6 1.5 1.5

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-:7 -:8 1:4 1:8	1.3 1.2 .8 8	1.4 8 8	6 -1.1	1.6	1.4 6 6	.0 3 -1.1	1 9 -1.5	.6 1.8 2.4	7 17 18	-1.1 0 7	.8 1.0 2.2	3.8 .2 .4	11, 11, 11, 11, 11, 11,	1.8 8 .5	6 6 1.1	:::::	- 4 - 1.0 1.0		7 1.3 -:4	1.3 7 8	-1.1 -1.1	1.0 8.0 .7	.5 1.8 .2 8	4444
6 8 .1	1.3 .8 7	9 0 1.1 1	.0 1.2 8	1.5 .9 .2	., 1.3 -1.5	-1.1 -1.1 .0	0 .2 0	l -l.l .9	-1.0 4 0	3 .9 1	4	0 7 1.1	.8 4 1.8	-1.1 .9 .8	9979	.2 1.8 3 1.7.	.1 1.1 .6	6	.8 -1.1 -1.2	****	4.8.8.8	1.6 1.6 1.6		1.0
-1.2 6 -1.2 8.0	-1.0 -1.0 8 2.5	2.0 1.2 1.3	1.9 4 -1.3 8	8.0 4 -1.8	.5 8.2 8.2 -2.0	1.9 1.0 .8 -1.3	8.1 .8 0 -1.1	1.9 -1.0 .2 2.3	1.1 -1.1 .8 8.2	2.0	-1.8 2.0 .7	8 -1.3 -3	• • • •		8 5 5 5	4.1 -1.8 1	1 -1.8 8.1 -1.1	2.0 -1.2 -1.3	2.6 1 8	1.5 2.8 -1.1 -1.0	1.1 -1.8 -1.3 8.1	1.1 8.8 1.8 -1.1	8.8 1.5 .8 -1.1	*725
8.1 -1.8 -1.0 -1.3		2777	5 -1.8 1	8.1 8. -1.5	.6 -1.5 2.1	2.6 2.2 1 0	3.4 1.4 -1.1	-1.3 .6 2.2 1		-1:1	2.3 -1.0 6 -1.2	2.2 -1.3 -1.3	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	-1:1	0 7 2.1	5 8.2 8	-1.3 1.7 -:8 -1.3	:::::	2.5 2.8 2	7 -1.3 1.7 -1.8	3 -1.3 8 1.7	1.1 1.6 -1.1 2.0	-1.8 1.9 1.3	14798
2 -1.2 6 1.0	.7 8 1.9	-1.8 8 9	9 .5 4 1.3	.1 2.0 8 1	.8 1.4 0 8	8 .5 1.4 3	-1.8 9 0	.8 0 1.8 +.9	8 1.1 5 -1.1	0 4 6 -1.8	4 -1.2 3	-1.17	-1.3 -1.2 1	7557	7 .8 1 5	5 9 -1.1		7 0 9 -1.8	.3 7 8	-1.8 9 -1.1 1	0 -1.0 -8	** **		70.00
-1.0 1 2 3	-1.1 0 0	-1.0 .1 .8	4 4	.1 -1.1 0	1 -1.8 0	.5 .8 1.5	12.00	6 7 1	-1.1 6 1	9 4 8	7 .5 0	1.4 .7 .6 1.0	-1.0 9 8.4 -1.1	2.5 5 -1.2	2.3 .4 1.1 -1.3	-1.0 -1.0 8.6 -1.0	2.5 0 -1.1 6	-1.0 E.5 .6 -1.1	-1.8 2.3 1.4 6	-8.3 .5 1.8 5	4 -1.3 8.6 9	-1.1 2.5 4 -1.5	-1.8 7 2.6	.4 -1.8 9 8.8
8 -1.1 1.6	1.5 1.4 -1.0	7 -1.1 1.4 1.4	8 1.6 3 1.7	-1.2 .9 1.5 -1.0	1.0 1.3 .3 -1.8	3 .0 1.2 -1.3	9 1.5 -1.8	8 2.0 1.4 1	8 2.0 4	1.5 .7 -1.0	.8 1.5 -1.0	7 1.0 .8 1.1	1.0 1.6 -1.2	2.0 .8 1.4	-1.0 1.8 .7	-1.0 .5 -1.2 1.6	0 -1.1 1.0 1.7	1.7 -1.1 -3	-1.8 1.5 .1	3 1.5 -1.8	2.3 -1 6	1:81:1	1 1.1 2.6 2	1.6 -1.2 -1.8
0 -1.1 1.7	.1 4 -1.0 1.6	5 1 1.6 -1.8	1.5 -1.3 0 5	1.8 5 0 -1.0	8 -1.8 1.5	6 -1.8 .8 1.6	-1.0 4 1.8	3 9 1.0	1.8 7 8 -1.0	-1.2 9 1.6 -1.0	8 -1.0 -1.3 1.5	1.7 0 -1.1	-1.0 -1.3 5 1.5	6 1.8 -1.3	6 1.9 9	6 -1.3 -1.1 1.8	1.0 1.9 9	.6 .3 9 1.8	1.5 5 -2 -1.3	1.9 1.5 1.8	.5 2.2 7 1.6	1.4 .2 -1.1 1.6	1.6 -1.5 1.2 0	1.7 1.4 1.8 -1.2
-1.3 -1.3 1.0	8 1.6 -1.3	-:a -:8	6 .1 .5	-:4	4 8 9	1.7 2.0 .0	1.5 1.0 .8 -1.8	8.1 .7 2.0	1.9 1.6 8	1.7 1.1 .5 -1.0	2.2 1.6 5 2	.5 1.8 6 2.1	1.0 -1.1 1.6	1.7 .6 5 -1.0	1.2 -1.5 .8	1.8 .4 .1 9	-1.5 1.4 1 5	4 1 -1.2 1.5	4 1 -1.8 1.5	-1.0 1.5 -1.8 8	2.0 6 7	.6 1.8 9 .6	-1.8 1.5 9	7 4 8.0 1.8
-1.0 -1.0 1.7	1.5	1.7 6 -1.0	1.4 6 0	8.3	-1.1 1.6 -1.0 6	-1.0 0 .8 1.7	1.5 6 .6 -1.2	.9 5 4 8.8	1.6 2 1.6 -1.8	1.7 5 9 1.9	-1.2 1.4 .3 1.6	-1.0 1.8 1.5 7	1.6 -1.8 1.1 -,1	.2 1.3 1.7 -1.1	.8 -1.1 6 8	.3 1.5 0 6	.1 1.1 .8 8	.5 4 1.5 .9	6 0 -1.3 .6	.2 .8 -1.0 -1.1	.4 .1 1.1 0	-1.8 .6 7 1	8 .7 -1.8	1.5 -1.8 5 .6

-8.978

-.578 -518

-.864

-.658 1.074

.298

.096

.865 -1.098 -.958

.750 .975 1.450 .900

.600 .550

.800 .715 .238

. 522

.925 .644 .295

.250 -1.050

-.850 .850 -.400 .850 .800 .500 -.500

Max. + Min. Max. • Min. Medies Median. μ .950 .350 .250 -.050 .150 -.800 1.557 -,080 -.080 -,050 -.187 .868 1.098 .849 .630 1.111 1.218 1.335 1.179 .370 1.049 1.704 .776 .980 .675 -.050 .885 .100 .850 .550 .050 .046 .150 1.290 ,650 -,050 .700 .060 .400 1.075 .200 .575 .618 8.500 -,201 -.400 -.750 1.050 -.510 .650 .800 .150 -.800 .850 .855 .550 .550 .825 .675 .575 .550 .400 -.150 -.275 .660 .660 .658 .606 1.050 0 -.150 .050 .800 -.460 -1.300 .850 .850 .850 .750 .380 .600 -.200 .300 .850 -.150 .600 .550 -.150 .600 .090 -.100 -.250 -.315 -.078 .578 -.576 -1.500 -.550 .525 1.860 -.050 .875 1.375 -,056 -.075 -.075 -.076 -.400 -.625 -.276 .025 .100 -,250 1.119 -.067 1.125 .325 1.000 .488 -1.554 -.125 -.528 -.474 -.360 -.100 -.050 -.760 -.450 .602 .758 1.108 -.050 -1.200 -1.239 -.600 1.160 700 800 1.485 .685 .675 -.323 -.260 -.500 .050 .500 .775 .876 .785 .327 1.338 .424 .076 . 59-1 .675 .636 .450 .813 .800 .486 1.048 .760 .558 1.005 -.500 1.100 -600 -750 -550 -.478 1.348 1.267 1.025 .700 .075 .750 -.375 .325 .476 .250 -.600 -1.000 -.050 -.300 .400 1.000 .700 .250 -.700 -.500 -1.415 -.650 -1.450 -,200 1.165 .820 .255 -.844 -.800 -.800 -.500 -1.176 -900 -860 -860 -160 -160 -100 -100 -460 0 .887 .835 .497 .402 .814 .985 .528 .610 .804 .680 .781 1.154 .370 1.015 .134 .370 1.015 .319 .791 .471 1.554 .867 .771 .745 ,865 -.125 -.576 -.825 .878 0 .385 .500 -.076 -.150 -.700 -.450 - 100 - 450 .575 .536 .575 .618 .687 .698 -.802 -.837 -.328 -.625 .425 .986 .885 .600 .860 .475 .680 .800 -.100 -.200 1.075 1.899 .21.5 . 688 -.184 .650 .200 -.100 .488 .480 -.113 .638 .850 .976 .900 .250 .850 .885 .150 .760 .714 .R54 .400 .050 .550 .451 1.084 ,874 ,450 .092 -.150 .075 -.281 .100 .200 1.100 .050 .150 .160 .365 .885 -,875 .675 .280 -.445 -.050 .100 .550 1.400 .700 .685 .800 .538 .486 1.600 1.660 .668 .100 0000 1.085 .600 .188 -1.000 -025 -.500 .125 -.678 -.100 -1.850 -.750 .050 -.850 .857 .756 .840 -1.167 .035 -.595 -.450 -.500 -1.800 .978 .888 .765 .045 -.450 -1.485 -1.650 -1.427 -.800 -.900 -.200 .800 .675 -.075 -.060 -.350 -.500 -.400 .950 .326 .460 .750 .167 .176 2.850 -1.161 -.147 .115 .568 -.450 .581 .676 .975 -.750 -.565 .800 .600 1.748 -.200 -.870 -.150 -.100 -.400 .400 .688 .876 -.376

-,250

-,450

-.800

..500 .050 -1.650

-.550

-.600

.250

.750

-.100

1.500

-.950

-.450 .150 -1.350 -.550 .300 -.500 .800 .050 .800 -.925 -.875

.350 .380 .160 -.850 .150 .080 .100 .450 .360 1.000

-.850 -.600 -.550

.850

-.850 -.850 -.360 .200 -.300 .560 .300 -1.300 .100 -.650 -.880

-.250 -.350 -.150 .150 .075 .450

-1,150

-.075 -.685 -.700

1.700

.850

.700 .875 .550

1.050 .765 .600

1.050 .725 .875 .850

.816 -.356 -.548 -.288 .189 -.085 .594 .690 -1.000 -.068 -1.486 -1.687

1.015 .687 1.080 .907 .756 .948 1.151 .918 .456

TABLE D.—Statistics for Drawings from Normal Universe

# APPENDIX II

97	178	.400	760	1.068	1.546	140	3.60	475	-1.000	.080	.000	.073	
52 I	,228	.080	. +600	.838	.396	.668	159	-100	.180	.000	.400	.406	- 844
85 I	325	·.060	600	.888	-947	343	356	486	.650	.800	.018	.610	.000
54 I	.600	.680	.380	.200 1	.856	.225	184	600	+.000	.880	1.180	1.408	-,486
56	220	-180	600	1.078	1.218	168	100	980	800	000	.780	.792	004
56	178	+.100	260	4868	1.166	+.180	186	700	780	780	.000	.018	-,002
57	376	800	880	478	.566	700	157	.088	+.150	.800	.488	608	.048
88	800	860	050	1.000	1.876	836	180	.886	.800	.780	.778	-804	777
99	,226	.080	,400	.000	.986	.306	100	475	800	460	.888	.819	063
60	.17B	w.080	.400	.528	.684	.276	180	275	650	.300	1.878	1.831	180
61	.888	-480	.000	.628	.684	.000	163	.850	-100	1 :200	.800	.867	
68	545	0.700	.050	.613	.709	489	168	660	-1.100	000	.800	.986	910
68	.528	.100	-000	.888	1,008	-584	165	-478	.300	.480	.818	.868	1.200
64	150	480	-150	150	.680	223	164	.800	100	.700	1.100	1.848	.894
66	100	-100	800	.700	.881	-180	168	-180	.000	.850	-478	-610	
88	.226	.880	460	.678	-817	.275	166	.860	.800		1,850	1.878	1 276
87	.880	.880	350	.880	.880		167	675	500	- 660	.326	408	-1.480
24	300	400	800	.560	.070	.516	100	.480	000	000	1.285	1.670	-806
69	.685	800	*.880	.975	1.186	-,588	100	.700	480	980	.700	.857	.014
70	-1.100	-3.880	950	.626	.700	-1.465	170	700	780	680	.480	.848	-3.800
71	1.100	-1.000	,600	.400	474	8.800	171	-100	000	000	1 .600	.786	.134
72	978	600	150	.686	.700	476	172	.005	-400	.880	.626	.680	
75	050	800	300	.078	.698	078	178	.800	.000	800	.680	.738	1.084
74	425	450	.400	478		.808	174	1.188	1,500	.780	713	.844	1.385
76	850	900	600	1.100	1.861	478	178	176	800	100	.888	377	404
76	-175	.800	-100	.685	.686	070	170	180	180	180	.480	.840	-,876
77	480	.880	.560	:480	.808	.899	177	.226		.480	.586	.046	.040
70	580	~.480	- 200		.567	610	179	.580	.480	.880	-480	.471	.745
70	-028	100	.150	.186	.837	-118	170	700	800	900	.800	.017	- 768
80	476	.600	.880	400	.016	.760	100	185	-,460	,800	.075	.988	186
81	1.178	1.000	1.860	.075	1,210	1,000	181	.400	-800	800	.800	.644	.681
82	800	700	800	.500	.418	-1.818	188	825	-,600	-,180	1.375	1.588	-,806
88	1.088	.000	1.000	.888	.984	-1.854	108	+.800	880	-,880	.300	.304	761
84	.350		7,700	.988	1.137	308	184	.080	100	.800	.385	.898	.180
85	.700	.000	.800	1.100	1,107	.800	188	700	480	880	.860	.675	-1.007
88	085	-,450	700	.480	.854	-1.106	186	1.326	1.800	.780	-478	880	2,400
87	.160	.850	.800	.800	.040	-,430	107	785	800	680	.885	.890	014
86	.500	800	.800	.880		1703	100	.373	.780	-777	.720	.870	-683
80	.378	480	1800		.925	406	100	1	.080	060	.860	.406	
90	1.175	1.880	1,000	1.878	1.806	.899	190	.178	.180	.100	.780	.084	2.000
91	1.080	1.400	4700	1.175	1.185	.038	191	885	.880	.100	.978	1.007	.899
	985	-1.100	750	1.876	1.608	610	198	495	450	400	.845	.884	767
98	.085	1,800	.580	1.175	1.001	.900	198	.800	-640	080	.700	,628	,848
94	-1.100	-1.100	-1.000	800	. 711	1.587	194	.078	.850	200	1.178	1,880	.000
95	180	1,180	-100	.588	.810	846	198	.100	.080	.180	.750	.661	.117
94	300	- 400	180	1.600	1.971	160	199	.175	-,180	.800	.928	1,089	.141
97	100	- 400	.100	.680	.779	198	197	.300	800	,800	.180	,150	.190
96	.100	800	800	.900	948	,104	198	.178	,100	.880	.878	.620	.811
	376	180	000	.679	618	-,808	100	-1.100	-1.100	-1.100	1.480	1.618	725
100	878	-,500	080	.480	4861	-,63.0	800	080	,800	800	.645	.688	804
	1				1:7:-								

Table D.—Statistics for Drawings from Normal Universe—(Continued)

Sample Runber	¥	Median	Max. • Min.	ш	σ	8	Sample Rumber	¥	Median	Max. · Min.	u	ď	
201	.126	,150	.100	1.445	1.508	<b>,085</b>	501	400	-,160	650	.480	. 654	749
202	.476	.400	.680	.975	1.087	.487	502	.625	1,100	.150	1.015	1.198	.582
205	.400	.500	.400	.250	.508	1.298	808	.125	,700	650	.0:3	1.124	iii
204	675	950	-,400	.888	1.028	-,656	304	100	100	100	1.750	1.866	054
205	.275	-460	.100	.575	.642	.428	305	325	500	.950	1.125	1.477	220
806	500	050	550	.800	1.002	299	306	.775	.600	.950	.925	.968	4607
807	875	250	500	.876	.60%	~.623	307	850	400	-,500	.450	.517	677
208	.750	.700	.600	1.050	1.188	.653	208	-1.000	-1.000	-,200	.100	.141	-,709
209	0	250	.250	.550	-675	0	809	.200	1.050	450	1.400	1.541	.183
810	1.100	1.050	,560	.480	.464	2.371	870	.325	.550	.100	.565	.481	.772
211	.750	.760	.760	.700	.782	.959	511	.400	.800	.600	.400	-474	.844
\$18	325	350	300	.476	.526	618	202	.126		,250	.238	.277	.451
218	500	-,500	800	.860	.430	698	315	475	,400	550	.525	.402	-1.182
214	050	.360	-,450	.675	.789	684	514	275	.860	0	.775	.884	512
215	325	500	-,150	1.075	1.108	894	815	626	.850	,700	1,050	.736	-,713
816	475	350	600	.925	.975	488	316	.650	,ê50	,450	.875	1.115	.583
817	785	960	500	.565	-421	-1.788	82.7	.425	,100	.750	.658	1.019	.418
816	.550	.160	* ,660	.600	.728	.486	\$18	560	400	-,500	.500	.540	648
819 820	.178	.100	.250	.725	.740	.840	519	900	-,900	900	.800	.945	-,954
821	~,528	-,480	-,200	.415	.618	625	320	.028	100	.180	.825	.896	.028
222	.500	+160	.450 460	.850	.418 .381	.718	591	325	-,650		.865	1.042	50.2
285	400	400 850	460	.880		-1.050 050	828	250	.200	700	1.125	1.379	182
224	500	150	460	-675	.858 .418	718	828	1.100	1,200	1.000	.950	1.102	.998
225	.180	-,100	800	.650 1.150	1.521	114	524 525	.050	.500	200	.800	.928	.054
226	-,225	100	850		.870				080	.200	- :625	-,634	.039
227	.878	.750	890	.525 .565	.444	1.971	525 527	150 125	050 100	250	.700	.789	190
	-1.076	-1.600	550	1.088	1.509	+.025	348	050		150	.288	.590	+,520
220	-1.070	700		.700	4860		589		880	.250	.685	.736	-,680
250	.700	200	.700	.600	.700	.814	580	175 225	-,250	-,100	488	.642	273
831	050	.050	150.	.650	.687	078	551	1.275	550 1.050	100 1.160	.378	.455	495
252	050	.650	950	1.475	1.710	089	532	1.270	.080	050	.926	.991	1.267
255	585	500	550	.675	-729	720	333	.200	******	400	.850 .450	.552	.382
254	.100	-150	050	460	495	208	834	875	-1.550	-,700	1.588	1.668	526
236	685	700	-,550	.985	.955	054	836	375	400	880	.525	.586	713
236	.650	460	1650	.600	.701	-784	586	075	-,150	*****	.625	.847	089
227	700	.860	1850	1.080	1,887	.505	857	.700	.450	.950	-800	.992	700
258	.575	.560	400	.225	.286	8.010	838	.575	4050	1.200	1.213	1.477	.589
259	.675	-750	800	.825	.878	.778	839	.650	500	4800	.550	.688	1.045
240	.888	650	400	446	.588	1.006	840	188	150	400	.488	.575	217
241	615	400	880	.688	.856	750	841	226	500	.080	1.125	1.516	171
848	175	,150	500	.065	.779	425	548	.725	-700	850	.925	1.064	.682
845	650	-,550	550	,400	.458	-1.484	848	.825	<b>4650</b>	1.000	.885	4887	950
B44	.800	.550	.050	450	.524	.572	544	.075	-,150	.500	.465	,546	.138
845	700	950	450	.800	.981	756	245	.175	.850	0	1.275	1.590	,186
846	.510	.150	.150	.950	.995	.151	546	1.125	.950	1.500	1.175	1.231	.914
247	575	550	800	.625	.672	668	847	785	700	750	1.125	1.202	603
245	.125	.100	.150	.675	.778	.168	548	225	850	200	.275	.308	742
249	.150 ·	.500		.600	.786	,204	849	.025	0	.050	.825	.978	.OR6
250	,575	.800	.350	.725	.886	.696	350	650	650	-,650	1.100	1.189	547

APPENDIX II

		LABLE L	,—STATIS	1103 1	OK D	CAWINGS	FROM	TUKMA	L UNIVE	:RSE—(Ca	nunu	ea)	
Sample Mumber	Ŧ	Median	Max. + Min.	ц	,a	3	Sample Number	Ī	Median	Max. + Min.	и	σ	
401	100	100	100	.400	.447	- 224	601	.375	-,200	.050	.375	.760	.493
402	.400	.600	.200	.750	.941	.425	502	750	-,700	800	.500	.585	-1.505
403	.550	450	.250	.175	.205 -	1.707	503	850	-1.100	600	.975	1.229	692
404	.500	.450	.550	.700	.718	-696	504	.680	.750	.550	.700	.807	.682
405	.175	.200	.150	.425	.536	.526	505		~.050	.050	.200	255	. 0
406 407	575	650	500	.625	.735	784	506	.575	.250	.500	.925	1.213	.509
408	.400 0	.650 100	.150 .100	.500	.596 .574	.671	507 508	575 525	550 250	500	.275	.356	-1.616
409	025	400	.550	.663	.775	585	509	-400	-,250	.250	.565	1.017	808 .393
410	725	550	-,900	.725	.856	868	510	100	500	.100	500	.503	199
411	.425	.550	.500	475	.589	-721	511	-325	.150	.500	.458	.586	.618
412	825	-,700	950	.875	.901	916	512	.575	.350	.800	.525	.634	.908
415	-,225	050	400	.625	.750	-,500	518	.525	-400	250	.625	.708	.459
414	.650	.650	.650	.700	.701	.927	514	1.050	1.150	.950	1.150	1,289	.915
415	0	.350	550	1.050	1.177	0	515	.250	.250	.250	.200	.205	1.219
418	500	~.450	150	.500	.367	817	516	150	-,250	050	.400	.439	342
417	.225	.100	.350	.536	-416	.542	517	.325	-450	,,200	1.475	1.457	.223
418	475	550	400	.375	.402	-1.182	518	.625	.700	550	.538	.415	1,988
419 420	.100 .350	.150 100	<b>\050</b>	.850	.941	,106	519 520	675	.200	200	.950	1.116	0
421	-,200	100	-800 400	1.175	1.452	.244 348	520 521	250	800 450	550 050	.488	.614	-1.099
422	150	500	200	.950	1.071	140	522	.225	.150	.500	1.075 .858	1.395	179 .198
425	.125	.150	100	.575	497	252	525	-1.000	900	1.100	650	.857	-1.167
424	175	-,300	050	1.575	1.451	-,122	524	-450		.900	1.075	1,285	.350
425	~.675	800	-,550	1,225	1.482	456	525	450	850	050	.925	1,128	599
425	-,250	-,100	.250	.525	.363	-,652	526	.525	.400	.650	.675	,835	.628
427	.200	.100	.300	.550	.612	.327	527	<b>.675</b>	.800	.550	.758	.965	.699
428	175	600	.250	1.075	1.249	112	528	.900	.950	.850	1,150	1,347	.668
429	075	100	050	.675	.775	097	529	125	400	.150	.775	.950	158
430	.550	.450	.550	400	.438	1.255	550	625	-,750	-,500	1.025	1.068	585
431	.850	1.250	450	875	1.035	.821	551	.500	-450	,150	1.550	1.586	.189
432 433	-,225 -975	350	100 1.150	.525	.567 .879	397 1.109	552 535	-775	.950	.500	.338	.396	1.958
434	600	850	950	.775 .850	972	-,617	534	.475	•700	.250	.575	.676	.703
435	075	.100	250	.775	.879	-,655	535	.075	,050	,200 ,100	.750 .725	.797	.126 .105
436	450	250	1.150	1.075	1.242	.362	536	10.0	.250	250	1.150	1.217	
437	925	+1.000	.407	925	.556	-2.598	537	.525	350	.300	.475	.526	.618
458	.225	200	.470	.375	. 585	-587	536	-,500	100	500	.550	.636	-,472
439	.325	.450	.846	-675	.864	.376	539	600	-,550	850	.550	.552	-,920
440	.950	.800	.501	. 400	.471	B.019	840	1.000	.650	.950	.650	.758	1.319
441	.050	.500	.595	.475	.572	-087	541.	-1.425	-1.450	900	.475	,638	-2,233
442	.250	.350	.535	.425	.540	.463	B4.2	026	.150	200	.738	.936	027
443	.650	.500	.555	-425	.522	1.245	B43	.450	•100	.800	.850	1.052	-429
445	.025	.200 .500	1.661	1.325	1.475	.017 1.411	544	.250	.950	-,450	1.330	1.556	.161
446	525	- 300	.546	.275	.527	994	545 546	.400	.950	150	1.000	1.190	.536
447	525	.850	1.458	1.165	1.410	301	547	.525	.800 .650	.550	-488	.618 .779	1.098
448	.825	.650	1.034	.925	.B44	.978	548	.475	500	350	.663 .675	.935	-,569
449	.400	400	.762	.600	.600	.667	549	.400	-800	1 2000	1.050	1.251	.320
450	150	200	.752	.600	.654	237	550	125	0	~.250	.425	.460	272

Table D.—Statistics for Drawings from Normal Universe—(Continued)

451	.200	.350	.801	.400	.466	-418	198	+180	.180	-180	.800	. 568	.887
482	,z00	~.150	.869	.880	.636	.51 6	808	078	100	080	.078	.698	10*
463	.775	1.000	.424	. 338	.390	1.987	803	.778	1.080	.800	.788	.876	.794
454	.800	1.300	1.255	1.000	1.178	.661	804	-,825	-1.000	800	.463	.884	-2.490
488	.250	.150	.601	.400	.438	.871	868	478	500	480	.048	.908	674
486	.225	.160	. 202	.225	.249	.904	866	378	-1.800	000	.928	.896	410
457	1.075	1.200	.535	.488	.460	E, 350	887	-480	.380	.880	1,600	1.518	.343
458	100	350	1.258	1.000	1.089	092	808	300		600	.800	.945	-,310
459	.026	*180	.971	.778	.817	.306	509	100	.960	580	.900	1.006	098
460	.200	.100	.758	.600	.748	-401	560	478	580	400	.878	.402	-1.182
461	.100	.100	1.758	1.400	1,780	.008	861	.825	050	.700	.886	1.078	.303
468	.075	.800	1.410	1.125	1.882	.095	262	480	700	800	.926	1.100	549
468	0	.080	.689	.550	.688		863	,200	-180	.250	1.180	1.168	1"1
484	.825	1.150	.768	.613	.736	1.181	864	.800		-400	-800	.616	.328
465	.150	,800	.877	.900	.709	*878	865	375	180	600	.575	.698	.537
486	.600	.800	.627	.500	.618	-,980	866	-1.200	-1.180	780	.900	.704	-1.200
467	275	350	.658	.526	.807	461	867	700	900	500	.880	. 636	-1.100
468	475	-,560	.298	.238	.295	-1.610	566	900	-1.100	100	1.200	1.233	730
469	800	-1.000	.877	.700	.872	918	869	1.178	1.480	.600	.488	.576	2.040
470	150		.407	.325	.890	365	870	-1.000	700	-1.100	.700	.846	-1.182
471	100	. 500	1.804	1.200	1.455	070	971	525	+.600	+,360	-975	.859	-2.028
478	025	180	.781	.076	.642	.030	972	078	380	.200		1.099	068
473	~.300	-,850	.515	.250	.274	-1.095	575	.500	.400	.600	1.800	1.810	.276
474	275	-,200	1.805	1.025	1.318	-,209	374	-,700	850	-1.150	-850	1.007	69B
478	075	+,150	.208	.338	.295	-,854	975	480	480	450	.600	.694	
476	800	480	.864	.480	.524	,362	976	.025	060	-100	.578	-444	.056 256
477	.150	850	1.25	1.025	1.205	-134	877	800	450	-,200	.500	.781	498
476	278	450	.674	.689	.668	411	578 579	385	450	450	.800	.687	105
479	.500	.150	1.135	.900	1.098	574	560	525	.650	400	.425	-476	1.108
480	- 550	600	.157	.125	-145	.538	561	.425	.550	300	.463	.501	.731
481	.028	-,200	.785	.625	.907	910	562	.178	.250	100	.288	363	.488
482	.625	.850	1.034	.825	.818	.732	563	950	1.000	.800	450	476	1.998
483	.375	.080	.576	.300	.339	295	284	.600	.800	.700	.700	.736	.816
484	.100	150	1.347	1.075	1.123	106	563	225	150	300	878	665	-,330
485	.275	.200	407	325	408	.684	586	- 178		-, 350	.778	.841	200
480	-1,190	-1.200	1 .501	1	.502	8, 291	507	028	250	300	.625	.947	026
488	350	-,750	1.279	1,100	1.293	229	566	225	.200	-,650	.868	1.045	E.S
489	-650	.950	.783	.625	.748	.675	509	800	0	-,600	-550	.656	457
490	-,880	480	721	.678	750	735	890	-1.000	850	-1,800	.750	.928	-1.100
493	300	180	.818	.650	.733	410	B91	800	100	300	.200	.248	616
492	128	200	971	.778	.798	.187	598	475	550	400	.488	,648	740
493	428	350	.178	.138	.164	-8.590	598	625	-1.200	-,400	.915	1.085	768
494	278	380	1.054	.825	.956	,886	894	.550	.450	.260	.650	.687	.610
495	700	.880	.752	.600	.711	.984	898	. 0	100	.100	.600	728	0
496	1 .100	200	.689	.550	.644	-105	2006	480	150	750	.878	.678	670
497	.380	450	1,847	1.075	.960	.865	597	-,180	-,200	080	.586	.622	201
498	478	,080	1.207	.965	1.186	411	598	.200		.B00	.628	.763	.326
499	.028		.788	.625	.756	.581	200	-1.080	680	-1.450	.978	1.180	890
800	.475	.850	.971	.775	.011	. 686	800	.800	.750	.680	.800	. 524	1.627

lample Imaber	Ŧ	Medien	Max. • Min.	μ	σ		Semple Eumber	Ī	Median	Max. + Min. 2	μ	_ σ	
601	.325	.200	.480	.625	.676	.401	701	-,275	. 0	550	.615	.729	877
608	600	600	-,500	.200	.224	-2.679	702	.275	.850	,300	.475	.658	.451
605	.675	.750	.600	.575	.622	1.085	703	.475	.800	.150	.888	1.078	.450
604	.750	.850	.650	.750	.856	.876	704	450	.680	250	1.000	1.114	1.980
608	450	550	550	.350	.415	-1.085 -536	705	1.400	1.111	900	.600	.707 .628	516
606	.576 .075	.450 .100	.700 .050	.975 1.175	1.114	.065	705	.150	.560	050	.776	.976	.154
608	.625	.700	.850	.468	.563	.952	708	450	750	150	,850	.986	456
609	450	600	500	.625	.798	566	709	.100	.100	.100	.650	-667	.150
610	225	400	050	.718	.904	249	710	500	450	150	.800	.567	811
611	+.300	650	,050	.600	696	450	711	.075	.050	.100	.376	497	.151
618	250	400	-,100	.375	.485	-,549	712	,075	0	.150	.675	.701	.107
615	275	.100	650	.818	.985	280	718	125	-,250	0	.625	.657	190
614	250	600	.100	1.500	1.591	167	714	376	050	700	.565	.661	567
615	.375	-400	.880	.925	1.018	.366	715	575	750	400	.625	.672	85
61.6	200	~.500	100	.450	.579	346	716	-1.125	-1.150	-,500	.375	.396	-2,840
617	.750	.050	.100	1,050	.675	1.111	717	.025	.200	250	.875	.954	.021
618	325	450	200	.925	.950	-,542	716	025	.200	250	.439	.550.	041
629	.200	.050	`.850	.250	.292	.685 .156	719	.775 .150	.250 .400	1.300	.963 .800	1.135 .928	.683
620	.125	-,250	,500 ~,950	1.036	1.260	417	720 721	125	500	.050	1.125	1.160	100
681	525	.150	.150	.200	.205	.752	722	.500	.450	350	.200	.256	1.950
622 623	.150 -1.126	-1.100	-1.050	.725	.795	-1.415	725	.625	.950	300	.965	1.161	.529
624	575	550	-,800	,625	.978	568	724	.625	.650	.600	1.175	1.181	.529
625	.700	250	1,150	1,100	1,552	.668	725	.600	850	.350	.800	.987	.606
626	.200	.500	100	<b>.650</b>	.768	.260	726	275	100	450	.565	.427	644
627	.425	.450	.400	.825	.844	.504	727	- 250	~,150	550	1.050	1.324	199
626	.500	.200	.600	1.200	1.221	.246	728	025	100	-,050	.525	.545	.046
629	.050	0.	.100	1.200	1.501	.884	729	125	450	.200	.865	1.061	116
630	.350	.100	.600	.650	.779	.449	750	-,800	<b>→.150</b>	-,450	.550	.644	460
653	.450	-150	.750	.950	1.031	.436	751	.300	100	.700	1.150	1.298	.253
638	.600	-630	.400	.550	.554	1.695	732	-,250	.450	050	.900	1.120	.221
685	.200	8	400	1.550	1,760	-112 150	733 734	.025 .450	.450	.250	.575	.642 .205	2.195
634 635	100	500	200	.750	.771 .497	-1.359	735	350	900	200	.975	1.152	309
636	125	150	100	.525	554	226	736	178	250	100	975	1,050	170
637	1.025	750	1.200	.775	.926	1.107	737	850	850	250	.150	.179	-4,750
628	.100	200		.550	.579	.175	738	325	-,150	500	.475	.554	-,587
639	.025	050	,100	.258	.295	.085	739	.975	.900	.850	.675	.701	1.591
640	.175	.100	.250	.275	.335	.522	740	575	900	.100	938	1.152	496
641	975	-1.150	700	1.075	1.256	756	741	.775	1.400	,150	1,238	1.451	.534
842	.750	.750	.750	1.000	.980	.761	742	.550	.250	450	.850	.907	.386
645	.925	.650	1,000	.658	-760	1.218	743	.125	.500	050	.463	.563	.222
644	.200	.500	100	1.080	1.510	.155	744	.325	.450	.200	.875	1.028	.316 -1.510
845	775	550	600	.415	.492	-1.576 -1.051	745 746	-1.550 400	-1.600 .500	-1.100 500	.825 .800	1.030	.451
846	675	~,850	500	.575	.642	455	747	600	-,750	450	.500	,543	-1,105
647 648	~.425 ~.800	-,550	-,500	725	.316	-2.531	748	.025	100	050	.475	.512	049
649	550	-,250	850	.850	.986	554	749	500	400	- 200	1.550	1.508	215
650	.250	300	800	.875	1.015	-247	750	,100	500	250	.550	.644	.155

TABLE D.—Statistics for Drawings from Normal Universe—(Continued)

Table D.—Statistics for Drawings from Normal Universe—(Continued)

Sample Humber	7	Median	Max. • Min.	μ	σ	=	Sample Ember	¥	Median	Max. + Min.	ц	σ	
801	-,275	~,360	200	4775	.844	326	901	625	600	250	.138	.179	-B.490
808	975	-1.000	250	.925	.209	-5.765	902	.075	.260	100	.788 a	.948	.080
805	.800	.100	.500	.850	.671	.447	905	-,800	<b>750</b>	850	.560	.628	-1.274
804	500	860	150	.600	.696	718	904	.500	.900	.300	1.500	1.565	.319
805	050	050	080	.400	.531	094	906	.776	.800	.550	.296	.890	1.987
606	325	400	500	.375	.471	690	906	.250	.800	800	.750	.792	.316
807	175	BOO	.150	.488	.663	511	907	800	-,500	100	.600	.736	-,407
808	.376	a100	.650	1.125	1.270	.895	908	100	050	+.150	.450	.604	166
809	500	.100	~.700	1,050	1.210	~,848	909	.400	.360	.450	.250	.524	1.234
810	-,225	100	550	.558	.415	842	910	225	150	-,800	.675	.858	264
811	125	-,150	~.100	.686	.729	'171	911	.275	.450	.100	.975	1.016	.271
612	.850	.550	,350	-400	.408	.871	912	-,500	600	400	-400	.458	-1.091
612	400	200	600	1.050	1,125	556	915	.250	.200	i 500	450	.476	.525
814	425	~.550	300	.418	.512	830	914	150	100	-,200	.400	-415	-,361
815	325	- 550	100	.612	1.016	520	915	.175	.180	.200	-575	.618	.283
616	825	850	700	.475	.526	-1.569	916	.675	.500	.850	.825	,873	.773
617	875	200	550	.565	.427	878	917	025	350	550	1.188	1.416	018
616	.125	150	.400	.588	.701	.178	918	075	- 600	500 550	1.315	1.616	046
819	.425	-050	.800	.988	1.205	.353	919	575 .525	450	550	.025	.755	541 -716
820	450		- 900	.625	.968	2.521	920	075	- 100	050	.575	602	125
621	.575	4600	.500	.225	.228 .890		OPE I	075	.500	150	788	.952	.184
822 823	.250			.800 1.050	1.178	.201	925	250	400	100	1.125	1.490	168
825	075	150	150	375	481	178	925	650	750	550	.650	.944	689
825	675	1.000	.560	638	.776	670	925	.275	.580	000,	.768	976	383.
828	-,175	.050	- 400	.725	.807	217	926	225	500	.050	.465	.536	-,420
827	050	.100	200	.550	.628	080	927	-050	100		.500	.365	,139
828	.750	650	350	.225	.268	280	928	275	550	ă	.588	.694	506
829	.525	.550	500	.275	.356	1.475	929	275	350	200	.738	.995	277
850	-,450	600	500	.500	.559	805	950	400	-,500	-,500	450	.524	765
851	.325	150	4800	.625	705	4461	931	575	550	200	,530	.577	996
638	825	-1.050	600	.613	.743	-1.110	952	.050	0	.100	.750	.829	.060
855	.525	400	.250	.188	.217	2.420	933	.125	.250	0	.625	.661	.189
854	450	.800	400	.550	.606	.742	954	225	.500	650	1.088	1.297	173
835	225	450	0	1.175	1.305	172	935	600	850	650	.450	.534	-1,124
836	450	450	-,450	.500	.559	805	956	.475	.600	350	.225	.259	1.035
837	175	.250	600	1.015	1.222	143	937	.025	.500	250	.563	-676	.057
838	-,525	250	800	.638	.766	-,685	958	.875	.950	.700	:588	208 €	1.744
839	,500	.650	050	.700	.828	.562	959	825	800	850	.438	.602	-1.370
840	925	650	+1.100	.688	.844	-1.096	940	.125	100	. 380	1,158	1.475	.085
841.	.675	-450	.900	1.075	1.121	.502	941	.525	.580	.500	.575	.497	<b>⊾654</b>
842	075	-,200	.050	.625	.766	098	848	.050	250	350	.925	1.157	.044
B43	.500	.250	.560	.750	.778	.386	945	.525	.500	.150	.525	.597	.545
844	.525	200	.460	.575	.698	.466	944	600	150	-1.050	1.200	1,594	431
845	350	200	-,400	.275	.519	-1.097	945 [	.550	.550	-1.050	.550	.680	.809
845	.476	+650	.500	1.425	1.460	.826	946	.100	050	.250	.350	.418	.239
847	1,600	1.650	.550	.400	.430	5,720	947	-1.100	-1.000	800	.500	.592	-1.858
848	250	.200	-,800	1.000	1.205	208	948	.425	.450	-400 400	.485	507	.838
849	1.500	1.450	.550	.550	.418	8.110	949	025	450	-400	.975	1.146	022
650	.078	.050	.100	.675	.718	.108	950	.100	.700	500	1.050	1.819	\$60;

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85)	800	280	,860	.800	1.038	80l	951		.200	200	1 .500		
858	100	.080	-,250	.800	.579	178	908	,328	,680		-818	.074	. 300
868	300	600	•	.650	.761	704	935	550	400	-,300	.880	.008	-,584
854	025	.100	180	.725	.769	-,035	984	-,200	180	280	.000	-01.0	B48
888	478	500	480	.675	.778	614	956	828	680	800	.400	.608	-1.270
888	.878	.880	.600	.775	.884	.653	956	-025	.880	.700	.076	.614	1.010
857	-,050	.150	800	.600	. 650	769	957	100	-,100	100	.400	.447	-,294
636	075	100	050	.775	1.028	+.078	950	.650	.750	.550	.800	.867	1.144
859	225	800	-,150	.325	.408	-,860	959	526	560	-,500	.578	.663	794
860	.150	.200	-1.500	.425	.817	.290	960	878	-,800	700	.075	1.016	068
861	.575	.300	.850	.825	.005	.894	961	.800	.100	.800	.800	,540	1.095
861	-450	360	550	.400	.438	-1,027	968	375	1.000	500	1.100	1.365	.871
	075	880	.100	.738	.948	080		-1.486	-1.400	7,750	.438	1.634	-2.650
863		500	050	.000	.939	.068	964	100	-1.00	.000	.550	.007	.190
884	.050	050	000			.180	905	.100	.350	050	.550	.044	
865	.175			1.325	1.461			.125					.155
866	-,100	060	180	.400	-420	258	966			.250	.836	.087	.162
867	.100	.050	.180	1.800	1.210	.085	967	.775	1.050	.500	.728	.685	.042
668	~.800	.050	480	.680	.784	~.866	908	.485	.800	.580	.728	.769	.863
869	.178	.150	.200	.875	1.081	.171	969	.800	.650	.860	.400	.459	1.766
870	400	380	~.480	.400	.584	749	970	025	-060	100	.325	.877	-,066
871	.885	.200	.480	.485	-460	.706	971	225	400	050	.668	.636	260
878	.680	.900	-600	.650	.770	.854	972	825	100	380	.878	.680	846
875	526	580	500	-625	.698	476	973	-080	050	.150	.375	-471	.106
674	.725	1.000	,480	,613	.729	.995	974	.480	,680	.250	.780	.925	.488
878	.600	.688	,380	.650	.791	.708	975	800	,300	700	.450	.680	930
876	225	350	100	-675	.098	365	976	600	680	550	.400	.474	-2.868
877	-425	.700	.150	.978	1.817	.349	977	-,206	B00	.100	.780	.926	818
878	.846	.850	.400	-685	.654	.51.5	976	976	360	100	.075	.084	-6.468
879	.200	-150	.480	.380	.416	.718	979	-460	.500	.400	.680	.600	.678
880	1	100	.100	.BO0	.683.		980	1.280	1.880	1.250	1.080	1.168	1.078
881	300	400	-,200	-400	.456	666	981	128	-, 360	.100	.468	.854	226
888	475	500	450	.025	.817	588	988	.088	.850	100	.668	.817	.OEL
885	150	860	080	.780	.814	184	965	350	850	360	.660	.889	686
884	180	1	.500	.345	.390	.384	984	076	1	-,150	.168	,100	501
865		.420	.850	.150	.179	8.515	986	100	.880	680	1.850	1.518	066
886	.450 .275		.860	.775	.904	304	986	.100	,100	.100	.080	.071	1.400
887	.550	.800	.800	.950	1.185	.480	987	388	-,880	400	1.130	1.607	800
	.700	.500	.900	.600	.756	.968	986	.125	100	.180		.061	.838
686		.860	1.150	-800	.730	1.057	989	-,825	260	100	.078	.678	356
889	1.000	.560	1.100	.176	.007	230	990	076	180		1.578	.811	841
890	.080		.100	.300	.361	1.108	991	400	320	450	.380	.406	065
891	.400	.400		1.150		.860	1 55	178	300	-,100	.488	.580	-,518
898	.728	.750	1.080		1.800	.188	993	.400	.580	2200	1.880	1.394	.887
895	.075	-,100	.250	.415		730	1 200	800		-,500	.680	1.797	
894	078	500	650	.775	.798		995	876	1.000	450	1,868	1.810	.188
898	.185	.100	.150	.866	.618	208	900	1.150	1.880	450	1.850	1.171	.182
898	-1.125	-1,000	-,580	.485	.460	-8.445	997			700	-900	.970	928
897	425	080	-,800	.688	.801	561		000	-1.100	100	475	.861	801
898	100	.150	360	.550	.676	148	940	-,178	-,280	100		277	1.175
899	225	250	0	1.076	1.098	805	999	.865	.200	.180	.720	.B44	296
900	250	-,680	.080	1.080	1.201	-,206	1000	-,250	680	.160	,780	.000	546

TABLE E.—STATISTICS FOR DRAWINGS FROM RECTANGULAR UNIVERSE

Sample Mumber	¥	σ		Sample Humbe r	¥	σ	3.	Sample Mumber	I	σ		Number Number	Ŧ	σ		Sample Number	Ī	σ	*
1	026	1.112	028	101	175	1.126	155	801	-1.100	1,239	+,888	501	.425	1.511	,285	401	.628	.779	.805
- i (	.650	2.045	.518	108	.525	1.418	.570	202	.050	1.579	.056	508	.650	1.656	.594	402	825	1.178	704
5	.825	1.542	.535	105	1.600	.765	2.555	203	.625	1.754	.860	505	1.675	.789	2.120	405	.850	1.195	.718
4	.475	2.041	. 235	104	.450	1.821	.896	204	450	1.040	.454	504	1.775	1.209	1,468	404	.475	2,178	.218
5	150	.785	-,102	105	.550	1.596	.21.9	805		1.701	0	805	.675	1.445	-467	405	675	1.695	590
6	.800	1.656	.489	108	.225	1.806	.185	206	.650	2.128	.505	306 507	.900	1.068	.648	406	-1.600	.667	-2.400
7	-1.175	1.348	878	107	.685	2.104	.397 .166	207 206	050 875	2,352	021	508	1.000	1.544	1.004	408	-1.850	1.548	.250 -1.525
2 1	150 .425	1.516	114	109	1.175	1.581	.851	200	-1.500	.698	-2.550	809	1.600	1.384	.434	409	-800	1.049	-764
10	480	1.141	594	110	100	1.412	071	210	-,925	1.139	818	810	525	,947	554	410	.200	1.377	146
ii	.650	1.846	.638	iii	-,485	1.807	358	211	.800	1.061	.754	811	025	1.784	014	411	-1.600	1.358	-1.550
18	-1.600	.636	-2.516	118	.425	1.454	.896	818	100	1.695	591	818	.625	1.467	.426	418	.125	1.114	.112
15	-1.550	.765	-2.051	115	1.175	1.005	1.171	215	-,676	2.078	277	515	-,500	1.458	544	415	.825	1.217	.680
14	.200	8.031	.098	114	-1.175	.415	-2.851	21.4	.785	.873	.650	31.4	1.100	1.475	.748	414	2.225	.497	4.480
15	-1.000	1.842	745	115	-476	8.087	.228	216	8.025	.426	4.754	81.6	250	1,155	281	418	1.150	1.687	.610
16	375	2.017	186	116	075	1.610	047	216	.150	1,950	.077	516	1,550	1.518	1.510	416	700	1.991	352
17	600	1.508	598	117	1.550	.868	2.728	217	.876	2.047	.154	817	.975	1.908	.510	417	.075	.998	.075
18	1.075	.680	1.706	116	.225	8,024	,118	218 219	1.000	2.185	.069	518 519	150 .450	1.278	138 .254	416 419	.925 675	1.678	404
19 20		1.595	-,158	119	275	2.143	150 503	220	050	2.095	024	250	.075	1.955	.039	420	.875	2.014	285
81	175	1.186	.370	181	950	1.001	879	881	1.550	1.211	1.115	521	800	1.298	155	481	175	1.059	164
22	1.800	.765	2,358	122	1.125	1.001	1.124	122	1.175	8.070	.568	548	800	1.875	107	422	400	8.108	190
23	-450	1.521	.896	128	485	1.540	876	225	750	1.991	.877	525	475	1.504	817	425	1.025	1.040	.985
34	.350	1.595	.219	124	,825	1.836	.286	284	.225	1.677	.134	584	.125	1.956	.065	424	.125	1.047	.119
25	.225	1.806	,185	125	-,050	1.689	030	225	-1.250	1.040	-1.802	525	1.575	.958	1.640	425	.150	1.410	.108
26	.625	1.575	.597	186	975	.775	-1.261	226	375	.646	580	526	500	1.946	258	426	-,225	1.652	159
27	.350	8,104	.166	187	.450	1.590	.285	227	500	1.461	842	527	.100	1.737	.058	427	675	1.548	500
28	-1.575	.795	-1.981	188	.050	2.205	.025	226	-1.225	1.544	911	528	400	1.605	249	428	925	1.874	568
29	.550	.868	.405	189	.425	1.571	.271	289	1.476	.580	2.545	329 830	.825	1.665	,156	429 450	1.550	1.917	6.190
\$0	1,500	1.358	1.105	150	.650	2,065	.315 121	850 831	1.450 .550	.687 .868	8.111 .406	851	1.050	2.286	-460	431	.775	1.580	491
\$1 54	.500 750	1.955	.259 406	151	176	1.45R .684	141	832	-,250	1,528	188	532	.500	1.690	,178	458	.200	1.895	106
38	.025	1.240	.080	188	100	2.348	.045	255	875	1.705	814	855	.125	1.578	1089	435	975	1.717	568
34	350	1.820	268	134	-1.000	1.558	644	854	8.178	4698	5.116	834	-1.000	.634	-1.200	454	375	.701	858
36	650	1.741	2.578	135	.650	1.467	,445	835	.050	1,110	.045	835	.676	1.601	.51.9	455	1.075	8.385	.450
86	1.025	1.929	,581	186	.450	1.526	.054	286	.450	.994	1458	556	-1.150	1.770	-,650	436	.600	8.051	.295
27	425	1,168	~.556	187	825	1.542	034	237	.750	1.509	-466	357	275	8,087	132	437	500	1.955	155
58	1.125	.769	1.465	158	1.500	.658	1.968	838	.150	1.518	-114	558	-1.050	1.754	605	458	-1,750	.641	-2.080
89	. 0	1.754	0	139	1.150	1.284	.696	259	075	1,538	654	539	500	1.454	209	459	.450	1.958	.250
40	175	1.038	169	140	500	3.465	-,128	240	985	8.072	446	540 541	.075	1.027	.041 .569	440	.685	.864 2.260	.077
41	500	1.071	176	141	4.800	1.366	686	841	~.026	1.671	-,015 -540	548	.775 .825	1.561 2.005	.161	448	-850	8,168	369
44	1.075	1.879	.841	148	800 585	1.699	471 156	845	1.000	1.830	.874	545	975	1.980	810	445	-1.575	. 769	-1.050
48 44	1.500	1.492	216 .886	144	,975	1.285	.759	244	800	900	-,222	544	575	8.087	277	444	450	1.787	.857
45	625	1.639	340	146	.725	1.108	.054	845	.800	1.991	.151	846	250	8.171	.175	445	1.625	.608	2.700
44	.050	.658	.076	146	.800	1.969	.254	246	-1.885	1.048	-,717	B46 .	-1.825	.755	-2.450	446	650	2.058	516
47	-1.175	1,618	726	147	485	1.165	-,365	847	.025	1.706	.015	847	-,500	1.007	470	447	.025	1.828	.020
46	.400	1.911	209	148	-,185	.286	487	248	-1.175	.817	-1.458	548	.678	8.159	*278	448	-1.100	.898	-1.550
49	.485	1.458	. 292	149	1.500	.464	8.238	349	,280	2,086	.180	549	1.080	8.001	.524	449	050	1.767	088
50	1.180	1,004	1.145	150	-,700	1.549	519	850	500	2,099	-,258	850	.626	1,480	.570	450	075	2.160	-,035

# APPENDIX II

Bl	.725	1.086	.660	161	•••0	1.906	316	251	,650	1.727	.37 6	861	.326	8.208	.144	633	.900	1.778	.808
54	.978	.438	8.257	154	.848	1.984	.168	200	.200	.962	.206	300	178	1.786	096	408	-,978	1.978	-, 368
63	600	8.125	262	256	-,425	1.602	226	256	.780	2.204	,838	806	-,125	2.494	087	4.08	880	1.041	200
84	.275	.701	.502	184	628	1.540	466	284	-,475	1.021	445	364	1.880	,007	8.886	484	.200	1.405	. 300
66	-1.700	.696	-8.448	185	.600	1.595	.374	200	-1.225	1.295	-1.028	350	080	1,068	~.048	488	,978	3.065	. 678
56	:450	1.841	.344	156	875	1.754	.000	256	1.875	1.356	.947	356	1.885	.008	1.372	454	1.078	1.173	1,34
27	825	1,232	670	187	1.100	1.151	.986	8.07	.676	1.048	.410	307	.380	1.700	:106	407	.800	8.098	,189
86	.900	2.108	427	108	.878	1.192	.53.6	200	080	1.690	-,027	300	,365	1.808	.816	404	476	1.400	324
89	.926	.060	.964	100	1.600	.925	1.720	800	1.078	1.301	.886	350 360	075	2.825	027	480	680	1.968	551
60	,850	1.445	,009	160 161	-,500	8.000	840	260	850 -1.650	8.060	411	361	880	1.626	-,406	460	.178	1.000	.094
61	678	8.050	589		.678	2.007	.866	961 868	175	.960 .867	208	<b></b>	.185	1.600	.031	441	980	1.000	-,470
62	-1.580	1.161	-1.16B 064	168	1.178	2.003	.868 197	868	- 578	1.118	517	365	188	3.274	088	443	-1.478	1.604	8%
65	100	1.840		164	600	1.360	441	304	- 125	1.021	006	864	-1.078	1,808	-1.480	1	300	1.600	
64	-,100	1,979	106	168	200	2.618	007	208	,878	.886	388	200	.800	1.750			,786	8.188	.341
65 56	.628	1.608	.83.3	106	300	8.426	124	260	200	1.678	110	100	.180	1.053	.002	464	400	8.194	-,182
67	850	1.712	.146	167	880	8.138	598	867	.800	1.448	.349	807	.800	1.640	.490	407	1.075	1.400	.706
66	-1,800	8.043	387	100	.875	1.099	790	266	.580	1.107	-470	300	-,200	1.849	100	466	-1.178	1.008	000
69	.500	1.345	.161	100	.815	1.878	.647	269	.885	8.854	.101	300	400	1.680	-,847	440	-,900	,908	-,907
70	500	.718	696	170	.185	3.188	.881	870	185	1.006	184	970	380	1.165	500	470	-2.078	.340	-8.046
71	1.050	,591	8.688	171	075	1.965	038	271	.825	2.136	,108	371	-,825	8, 200	360	471	775	1.754	447
72	1700	1,068	.689	178	078	1.601	468	278	850	3.919	-,180	578	.545	1.008	.866	472	.888	1.888	.448
75	.250	1.704	-147	178	.628	1.137	.860	275	025	1,299	110	975	-,400	1.738	-, 238	478	080	1.401	086
74	478	8.306	23	174	.100	2,715	.057	274	-1.680	.934	-1.771	874	.800	1.786	,168	474	1.100	1.081	1.066
78	-1.045	1.897	790	178	180	,6B7	218	276	.980	1.178	.611	370	-,900	1.461	618	478	-,375	1.958	-,194
76	1,850	1,850	,685	176	.850	1.068	.800	876	.725	8.079	.840	376	-1,080	1.480	-,788	476	.400	1.966	.908
77	1.845	1.968	.677	177	-1.000	1.870	-,828	877	.880	1.007	.600	577	.486	1.880	.514	477	. 880	1.880	961
78	.180	3. 684	.060	178	1.600	1.544	.907	270	.925	1.884	-,586	270	-,300	1.687	-,188 -1,006	471	-1.078	1.496	848
70	1,550	1.872	.859	179	800	1,839	-,646	22	-,645	1.871	516	200	180	-441	346	1 200	.600	1.078	.341
80	-,650	2,110	508	180	.200	1.565	.181 461	1 m	450	1.890	360	<b>B</b> 1	.976	.844	1941	4	1,900	,886	8.146
63	-,950	1.768	587	181	900	1.994	180	-	850	1.878	.580	l Si	.480	1.604	.861	443	986	1.498	680
88	028	1.984	018	188	-1.700	1.098	-1.888	285	-1.688		-1.800	202	-1.888	1.801	-1.108	405	-1.878	1.004	650
88 84	400	1,100	.107	184	7.786	1.888	588	204	1,080	1.880	.854	204	.100	.800	.166	404	-,100	1.861	068
88	850	8.277	373	188	.625	1.960	-8.0	888	-1.880	1.899	659	806	-,700	.061	081	485	.225	1.987	.175
88	-1.850	1,384	013	186	-1.845	.976	-1.808	200	.676	1.401	.006	896	.625	1.600	.541	486	685	1.618	507
87	-8,880	296	-7.601	187	-1.450	.910	-1.895	287	1.250	1.059	1.168	78.7	8.976	.865	6.710	487	1.625	.801	3, 178
فقا	-1.100	1.118	984	166	1,175	.968	1.814	286	.076	8.186	.271	396	125	2,084	084	480	.800	.663	.458
80	.150	1.891	.116	189	900	1.100	770	200	.400	8,298	.178	200	1.678	1.844	1.480	489	1,400	1.971	1,799
90	1.926	.735	8,626	190	.500	1,048	.485	890	1.268	.769	1.660	800 801	-1.785	1.074	-1.480	401	580	1.570	433
91	1,345		1.656	101	.900	9.000	.451	801	+400	1.450	.085	302	880	.898	618	402	478	1.870	574
98	750	1,770	484	768	.478	.640	,860	292	.080	2.016	.688	201	.888	.990	,245	406	.600	1.111	.480
93	728			195	1,008	1.124	1,080	395 394	1.000	1.806	1,100	201	.800	1.768	.488	494	-,085	1,005	685
96	128			194	1.575	1.686	.968 -1.180	205	1.788	.760	2.870	808	.600	8.01	.184	495		2.970	0
98	1.400		1.310	196	-1,400	1,880	045	200	-,880	1.079	100	304	475	1.302	-,842	406	.900	1.826	. 493
96	-1.725	1.474		196	075	14550	874	807	675	1.45	400	807	.400	1,086	.980	497	575	1.690	340
97	-1.600	1.882	-2.186	198	800	1.000	-,197	200	1.188	8.000	.860	300	.680	1,906	.342	498	.175	1.471	.162
#	1.785			199	400	1.70	850	299	178	1.781	108	301	,800	1.084	.740	400	878	1.092	-,801
100	1.746		1.00	800	+.880	1.630		800	-1.178	1.641	717	400	.975	,986	,968	800	.228	.735	.307

Table E.—Statistics for Drawings from Rectangular Universe—(Continued)

Sample				Semple				Sample				Sample				Sample	,		
Reabor	7	0	•	Musber	Ŧ	ъ	•	Manher	¥	٥	•	Musbez		σ	•	Runber	¥	σ	
501 502	950 075	1.230 2.401	772 .050	601 808	950 1.450	1.295	1.459	701 702	.675 -1.725	.975	.694 -1.845	801 808	1,500	1.016	759 .950	901	1.425	1.045	1.565
903	150	1.534	098	803	.075	1.254	.060	705	-1.875	1.040	-1.805	805	1.475	1,707	.840	905	1,575	1.008	1.562
504	1.000	1.768	.565	504	.650	1.704	499	704	-1.300	.815	-1.595	804	.625	1.235	.505	904	.950	1.770	.536
505	-1.225	1.045	-1.176	605	176	2,255	076	705	925	1.417	655	805	1.500	1.225	1.062	905	575	.978	584
506	.300	2.176	.126	606	400	1.619	247	706	575	1,152	499	B06	-,325	1.595	204	906	1.400	.946	1.480
507	1.375	1.686	.845	607	876	1.105	540	707	.075	1.176	.064	807	.175	1.853	.094	907	-1.975	.769	-2,568
508 509	950 325	1.137	839 148	608 609	650	1.817	568 -1.015	706 709	.750 .375	1.479	.507 .190	808 809	.700 .225	1.602	,437 ,156	908	825	1.418	581 .109
510	.275	1.511	.185	610	-1.150 .125	2.005	.062	710	025	1.698	015	810	-,100	1.214	062	910	1,500	1.576	.952
511	-1.025	259	-3.951	611	1.160	.986	1.166	711	-1.650	459	-5.759	811	-1.950	250	725	911	-1.700	711	-2.590
512	350	2.103	166	618	1.750	4887	1.975	712	-,200	8,241	089	818	525	1.497	285	912	1.375	.981	1.401
515	.475	1.516	.365	615	.250	.971	.267	715	.400	.604	.662	815	.050	.492	.102	915	-1.725	.870	-1.981
514	.050	1.742	.029	614	725	1.846	395	714	1.750	1.879	.951	814	-2.150	.765	-2,810	914	-2,400	.676	-8.556
515	-1.600	1.084	-1.761	615	576	1.150	506	715	.150	1.176	.128	815	.925	.942	\$968	915	950	1.258	755
516 517	.550 575	1.159	.510	616 617	225	.691	-,326	716 717	.276 .800	1,279	,284 ,526	816 817	775	1,929	.117 590	916 917	1.400	8.004	555 .699
518	475	1.814	260	618	-1.150 -1.925	1.197	961 -1.517	719	875	1.557	654	818	-1.025	1.148	-1.682	918	-1.275	1.217	-1.098
519	.475	1.662	,285	619	1.450	1.071	1.364	719	.150	1.563	.108	819	.800	1.887	.683	919	-,950	1.927	492
520	.250	1,539	,187	620	-,325	1.620	214	720	2.175	.512	4.248	820	.080	1,524	.055	920	1,050	1.226	856
521	.950	1.727	.660	621	725	1.215	597	721	.525	1.712	.307	821	-, 226.	8.171	104	921	1.550	1.110	1.599
522	.675	1.025	.660	628	-,750	1.741	451	728	.175	8.029	,086	622	.525	1.150	.471	922	1.426	.942	1.510
825	1.125	1.750	.650	625	1.728	.722	2,589	725	.975	2.019	.485	685	400	1.070	574	925	-1.625	.628	-1.695
524	025	1.890	018	624	.200	1.369	-146	724	.100	1.308	.076	824	775	1.865	560	924	-2,000	339.	-2.450
525 526	-1.200	1.762	-,681	825 - 826	.125 .876	2.068	,060 ,425	726 726	1.500	1.156	1.126	825 828	1.600	1.252	1.699 -1.561	925	900	2.061	747
527	2.175 -1.650	1,186	2.688	627	400	2.125	.188	727	1.000	.977	1.025	827	.276	1.078	256	927	525	1.159	461
528	-1.925	.895	-2.156	628	-1.825	1.215	-1.008	728	800	1.795	446	828	.725	870	635	928	.600	2.104	.284
529	-1.100	.951	-1.167	629	-1.450	.879	-1.650	789	1.475	1.565	1.001	829	-1.850	1.429	-1.295	929	1.225	1.279	.959
550	,250	1.590	.160	650	225	1.777	127	750	.460	1.655	.875	850	1.885	2.284	.556	950	-1.500	1.384	-1.081
531	100	2,378	*.04Z	651	-1.425	.763	-1.868	731	.825	1.545	.634	851	525	1.656	517	<b>∮31</b> ⋅	-,850	1.797	47€
532	500	1.745	172	632	700	1.765	397	738	1.550	.450	5.000	852	500	2.518	216	958	776	.873	669
585	.900	1.288	699	688	850	1.544	551	735	-1.478	1.956	765	835	-1.475	1.502	982	955	.500	1.377	.218
554 555	325	.934 1.428	348	654 655	-1.125	1.445	779 104	754 735	.050	1.588	.051	854 855	-8.450 -475	.427 1.425	-0.745 .534	954 955	.050 .525	1.781	.028
-556	.500	1.326	.226	656	-1.100	970	-1.154	756	.575	1.021	.267	656	900	1.177	.766	936	-1.050	2.529	461
557	1,200	1.168	1,027	687	-1.775	.51.2	-5.467	737	-,800	1.455	650	837	-,950	1.895	755	957	-,850	1.774	479
558	1.600	2.024	.791	658	-,425	.471	908	758	.525	1.184	.274	656	-,175	1.650	106	958	200	.745	.268
539	500	,735	408	659	.576	2.179	.364	759	.250	1.521	.164	859	~.375	1.954	198	959	-1.625	1.645	989
540	.600	.686	.677	640	.775	2.125	,565	740	-1.275	1.580	607	840	1.100	.255	4.520	940	600	1.951	-,524
541	.700	1.810	.307	641	.500	2.457	.122	741	1.100	1.688	.652	841	425	.884	481	941	550	2.055 1.819	267
542 543	1,300	1.221	1.065	648 643	675 875	2.084	50.0 420	748 745	125	1.846	068 .280	842 843	675 ,600	1.197	564 508	945	-,150 -,675	.487	-1.307
544	.100	1.482	.087	844	1.250	8.129	.587	744	-1.650	.684	-8.605	844	400	.851	481	944	.075	.795	.094
545	1.600	.919	1.741	645	1.550	.643	8.414	745	826	1.699	486	B45	625	1.259	505	946	325	1.827	178
546	.325	1.797	.186	646	978	2.014	484	746	.800	2,250	357	846	.675	1.647	.409	946	1.876	.602	3.115
547	200	.951	210	647	1.050	1.901	.562	747	-1.425	1.555	-1.055	847	.025	1.851	.014	947	350	2.179	~.161
548	1.725	.779	8.214	648	.775	1.404	552	748	.825	1.502	.549	848	-1.200	1.259	970	948	525	.915	574
549	-1.475	.895	-1.648	649	-1.400	1.896	-1.004	749	500	2.125	141	849	1.575	1.669	- 945	949	060	1.986	-,025
550	.400	1.991	.201	650	025	1.858	014	750	.360	-466	.751	850	200	1.435	159	950	275	1.964	140

561	028	1.171	OE1	697	.850	1.145	.744	751	.500	1.084	.276	881	.775	.923	.830	981	1.500	1.613	1,091
558	.176	1.659	.107	602	.628	1.165	.866	758	600	1,806	335	852	275	8.078	+.186	954	.475	1.900	.483
808	600	.718	-,836	606	200	1.020	110	768	.060	.868	.000	859	1.345	.798	1.671	155	880	1.178	469
884	380	1.968	178	654	.380	.776	.451	754	.628	.975	.642	854	-2.700	.902	-1.731	954	1.478	.680	8.841
888	.480	2.207	.204	658 658	825	1.803	886 .229	755 756	478	1.287	369	858 864	-1.880	2.025	,146	955	-1.800	1.108	-2.180
806	1.800	.406	1.960	607	.000	1.883	.478	787	.525	1.397	.275	857	-1.550	1.965	706	954 957	180	1.667	.851
888	628	1,840	804	458	1.800	2.332	.807	788	728	1.838	472	Ana	-1.778	.749	-8.80	950	378	1,594	263
509	450	2.143	210	600	-1.000	1.858	540	759	478	1.794	208	851	-1.000	1.170	085	950	.878	.634	.008
860	625	1.785	308	660	-1,078	1,455	734	780	.875	1.378	.656	860	1.800	1.745	.688	900	450	1.980	-,830
861	200	1.785	110	661	.278	.988	.267	761	.480	1.610	.279	861	880	1.000	018	961	778	.004	877
568	-1.800	.785	-8.485	662	.800	8.210	.561	762	178	1.242	141	848	.096	.963	.088	968	.178	8,838	.078
868	.075	2,014	.037	668	650	1,638	397	768	050	1.770	~.018	868	485	1.706	342	968	.125	.061	.109
864	-600	1.061	.566	604	080	1.755	029	764	925	1,937	478	884	.075	8, 091	,086	964	.880	.007	1.830
565	.600	1.168	.514	666	428	1.848	-,830	765	.678	1.266	.404	868	.575	1.676	.224	988	.980	1.480	.688
866	-,850	.669	-1.R71	666	625	1.750	500	768 787	500	1.259	397 086	806 867	975	1.678 8.039	881 851	966	825	1.866	174
867 868	.380	1.883	1.725	667 668	1.475	1.621	.910 .205	768	100	2,803	.810	868	325	8.088	160	900	780	1.600	662
B69	1.525	1.805	.048	669	1.725	1.429	1,207	769	.500	1.851	.164	869	.078	1.885	.040	969	-,860	.986	-,862
870	1.025	1,159	.877	870	100	1.796	.088	770	-1.776	1.880	-1.480	870	050	2.108	084	970	-,875	.926	-,897
871	978	1.859	-,524	671	-,826	1.875	647	771	-,450	1,844	561	871	-,925	.164	-6.640	971	085	1.429	-,018
572	.600	1.608	.511	672	.650	.976	,668	772	678	1.366	499	878	575	1.684	504	972	.078	1.651	.166
675	1.500	.631	1,508	673	-1.400	.925	-1.514	773	-1.576	.746	-8.111	875	-,580	1.484	236	973	-,800	1.612	165
574	.250	1.947	,188	674	128	1.699	074	774	,550	1.064	.617	874	1.500	1.248	1.209	974	-1.850	.808	-8,661
575	350	1.471	238	676	-,326	1.845	176	775	.725	1.807	.063	875	1,225	1.489	.859	975	.875	8.170	.187
576	.475	1.308	.365	676 677	680	1.526	489	776	-1.325	.919	-8, 348 -, 934	876 877	.800	1.751	1.231	976	-1.800 .888	.894 8,066	-2.861 .256
577 578	825	1.339	927	878	275	1.861	-1.073	777	900	1.541	563	878	580	770	455	978	-1.278	1.148	-1.110
979	.825	1.866		679	275	936	894	779	-,650	1.365	-,476	879	.550	480	1.220	970	378	1.640	
580	680	.853		880	-1.200	.678	-1.770	780	.750	1.362	.864	880	.078	1.758	.043	980	-1.525	1.348	-1,221
581	-2.475	.311	-9.958	661	380	1.795	195	781	.150	8.008	.075	861	128	8.625	048	981	-,285	2.035	111
508	.575	.898	.840	681	.626	2.373	.263	782	075	.630	119	882	.475	.807	.588	988	.375	2,386	.178
568	-,850	1.778	478	688	-1.325	1.335	994	783	-,725	1.464	495	865	800	.962	610	968	.176	1.803	.126
884	1,680	1,188		664	.900	1.395	.502	784	025	1.907	018	864 865	+,850 -1,350	2.015	808 -1.988	984 985	1.378	.109 1.897	18.620
565	.500	2.304		565 565	-1.478	1.917	769	785 786	-1.325	1.006	682	886	100	1.715	.079	986	.100	1,894	.112
586 587	878	2.069		567	-1,450	743	-1.962	787	900	1.230	726	887	-1.025	1.117	919	987	.878	1.536	,244
588	800	.919		886	125	1,807	104	788	300	1.210	-,248	888	,080	1.587	.083	988	1.500	1.301	1.079
569	1.150	1.665		689	-1.128	.672	-1.674	789	-1.028	1.906	639	869	,978	1.846	.203	989	678	1.219	-,564
890	.900	8,083		890	-1.075	1.404	766	790	1.875	1.699	.751	890	625	1.561	605	990	100	1.805	055
591	1.025	1.401	.692	691	-,180	1.929	076	791	.175	1.590	-770	891	1.400	.696	2.018	993	-,600	1.802	609
502	,375	1.978		692	650	1.398	-,609	792	.175	1.642	.107	892	580 .950	1.920 2.159	206	992 993	050	2,029	025
598	.878	1.883		693	.200	.000	.202	793 794	-1.025	1,412	040	893 894	575	.740	-,779	995	.025	1.820	.014
594	,160	.681		694	.225	2,073	060	795	325	1.627	199	895	680	.921	708	998	050	1.613	031
596 596	900	1.194	.754	695	185	1.942	060	796	200	.574	.548	896	-,475	1.502	50.6	996	.700	.930	.754
507	675	1.810		697	478	1.874	.573	797	-,600	1.847	328	897	. 223	1.184	.190	997	-,800	.615	981
1 598	.680	.001		698	400	.808	-,792	798	875	1.431	400	898	-1.375	.861	-1.596	998	125	1.756	071
899	575	8.08		. 899	-1.425	.981	-1.453	799	-,225	1.942	116	899	-1.675	1.840	-1.087	999	1.175	1.488	.025
600	.850	8.18		900	.750	2.254	.536	800	-1.750	.208	-8.500	900	900	.728	-1,858	1000	600	1.052	370
_			<del>'</del>						-										

Sample Sumber Sample Mumber Sampla Number Sample Sample ¥ 7 σ 101 102 103 -617 .128 1.422 .025 .500 -.178 .700 .590 .575 .025 -.275 1.021 .024 -.424 .762 .055 -.767 205 .618 1.262 1.089 1.118 .674 .298 .154 -.225 -.591 -.445 303 304 305 306 307 308 309 310 311 313 313 315 316 400 .658 .613 -.169 -.790 .681 .633 .197 -.082 -1.050 .400 .375 .661 .567 -.776 .567 .593 .635 .610 .360 .495 .494 .575 204 205 206 206 208 209 210 211 212 213 214 .378
-.500
.425
.050
.025
.100
.200
.250
.076
-.550
-.550
.626
-.750
.375
.178 -.075 .708 -.106 -.450 -.656 -.738 -.820 .125 .755 1.070 .234 .360 .563 -.450 .610 .050 .050 .050 .200 .125 .025 -.525 .918 -.490 .049 .058 .132 .025 0 .366 -.169 .024 -.095 -.399 .108 .675 .336 -.374 -.062 1.870 -.050 -.400 .064 .640 1.190 1.110 1.308 1.010 .875 .525 .776 .961 -.200 -.404 -1.450 .815 .735 .725 .123 -.050 -657 -.076 -.045 .708 1.098 .272 .656 -.591 .338 .346 .112 .125 .085 .045 1.195 -.225 -.200 .695 -.888 -1.005 1.035 .616 .512 .507 .559 .567 .540 1.001 .350 .671 .770 -,125 .661 -,189 -4.065 1.099 -.714 .175 .718 -7.559 .550 -.175 .025 -.100 -1.030 .955 1.035 1.035 .695 -.989 -.910 -.525 -.791 -.675 17,330 £15 216 217 218 219 220 .325 .641 -.447 -.220 .694 .725 .901 -1.055 .660 1.050 -.600 -.250 -.125 -.400 .720 -.555 .456 -1.061 -.679 -.788 1.056 .739 .660 .696 1.239 .444 -.509 -.700 .759 .766 .536 .539 .683 .705 .678 .672 .685 -.880 .041 .359 -.911 .28B 2.379 -.4E5 -.250 .078 .800 .200 -.175 .225 -.050 .828 -.028 .150 -.325 .700 .627 -.475 .025 -694 .602 -,748 .626 .576 .577 1.185 .225 -.748 .601 .179 -.385 1.146 1.025 -.865 -.085 -.151 .855 -.465 -.229 .604 .676 .618 -.525 -.350 221 225 225 226 227 228 227 228 227 230 231 232 235 236 236 237 236 240 241 242 244 245 244 247 248 249 249 240 247 .110 1.325 1.156 -2.095 -.035 -.450 .459 .452 5.212 .148 .148 .166 .141 .141 .141 .158 1.150 -.450 -.780 -.575 -2.196 .641 .462 .510 1.185 .610 -.325 .650 -.775 -.507 1.349 1.600 -.075 .661 -.405 .608 .592 .100 .662 -5.725 -1.520 .575 6.725 .253 -.522 1.193 .758 .758 .675 .595 +.575 -1.115 -.152 -.375 .776 .758 .878 427 428 429 -7.098 .628 .492 -.225 -.750 -.457 -.396 -.350 -6.650 -1.495 -.111 -.200 -1.265 .650 .625 .550 .250 .250 .885 .304 -.738 -1.336 -.886 .627 1.057 1.152 1.000 -475 -175 .558 .575 .576 .580 .536 .566 .604 .636 .742 .758 .691 .742 -.036 .376 .630 .595 -.345 -.157 450 451 458 455 456 456 457 459 440 441 448 445 446 447 449 449 450 -3.800 .800 .552 -.067 -.225 .653 .844 .796 .716 .635 -.425 -.444 1.267 .264 .445 -1.887 .455 .456 ~.318 -.775 -.475 -.175 -.100 .654 .578 -.276 -.175 1.136 .860 -.408 .548 -.314 .212 .180 .890 .898 1.010 .653 -.250 -.440 .655 .950 .215 .444 -3.599 .350 .100 .500 .150 -.600 -.828 .728 .775 .089 1.480 -3.056 .565 -.500 .500 .675 .998 -.400 -,775 .228 -.936 -.936 -.042 -.487 -.267 -.369 -.475 .875 -.425 -.100 -.050 -.250 -.548 -.727 .230 -.248 206 .550 .475 .586 .596 .695 1.498 -.750 -.600 -5.641 -5,220 -.371 .596 1.570 -.OE5 -.033 -.715 .167 .480 .300 .350 1.030 .250 .450 .550 .455 -.144 -.150 -.236 1.125 1.00E 1.010 .680 .718 -.074 -.125 .621 -.208 .058 1.160 -366 -.050 -,049 .650 -.125 -.128 .225 -.175 .5£8 -,£91 -1.091 1.162 .075 .425 .066 .572 -.025 .843 1.043 .608 .638 .638 .650 .723 -.225 - . \$68 - . 543 1.195 1.148 .580 -.161 1.141 -.425 -.407 -.425 -.666 -.200 . 583 .815 .523 .665 -.485 -.360 -.150 -.668 -.539 -.207 -.325 1.042 -.512 -.515 -.201 -,200 1.245 1.008 1.060 1.244 .950 1.064 1.034 .775 -.475 -.400 .659 1.750 -.728 -.681 .525 1.117 .875 1.438 .975 1.268 .470 -.175 -.164 .262 .653

TABLE F.—STATISTICS FOR DRAWINGS FROM RIGHT TRIANGULAR UNIVERSE

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51	.400	1,081	.970	151	628	.722	866	801	300	.772	434	2003	800	.058	295	450	.000		
£2 53	-325	.988	.280	184	.880	.439	1.256	858		.758		354	+,226	.630	307	454	086	.304	1.900
54	.180	.930	.101	155 184	700	.436	-1.750	205	.178	.728	.844	\$65	800	.426	810	480	625	.441	-1.480
55	025	1.006	026	106	800	.486	418	254 255	.050	-666	.076	254	078	.041	117	454	900	.410	-6.156
56	380	.638	549	104	500	474	-1.058	256	1,000	-665	1.816	505	800	.716	278	456	175	.409	~45
27	425	1.112	388	157	125	830	236	257	.178	-779	1.440	804 857	- 400	.758		454	.080	.430	-114
<b>56</b>	.228	1.081	.300	188	67B	.490	-1.375	808	825	-669	336	308	550	.610 .610	728	407	380	.496	708
59	600	1.100	845	150	336.	-490	1.070	839	250	.697	-,308	800	070	.676	800	420	178	.580	1.840
	300	1.008	290	160	-,450	.402	916	B6Q	378	.789	478	860	.100	-006	1144	460	-,700	.976	-1.107
92	175	.478	165	181	-325	.792	-410	261		.824		861	-,200	.490	408	461	1.025	.876	8.710
33	70C	.485	.893	162 163	.880 .825	.740	.475	868	-,125	.737	-,169	362	.026	.421	.059	448	.125	.877	-481
14	.200	.485	.413	164	625	.443 .887	1.823	263 264	.025	•740	.054	863	-,080	-409	124	468	775	.218	-8.880
65	525	.615	1.020	165	47B	1448	-1.060	145	.128 050	.780 .783	.167 064	364 368	250	-458	880	464	-,800	,800	-1.500
68	.080	1.169	.043	166	578	.449	835	266	-,830	.758	264	366	.725 -,425	.476	1.588	468	-1.000	.886	-3.922
67	.975	1.058	.921	107	825	400	-1.180	167	-,275	.926	297	367	825	-376	-1.127 -1.50a	466	-1.000	#844	-4.260
68	.050	.996	.050	168	.125	.438	.265	866	.125	-698	179	300	300	.413	729	1 22	750 750	.220	-8.278
69	.778	.981	,790	169	575	.48)	-1.368	269	,125	.708	.177	869	175	.206	44	449	075	.849	-3.575
70	.200	.967	.807	170	050	-415	121	270	.775	.729	1.068	370	-,850	-394	-,630	470	050	.486	117
71 72	.050	.986	.152	171	.460	-450	1.000	271	.050	.740	.068	871	.800	-611	.327	471	900	300	-8.888
75	500	1.039	291	172	725	.440	-1.650	878	125	.718	174	372	.650	-608	1.078	472	.880	, 863	3.010
74	050	.978	051	174	275	.480	570	273	200	.680	304	878	185	.658	101	478	+,225	.818	~.708
	300	1.008	296	176	878	.482	-1.610 -1.193	275	.100 676	-736	919	974 975	.885	-636	.368	474	.685	.839	8.027
76	.025	1.141	.022	176	678	403	-1.400	276	485	4660	044	876	-,425	.608	784	475	-,275	.268	-1.086
77	.725	1.140	.637	177	.050	435	.116	277	375	.660	.868	377	225	.866	- 863	476	.880 ,630	.300	8.840
76	.825	1.064	.775	178	.275	.438	,637	276	400	-702	.870	978	.400	-644	.663	478	,630	.296	8.440
79	.775	1.071	.784	179	478	.488	-1.019	279	+.500	.707	707	379	.675	.705	1.856	470	500	.874	-1.098
80	.525	1.849	.261	180	680	.427	-1.522	880	.050	.743	.067	860	.475	-901	.477	480	.680	.850	8.480
61 62	.160	1.230	-122	181	-,385	.436	548	281	475	.715	668	801	1 0	.592		401.	900	,300	-8,000
88	.625	1.169	,506 ,708	188 188	1,025	.769	1.355	982 985	,585	.661	.794	862	-,575	-590	968	468	-,650	.342	-1.905
84	.150	1.059	.148	184	.150	1.170	.128	264	300	-540 -718	469	385 384	725	-400	-1.318	488	375	.310	-1.E10
88		1.084		188	178	1.043	168	286	.100	.756	.138	366	150	-455 -364	418	485	350	.27.0	-1.098
66	-675	1.060	.637	186	025	1.030	025	200	-,325	.638	610	386	,975	-418	2.349	486	-,500	.363	-1.438 1.435
87	.725	1.060	.665	187	.176	1.171	.149	807	250	-686	-,364	807	800	.361	1,365	497	.500	808	.976
88	-160	1.198	.126	188	.650	7.009	.848	168	576	-905	815	368	750	. 584	-1.953	488	878	. 21.2	-8.736
89 90	075	1.180	068	189	378	.701	534	369	£25	-676	333	888	.576	.391	1.505	489	700	,891	-8.410
91	150	1.125	267	190 191	060	458	-,114	290	.775	.844	.916	390	.075	-370	.808	490	,250	.380	.781
92	300	1.168	.257	192	100	-464	-,216 -,531	291 292	178	.122	842 .733	301 302	325	-870	.878	491	-,400	.500	-1.335
98	.47B	1.064	.446	193	1,188	4.180	.955	195	900	-702	1.380	303	575	.358	2.340 -1.554	492 493	080	.336	149
94	.050	1.060	.047	194	850	1.846	201	194	125	.746	.168	304	900	.374	-2.406	494	500	. 354	-1.699
95	-150	1.074	.140	195	1,080	.187	-5.620	298	-,250	.730	343	395	400	.375	-1.070	495	900	. 363	-2.548
96	225	1.184	+,190	198	225	1.462	154	296	1.880	.808	1.580	396	.785	- 396	1.650	496	180	.378	307
97	100	1.009	098	197	-,350	- 335	-1.045	297	.475	.770	.618	397	775	. 502	-1.975	497	300	,33£	904
98 99	125 500	1.110	118	198	160	.929	161	898	275	.642	420	396	-1.000	-406	-2.468	498	100	400	250
100	078	1,134	868	100	.300	1.058	.385	899 300	.178	.661	.871	309	-,580	.801	-1.099	499	800	.400	-a.000
				1	1 .150	2,000	.148	, acc	-, 225	-657	342	400	.460	-805	.895	800	550	.296	-1.660

Sample Number	¥	σ	•	Sample Bumber	Ŧ	σ		Sample Pamber	¥	σ		Sample Mumber	7	ø		Sample Bumber	¥	σ	
501	175	1,050	178	601	450	.449	-1.002	701	325	.829	-,592	801	-,250	1.115	-,824	901	.850	1.059	. 256
808	.100	1.154	.087	608	480	.350	-1.286	702	485	1.008	.423	802	180	1.550	110	908	.475	1.055	.457
508	.700	1.065	.667	608	.050	.880	.145	708	. 250	.991	.252	808	150	1.510	116	908	.250	1.160	.216
504	.525	1.045	.808	604	.375	1.270	.295	704	.850	1.008	.348	804	150	1.225	125	904	.550	1.115	.483
506 506	.750 .878	.907	.827 .625	605 606	-075	1.865	.056 280	705 706	-,225	.856	36R	805	125	1.860	099	905	0	1.180	
507	100	.920 1.020	.098	607	100	1.225	082	707	-,188	.750	167	808 807	.425	1.145	.871	906	.350	.965	.368
508	.880	1.050	.825	608	425	1,230	546	708	275	.764	560	808	.826	1.510	.510 .178	908	-,125	.995	125
B09	. 278	.965	.205	609	.875	409	.818	709	.525	.760	-685	809	.850	1.588	.640	909	700	1.032	-678
510	.500	1,061	283	63.0	450	.476	945	710	250	-787	550	81G	.750	1.198	.689	910	500	1.027	.487
811	.075	,950	.079	611	.275	-465	.591	711	-,178	.625	-,212	811	.150	1.846	.120	911	.500	.919	.844
512	.888	.975	. 540	618	100	.510	197	718	.550	.757	.468	818	.078	1.880	.060	918	.425	,912	.466
618	.525	.966	.880	615	.100	.510	.196	713	.520	.798	.408	815	.125	1.220	.102	915	.675	.915	.757
514	175	.887	197	614	.250	1.850	.200	714	400	.886	451	814	.200	1,290	.158	914	.550	1.062	.350
515	125	.855	146	615	150	1,061	159	715	.880	1.159	.508	815	075	.856	.089	915	. 375	1.842	.501
516	.775	1.050	.756	616	.160	.866	.169	716	.480	1,143	.394	816	-425	.825	.816	916	.350	1.550	.259
517	.325	1.048	.312	617	.050	.898	.056	717	.476	1,234	.385	817	.100	.840	.119	917	.175	1.198	.146
978	025	1.146	028	618	025	1,008	027	718 719	.678 .160	1.119	.01.6	818 819	625	.844	741	918 919	075	1.327	057 078
520	.050	1.056	.579	619	1.000	.888	1.135	780	.625	1.101	.180	820	-,285 .450	.84E	-,268 -,868	920	100	1.881	.410
521	1.100	.943	1,168	621	.875	1.145	.508	721	.150	.750	.800	821	.850	1.455	.244	921	~,085	1.000	025
522	.025	.665	.286	888	.625	1,136	.850	722	.188	.804	.158	828	.178	1.470	.119	988	.550	1.060	.519
BES I	500	.925	~.825	685	.175	1.581	.129	725	-400	.821	.476	823	.878	1.234	709	928	****	1.090	
584	.025	.908	,028	684	.725	.795	.918	724	1.200	.822	1.460	884	.875	1,250	.700	924	.850	1.150	.751
B2B	.050	.961	.052	686	.225	.795	.283	725	. 250	.862	.290	825	.025	1.557	.018	925	-,200	1.148	174
886	350	.688	894	626	. 565	.817	.598	726	800	.750	266	888	850	1.419	847	926	<b>~.</b> 080	1.087	048
527	550	.885	595	627	.480	.854	.627	727	225	.875	-,258	827	.500	1.841	.242	927	.075	1.045	.072
528	.050	.887	.056	688	225	.815	676	728	675	.855	-,790	826	.175	1.846	.140	928	050	1.031	048
E58	275	.975	+.288	689	078	.680	085	729	.125	.885	.145	689	.150	1.884	.180	929	225	1.057	213
580	-,900	.995	801	650	+.275	.828	355	730	.250	.858	.478	850	.850	1.815	.454	950	.175	1.045	-167
561	1.000	.870	1.149	681	.800	.866	.908	781	.500	.765	.502	851	.480	1.820	.869	931		1,058	0
552	800	.986	-,208	658	050	.910	055	752	~.150	.789	+.190	658	.950	1.484	.640	938	.180	1.109	.155
555	-,875	.988	860	658	550	.655	-,411	788	.400	.828	.487	855	.475	1.470	.885	935	100 .025	1.118	.088
884 688	175	.998	188	654 655	-1650	.741 .785	875 1.841	734 785	425	.766 .820	518	834 835	.860 .878	1.265	.276 .295	934 935	800	1.160	172
856	.565	.978	.554	656	1.050	.758	.864	756	888	.880	874	856	.080	1.587	.036	956	575	1.145	-,388
557	485	.950	448	637	.800 400	.995	446	787	.300	.986	.894	857	125	1.417	088	937	400	1,110	588
556	125	.884	148	686	.876	.781	,552	788	.950	.901	1.054	688	300	1.455	806	938	125	1.108	115
859	100	1.068	-,100	659	350	748	471	739	.976	.795	1.826	839	150	1.477	108	930	526	1.091	298
540	150	960	186	640	685	.942	668	740	078	.746	101	840	-,460	1.848	868	940	. 376	1.040	.361
F41	.500	.857	.565	641	825	904	860	741	.850	.805	1.065	841	100	1.270	079	941	.050	1.097	-046
548	.400	,897	.446	848	800	.918	529	748	178	.898	-,198	842	.225	1.176	.191	948	875	1.112	.337
848	850	.844	298	645	.500	.897	.884	745	.050	.625	.061	845	250	.959	262	945	. 225	1.290	.174
B44	.565	1.040	.505	644	.015	.995	.025	744	.500	.926	.885	844	.150	.614	.184	944	500	1.178	256
845	.475	.995	.478	645	.976	1.455	.687	745	0	.867	. 0	845	.950	.800	1.190	945	.475	1.188	.400
546	015	1.08	024	646	.150	.864	.175	746	.100	.867	.878	846	028	.881	031	946	-,178	1.159	154
847	.800	1.809	.229	647	586	.665	490	747	.478	1.819	.590	847	450	.886	.538 .504	947	625	1.110	565 752
546	.900	1.180	.768	648	025	.918	027	748	800	.480	698	848 849	-,200	.844	804	949	.585	1.508	.702
849	.875	1.150	.808 .551	649 650	.850 .025	.907	.028	749 750	750 285	.470	-1.590 648	850	.476	.984	.510	950	.900	1.170	.770

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#### APPENDIX III

A BIBLIOGRAPHIC GUIDE WITH SUGGESTIONS FOR STUDY IN THE FURTHER DEVELOPMENT OF A SCIENTIFIC BASIS FOR THE ECONOMIC CONTROL OF QUALITY OF MANUFACTURED PRODUCT

As stated in the preface, the present book is but an *initial* step toward the formulation of a scientific basis for securing economic control. Much remains to be done. In presenting a list of references for further study, an attempt has been made to include those suggestive of what appear to be profitable lines of further development.

Throughout the book we have had occasion to give many specific references. The object of the present bibliography is to suggest references of a more or less general nature to be read in connection with each of the seven parts. It is hoped that in many instances these references will be suggestive of work which may be profitably done in extending the theory of quality control, particularly in the direction of the development of improved ways of securing good data through the more thorough application of the scientific method.

#### REFERENCES FOR PARTS I AND III

### 1. Exact and Statistical Laws

In Parts I and III the rôles of exact, empirical, and statistical laws in helping us to do what we want to do are touched upon.

The recent book, A History of Science, C. D. Whetham, 2nd edition, Macmillan Company, New York, 1930, gives an interesting and up-to-date survey of the results of human effort in establishing laws of nature. To get a more exact picture, however, we must turn to some such book as Introduction to Theoretical Physics, A. Haas, 2nd edition, Constable & Company, London, Vol. I, 1928, Vol. II, 1929; or the book of the same title by L. Page, D. Van Nostrand Company, Inc., New York, 1928.

With the development of the atomic structure of matter and electricity, it became necessary to think of laws as being statistical in nature. The importance of the law of large numbers in the interpretation of physical phenomena will become apparent to any one who even hastily surveys any one or more of the following books: Statistical Theories of Matter, Radiation, and Electricity, K. K. Darrow, The Physical Review Supplement, Vol. I, No. 1, July 1929, also published in the series of Bell Telephone Laboratories' reprints, No. 435; Introduction to Statistical Mechanics for Students of Physics and Physical Chemistry, J. Rice, Constable & Company, Ltd., London, 1930; Statistical Mechanics with Applications to Physics and Chemistry, R. C. Tolman, Chemical Catalog Company, New York, 1927; Kinetic Theory of Gases, L. B. Loeb, McGraw-Hill Book Company, New York, 1927; The Kinetic Theory of Gases, E. Bloch, Methuen & Company, Ltd., London, 1924; Introduction to Modern Physics, F. K. Richtmeyer, McGraw-Hill Book Company, New York, 1928; Modern Physics, H. A. Wilson, Blackie & Son, Ltd., London, 1928; Introduction to Contemporary Physics, K. K. Darrow, D. Van Nostrand Company, Inc., New York, 1926; and Atoms, Molecules and Quanta, A. E. Ruark and H. C. Urey, McGraw-Hill Book Company, New York, 1930.

One cannot return from even a brief excursion into the field of modern physics and chemistry without having caught a glimpse of the importance of the concept of the statistical limit in all of the latest developments. Even in this field of exact science nothing is exact. In the last analysis the influence of chance causes is felt. Almost the only things that appear to be constant are distribution functions or statistics of these functions—and this constancy is only in the statistical sense. For example, one interested in the specification of quality of materials need read only Chapter III of The Physics of Solids and Liquids, P. P. Ewald, Th. Pöschl and L. Prandtl, Blackie and Son, Ltd., 1930, to see how far we are from being able to explain some of even the simplest mechanical properties in terms of atomic physics.

# 2. Empirical Laws

To contrast the way in which the so-called exact and statistical laws enable one to predict with the way in which an empirical law does, the recent excellent book *Business Cycles*, W. C. Mitchell, Na-

tional Bureau of Economic Research, New York, 1927, should prove to be of interest. The author of this book discusses in a critical manner the very extensive amount of work that has been done in trying to develop a rational basis for predicting cyclic movements with a net result that is not so very encouraging. Even a casual reading of this book must impress one with the serious hopelessness of trying to predict the future in terms of the past when the chance cause system is not constant. In the present state of the scientific method of induction, it appears that empirical relationships such as time series give little basis for prediction. This conclusion is consistent with that so admirably presented in a recent paper by S. L. Andrew in the Bell Telephone Quarterly, Jan., 1931, and also with conclusions set forth in the recent book Business Adrift, by W. B. Donham, Dean of the Harvard Business School. Such reading cannot do other than strengthen our belief in the fact that control of quality will come only through the weeding out of assignable causes of variation—particularly those that introduce lack of constancy in the chance cause system.

## 3. Frequency Distribution Functions

In Part III we considered very briefly the problem of determining the kind of frequency distribution function or functions that we might expect controlled quality to follow. In this connection we touched upon the philosophy of frequency curves as laws of distribution.

Two systems of curves were mentioned in particular, namely, the Pearson and the Gram-Charlier systems. Although we have not had occasion to make much use of these functions as such, a serious student of control of quality will find it greatly to his advantage to read some of the original memoirs dealing with these two systems of curves. Those of Pearson are naturally available in English and cannot help but prove stimulating. The more formal part of Pearson's work in this field has been summarized by Elderton in the interesting book, Frequency Curves and Correlation, second edition, Layton, London, 1928. T. L. Kelley, a former student of Pearson, also has much of interest to say about this system of curves in his book, Statistical Method, Macmillan Company, New York, 1923.

Very interesting and stimulating accounts of the significance of the Gram-Charlier series have been given by Arne Fisher, Mathematical Theory of Probabilities, 2nd edition, Macmillan Company, New York, 1922; by F. Y. Edgeworth in a series of articles referred to in his article Probability in the 13th edition of the Encyclopedia Britannica; and by T. N. Thiele, Theory of Observations, London, 1903. J. F. Steffensen in Some Recent Researches in the Theory of Statistics and Actuarial Science, Cambridge University Press, 1930, makes some very interesting and pertinent remarks on the theoretical foundation of certain types of frequency curves.

It is of particular interest to note the way in which Edgeworth arrives at the Gram-Charlier series as a method of expressing the results of the joint action of a complicated system of causes. Of course, the Pearson system can be given somewhat similar causal interpretation although great emphasis has not been laid upon this point by many of those writing about the Pearson system.

The sythentic building up of a frequency curve in terms of the effects of component groups of causes forms a basis, as we have seen, for our discussion of the necessary and sufficient conditions of maximum control. We have emphasized the significance of the fact that, as the number of causes of variability is increased, we seem to approach closer and closer to what we have termed the point (0, 3) of maximum control in the  $\beta_1$   $\beta_2$  plane.

In this connection *The Behavior of Prices*, F. C. Mills, National Bureau of Economic Research, Inc., New York, 1928, should prove interesting reading, particularly that part having to do with the march of the  $\beta$ 's back to normalcy, as he puts it.

# 4. Probability

Probability and its Engineering Uses, T. C. Fry, D. Van Nostrand Company, New York, 1928, and An Introduction to Mathematical Probability, J. L. Coolidge, Oxford University Press, New York, 1925, contain interesting discussions of the meaning of probability and the difficulty involved in defining it.

# 5. Quality Control

The only book touching upon the subject of quality control in anything like the sense of the present text is that by Becker, Plaut, and Runge, referred to in Chapter I of Part I.

#### REFERENCES FOR PART II

#### 1. Economics

The problem of economic control of quality in its broadest sense is, as we have seen, that of doing what we want to do within limits which are economical. To do this, we must establish economic standards of quality. A brief outline of the economic considerations which must be taken into account in attempting to establish such standards of quality is given in an interesting article, "Standard Quality," G. D. Edwards, Bell Telephone Quarterly, Vol. VII, pp. 292-303.

For example, in establishing such a standard, we must consider the relationship between cost and value. Value, however, is not so easily defined in a way that will cover all of the prevalent concepts of this term. To attempt to do so leads us into difficulties touched upon in our discussion of the definition of quality.

Naturally, value in some way or other depends upon the degree to which a given quality satisfies human wants; but, in turn, human wants are not constant even for the same person. Furthermore, the degree to which a thing having several quality characteristics tends to satisfy the human wants of even a single person is to a large extent a complicated and unknown function of the magnitudes of the physical characteristics of the thing. Even assuming that the value determined on the basis of the wants of a single person is a constant, it is apparent that the values for different people differ among themselves so that, in the last analysis, value, if it can be expressed quantitatively, is presumably a frequency distribution function.

A brief, terse exposition of the fundamental economic problems involved in attaining a dynamic measure of value will be found in the *Mathematical Introduction to Economics*, G. C. Evans, McGraw-Hill Book Company, New York, 1930. Having obtained a picture of the complicated nature of this problem, one may feel inclined to despair of its solution. However, for some time to come, it is likely that we shall not get away from the desire on the part of all of us to find some measure of quality which is common to all qualities.

In our discussion of economic control, we left out any detailed consideration of this problem of finding an adequate measure of value, even though such a measure apparently would serve a very useful purpose. We started with the tacit assumption that when such a measure of value can be found, it will have two characteristics: it will be a statistical quantity, and it will be statistically related to the measurable quality characteristic of the product.

Beginning at this point, we have shown, particularly in Part I, that certain economic advantages can be attained in the production of a controlled quality. This means, of course, as previously stated, that the quality standard is some frequency distribution function. We emphasized the importance of at least two characteristics, namely, the average  $\overline{\mathbf{X}}$  and the standard deviation  $\boldsymbol{\sigma}$  of this function. To insure that the specified parameters in a given case are economic standards would require a consideration of the fundamental problems involved in establishing measures of value already referred to. In such cases we must choose standards which to the best of our knowledge at the present stage of the development of the subject appear to be reasonable estimates of economic standards.

## 2. Texts on Statistical Theory

The ninth edition of Yule's An Introduction to the Theory of Statistics, C. Griffin & Company, Ltd., 1930, should prove to be a veritable storehouse of knowledge in respect to many of the things discussed in Part II. This is particularly true in respect to measures of central tendency, dispersion, and correlation. As supplementary reading for the more technical part of the discussion, Mathematical Statistics, H. L. Rietz, Open Court Publishing Company, Chicago, 1917, should prove of great value, particularly in connection with the consideration of the analytical aspects of correlation. A. L. Bowley's Elements of Statistics, Chas. Scribner's Sons, New York, 1926-in particular the second volume—contains much of interest in regard to the point binomial and the second approximation (23). The Mathematics of Statistics, R. W. Burgess, Houghton Mifflin Company, New York, 1927, will be found helpful as a general elementary text. It also contains references to several elementary books dealing with statistical methods and their application in other fields such as economics. Two of these should be mentioned here: Statistical Methods Applied to Economics in Business, F. C. Mills, Henry Holt & Company, New York, 1924, and Principles and Methods of Statistics, R. E. Chaddock, Houghton Mifflin Company, Boston, 1925. Attention should also be called to the recent book, The Mathematical Part of Elementary Statistics, B. H. Camp, D. C. Heath & Co., New York, 1931.

#### 3. Curve Fitting

In connection with our discussion of the derivation of empirical formulas to represent relationships, the little book, *Empirical Formulas*, T. R. Running, Wiley & Sons, New York, 1917, is of interest. The method of moments is discussed in some detail in Elderton's book, *Frequency Curves*, previously referred to. The method of least squares is admirably treated in the *Calculus of Observations*, E. T. Whittaker and G. Robinson, 2nd edition, Blackie & Son, London, 1926.

#### REFERENCES FOR PART IV

In 1922, R. A. Fisher presented in *The Philosophical Transactions* of the Royal Society in London an article, "The Mathematical Foundations of Theoretical Statistics," in which he characterized three fundamental problems, namely, specification, distribution, and estimation. At least the first nine paragraphs of this paper should be read by any one interested in the application of statistical theory in the control of quality. In Part IV, we are particularly interested in the theory of distribution which has been developed to a marked extent during the last few decades at the hands of R. A. Fisher, "Student," J. Neyman, L. Isserlis, A. E. R. Church, V. J. Romanovsky, J. Wishart, E. L. Dodd, B. H. Camp, H. Hotelling, Karl Pearson, E. S. Pearson, L. H. C. Tippett, P. R. Rider, A. A. Tchouproff, A. A. Markoff, M. Watanabe and E. Slutsky.

Perhaps one of the best ways for a newcomer to orientate himself in this field of investigation is to read the excellent "Report on Statistics" by H. L. Rietz, published in the Bulletin of the American Mathematical Society, October, 1924, pp. 417-453. References to later work of the men mentioned in the previous paragraph and others on the theory of distribution will be found in the bibliographies of the books by Yule, Rietz, and Kelley, already referred to. In connection with the discussion of Tchebycheff's theorem, one of the most interesting articles is that of A. A. Tchouproff, "Asymptotic Frequency Distribution of the Arithmetic Means of n Correlated Observations for Very Great Values of n," Journal of the Royal Statistical Society, Vol. LXXXVII, 1925, pp. 91-104. This article gives detailed references to the work of Watanabe, Markoff, Slutsky, and others touching upon this same problem.

A recent paper, "British Statistics and Statisticians Today," H. Hotelling, Journal of the American Statistical Association, June,

1930, pp. 186–190, gives an interesting brief account of what is going on in England today in the development of statistical theory. If one is interested in tracing the development of the theory of distribution or, in fact, any part of statistical theory back through the ages, Studies in the History of Statistical Method, Helen M. Walker, Williams & Wilkins Company, Baltimore, 1929, will be found helpful. Perhaps our best general source of information on the important work of the Scandinavian School of statisticians is the book by Arne Fisher previously mentioned.

#### REFERENCES FOR PARTS VI AND VII

#### 1. Estimation

Two fundamental statistical problems are touched upon in Parts VI and VII. One is that of going from a random sample of size n to its universe.

Today there are in the literature the following three general methods of going from a sample to its universe:

- (a) The a posteriori method.
- (b) The method of maximum likelihood.
- (c) The empirical method.

To mention these three in the same breath in the presence of a group of statisticians is almost certain to start an argument, for there is a wide divergence of opinion as to the comparative validities of these methods.

For this reason, the reader will find it advantageous to consider in some detail the original memoirs dealing with these separate methods. The a posteriori method is tied up with the theory of causes and the name of Bayes. The recent important article, "Frequency Distribution of the Unknown Mean of a Sampled Universe," E. C. Molina and R. I. Wilkinson, Bell System Technical Journal, Vol. VIII, pp. 632-645, October, 1929, should prove an interesting starting point for the consideration of this method, although the reader will doubtless wish to read other original memoirs referred to in connection with the discussion of Bayes' theorem in the general bibliographies mentioned in a previous paragraph.

The method of maximum likelihood is tied up largely with the work of R. A. Fisher, starting primarily with his article in the *Philosophical Transactions* previously mentioned.

A recent article, "On the Use and Interpretation of Certain Test Criteria for Purposes of Statistical Inference," E. S. Pearson and J. Neyman, *Biometrika*, XXA, pp. 175-240, 1927, and XXA, pp. 263-294, 1928, is perhaps the best critical discussion of the available methods of solving the problem of estimation. It should certainly be read by any serious student of this subject.

The third edition of Statistical Methods for Research Workers, R. A. Fisher, summarizes most of the detailed methods of estimation developed by him. It is a book of particular value to scientists and engineers, although one must keep in mind the serious limitations of all methods of estimation based upon small samples as noted in the text and discussed in such references as that of Pearson and Neyman.

It is of interest to note that a divergence of opinion is expressed in the literature as to the usefulness of the theory of the so-called small sample. Perhaps most of the critical remarks are based upon the assumption that this theory is to be used as the basis of estimation, and that it may give the impression that we can replace large samples by small ones. In the first place, a careful reading of the available literature does not reveal any specific suggestion to substitute small samples for large ones. In the second place, it should be noted that the application of small sample theory used in this text is required in handling large numbers of data in a rational way by breaking them up into rational subgroups. In this work the distribution theory for small samples plays a prominent rôle.

In general the problem of estimation presents the universal difficulties involved in all induction. If one reads such a book as A Treatise on Probability, J. M. Keynes, Macmillan Company, New York, 1921, he may feel at first very much discouraged, because his attention will have been directed to many of the serious difficulties involved in the application of probability theory. A useful tonic in such a case is to read any one or more of the following books: The Nature of the Physical World, A. S. Eddington, Macmillan Company, New York, 1928; The Logic of Modern Physics, P. W. Bridgman, Macmillan Company, New York, 1928; The Analysis of Matter, Bertrand Russell, Harcourt, Brace & Company, Inc., New York, 1927. At least, these three books should prove to be a tonic, if it is true that misery loves company. Certainly the serious difficulties involved in the interpretation of physical phenomena are common in all fields, and the discussions in these books show how much we must rely upon the application of probability theory even in an "exact" science.

## 2. Detecting Lack of Control

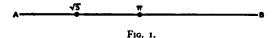
The second fundamental statistical problem is that of determining whether or not a given set of data comes from a constant system of causes, or more generally it is the problem of dividing the universe of objective values into rational subgroups schematically represented in Fig. 144. In our discussion of ways and means for detecting lack of control, we have pointed out again and again the necessity of subdividing the data into rational subgroups. To do this requires the exercise of human judgment.

In the last analysis we must depend upon the use of scientific method—that is, upon human intuition, imagination, reasoning, and knowledge. It is perhaps only through the application of this general method that we can hope to attain good data, one characteristic of which is that they be subdivided into rational subgroups. It may be of interest, therefore, to sketch briefly a course of reading which will be found helpful to the student in the application of scientific method to the further development of the theory of quality control. To do so necessarily takes us into the fields of psychology, philosophy, and logic; into the field of psychology because we must get some sort of picture of the way the mind works; into the field of philosophy because we need some hypothesis as to the nature of reality and the function of laws, theories, and causal explanations; into the field of logic because it presents what we know about the formal methods available in the theory of deduction and induction.

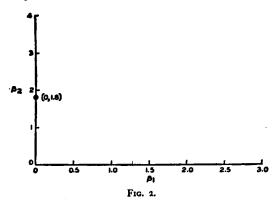
How do data depend upon the mind? What is the effect of factual experience and the effect of reasoning upon an observer? These are important questions. What we sense through any one of our senses depends partly upon previous use of these senses. Thus a child looking at a straight stick extending beneath the surface of a pool of water sees a bent stick. Similarly, the first time one sees what is shown in Fig. 131, he sees the length of the line (a) to be different from that of line (b), although they are of the same length. In this way, factual experience influences what we sense through any one of our senses.

Perhaps more important, however, is that the mental experience involving reasoning influences to a marked extent what we sense. One looking at a line AB, Fig. 1, and thinking of the points on the line, sees those points in an entirely different way after he has tried to place such points as  $\sqrt{3}$  and  $\pi$  on that line.

Almost every day one hears of some physical discovery which has been influenced by a conceptual theory. A trained experimentalist who is at the same time familiar with the current theory or theories having to do with the phenomena which he is investigating will, in many cases at least, be able to get better data for the particular purpose in hand than he would be if he did not know the theory.



In this same connection, it is important to note some of the applications of the theory of frequency curves in assisting one to break down an observed set of data into rational subgroups or to indicate in ways other than those described in the text whether or not this can be done. For example, the fact that an observed point in the  $\beta_1 \beta_2$  plane is in the neighborhood of (0, 1.8), Fig. 2, is consistent

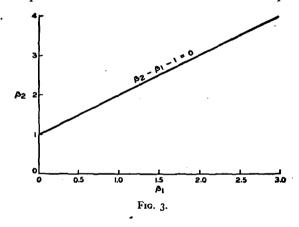


with the hypothesis that the observed set of data came in approximately equal proportion from, let us say, m rational subgroups. In a similar way, an observed value of skewness may be consistent with some rational hypothesis in respect to the causes of variation. In other words, an observed set of statistics can be suggestive of a working hypothesis in much the same way that a rough plot of an observed frequency distribution may be suggestive in the sense indicated by E. B. Wilson in his article, "The Development of a Fre-

quency Function and Some Comments on Curve Fitting," *Proceedings of the National Academy of Sciences*, Vol. 10, 1924, pp. 79-84.

Another very important use of the knowledge of the theory may be that of detecting mistakes in computation. For example, if one found a point  $(\beta_1, \beta_2)$  below the line  $\beta_2 - \beta_1 - 1 = 0$ , Fig. 3, he would know that a mistake had been made because, as was originally shown by Pearson, it is not possible for a frequency distribution function to have a point in this area.

Broadly speaking, we see again why it is so necessary in the control of quality of manufactured product to have data accumulated by someone acquainted with the available factual and conceptual expe-



rience relating to the particular problem in hand. Books such as: Scientific Thought, C. D. Broad, Harcourt, Brace & Company, Inc., New York, 1927; The Function of Reason, A. N. Whitehead, Princeton University Press, Princeton, New Jersey, 1929; The Analysis of Mind, Bertrand Russell, George Allen and Unwin, Ltd., London, 1922; Conflicting Psychologies of Learning, H. B. Bode, D. C. Heath & Company, New York, 1929; The Principles of Psychology, William James, Henry Holt & Company, New York, 1890; The Revolt Against Dualism, A. L. Lovejoy, W. W. Norton & Company, Inc., New York, 1930; and Human Learning, E. L. Thorndike, The Century Co., 1931; contain much of interest in this connection.

Having seen what an important part conceptual experience may play in taking data, one is likely to become more interested in formal logic. The meaning of the laws of thought and the application of syllogistic reasoning take on a new interest. For example, a fundamental understanding of the theory of control tacitly involves such mathematical concepts as function, limit, continuity, and so on, developed to a degree of refinement which comes from the study of the discussion of these subjects in such a book as G. H. Hardy's Pure Mathematics, Cambridge University Press, London, 1928.

Perhaps of even greater interest, however, is the consideration of what we mean by judgment and common sense—two things which we find we must use so often in experimental work of all kinds. One soon finds that there is a considerable divergence of opinion in respect to such matters as will be evidenced by a more or less systematic browsing in the following treatises on logic. Elementary Logic, A. Sidwick, Cambridge University Press, London, 1914; Principles of Logic, H. W. Bradley, Vol. I and Vol. II, 2nd Edition, Oxford University Press, London, 1922; An Introduction to Logic, H. W. B. Joseph, and Edition, Oxford University Press, London, 1922; Formal Logic, J. N. Keynes, 4th Edition, Macmillan Company, Ltd., London, 1928; Logic, W. E. Johnson, Cambridge University Press, London, Vol. I, Logic, General, 1921; Vol. II, Logic Demonstrative Inference: Deductive and Inductive, 1922; Vol. III, The Logical Foundation of Science, 1924; The Logic of Discovery, R. D. Carmichael, The Open Court Publishing Co., Chicago, 1930; Rational Induction, H. H. Dubs, The Chicago University Press, Chicago, 1930; and Scientific Inference, Harold Jeffreys, Macmillan Co., New York, 1931.

It will be noted that the application of the formal scientific method in discovery involves a human choice at every step. For example, in the discovery of a functional or statistical relationship, the following choices must be made:

- 1. Choice of data.
- 2. Choice of functional form.
- 3. Choice of number of parameters, at least in certain cases.
- 4. Choice of method of estimating parameters.

To a certain extent this field of choice is a kind of methodological No-Man's Land.

History of science shows, however, that the discoverers of the past have, in general, been those broadly trained in the particular field of discovery of their choice. They have been those familiar with the status of experimental and theoretical results in their particular field. The importance of theory in helping one to choose the

right thing to be discovered is illustrated by the fact that several elements in the periodic table have been looked for and found because their existence was suggested by the blank spaces. So it is that many of the discoveries of science have been suggested by theory.

Furthermore, it is of interest to note that important discoveries have usually come only after the investigator has surrounded himself for a considerable period of time with the facts bearing upon the subject and during this period has kept these more or less constantly in mind. It is true, however, history also indicates that many of these discoveries have only come after the investigator has dropped the search for a time more or less completely from his conscious consideration. In all cases, however, it appears that preliminary conscious attention to the facts in hand is essential.

Coming now to the more or less formal treatment of scientific method, the following books will be found helpful in something like the order listed: The Foundations of Science, H. Poincare, The Science Press, New York, 1929; The Principles of Science, W. S. Jevons, Macmillan Company, Ltd., London, 1924; Essentials of Scientific Method, A. Wolf, Macmillan Company, New York, 1927; Scientific Method, A. D. Ritchie, Harcourt, Brace & Company, New York, 1923; and Physics, The Elements, N. R. Campbell, Cambridge University Press, London, 1920, together with Vol. III of Johnson's Logic noted in the previous paragraph.

Books such as the Quest for Certainty, John Dewey, Minton Balch Company, New York, 1929; and in particular, A. N. Whitehead's Process and Reality, Macmillan Company, New York, 1930, contain much of interest. Just as a simple example, it is necessary for us to think of a quality characteristic as an entity in the sense adopted by Whitehead if it is to be general enough to be of use in the many practical problems that arise in the interpretation of a sample.

#### OTHER REFERENCES

#### 1. Errors of Measurement

It is assumed that the reader has available one or more of the following books on the discussion of the errors of measurement: The Combination of Observations, David Brunt, University Press, London, 1917; The Calculus of Observations, E. T. Whittaker and G. Robinson, Blackie & Son, London, 1924; The Theory of Measurements, A. D. Palmer, McGraw-Hill Publishing Company, New York, 1930; and

The Theory of Measurements, L. Tuttle and J. Satterly, Longmans, Green & Company, New York, 1925.

Brunt's book contains, in addition to the ordinary discussion of the theory of errors, an interesting introductory chapter indicating various ways of developing the normal law. The book by Tuttle and Satterly gives a particularly good elementary discussion of manythings which must be considered in correcting data for errors of measurement. Palmer's treatise is of particular value in outlining things which must be considered in planning physical measurements so as to reduce the errors of measurement to a minimum.

#### 2. Tables

Of course, every one needs a table of squares, reciprocals, and square roots such as that of Barlow published in revised form by E. and F. N. Spon, Ltd., London, 1930, and a table of logarithms such as those of Vega published by D. Van Nostrand Company, New York, 1916. In addition to these, any one interested in the theory of quality control will find much use for Pearson's Tables for Statisticians and Biometricians, published by the Cambridge University Press, London, 1924. The second volume of these tables which is now in the process of preparation is supposed to contain the tables which have appeared in Biometrika since the publication of the first volume in 1924. In a way, the promised second volume will be even more helpful than the first. The books by Fry, Arne Fisher, and R. A. Fisher contain many useful tables. For a more complete bibliography, the reader is referred again to that of Yule.

## 3. Magazines

Without question, one magazine which has been found most useful in our study of quality control has been Biometrika, edited by Karl Pearson and his son Egon Pearson, and published by the Cambridge University Press, London. It has carried many of the important papers of "Student," R. A. Fisher, L. H. C. Tippett, J. Neyman, J. O. Irwin, Karl Pearson, E. S. Pearson, J. Wishart, and their associates. The Skandinavisk Aktuarietidskrift, Stockholm, contains many important articles in English as well as in foreign languages. The same is true of Metron, an international review of statistics published in Rome, Italy.

The Journal of the American Statistical Association, New York, contains many discussions of the applications of the more elementary theory of statistics in the field of economics. The same can be said of the Journal of the Royal Statistical Society, London, although this Journal has also published several important articles on the theory of statistics. Both of these Journals are of value because of their reviews of current literature. The Annals of Mathematical Statistics is a Journal recently started in cooperation with the American Statistical Association. It is devoted to both theory and application of mathematical statistics.

A glance at any of the complete bibliographies previously referred to will show that important articles have appeared in many other journals than those listed here.

#### 4. Mathematics

It is assumed, of course, that the student of the theory of control is equipped with elementary texts up to and including differential and integral calculus. For a more complete treatment than is ordinarily given in any elementary text, the following books are suggested. In questions involving purely algebraical manipulation as in the discussion of the multinomial theorem, the student will find Algebra, G. Chrystal, Vol. I and Vol. II, 5th Edition, A. and C. Black, Ltd., London, 1920, of great help. For a discussion of the subject of symmetric functions and related topics of interest in the application of the method of moments and the use of semi-invariants, M. Bôcher's Introduction to Higher Algebra, Macmillan Company, New York, 1921, will be helpful. Advanced Calculus, W. F. Osgood, Macmillan Company, New York, 1925, treats in sufficient detail for most purposes the analytical methods required for an understanding of the mathematical theory found in most articles on the subjects of specification, distribution, and estimation. Two excellent books on the mathematical theory of statistics are: Statistique Mathématique, G. Darmois, Gaston Doin et Cie., Paris, 1928, and Statistique Mathématique, Charles Jordan, Gauthier-Villars et Cie., Paris, 1927.

## 5. Graphical Methods

We have neglected to consider in any great detail the important problem of presenting the results of quality control studies in a way to be of greatest service even though so much depends upon a thought-

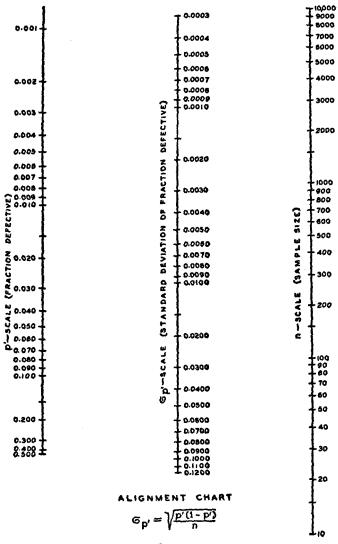
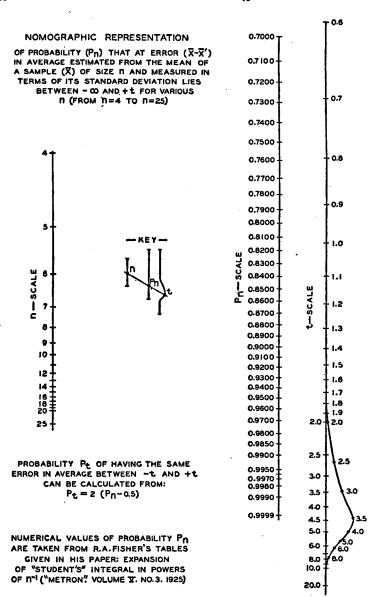


Fig. 4.



F10. 5.

ful and artistic layout of the graphical presentation. In this connection, Layout in Advertising, W. A. Dwiggins, Harper & Bros., New York, 1928, should prove to be suggestive.

In closing, we should note that in the application of the method of control, it is sometimes advisable to substitute nomograms for tables in shop practice. For example, Fig. 4 gives a nomogram which enables one to read off the standard deviation  $\sigma$  in terms of a given sample size n and probability p'. In a similar way, Fig. 5 presents in graphical form the very complicated table of "Student's" integral. For a discussion of this nomogram and of the application of nomography in this way, see the paper by V. A. Nekrassoff, "Nomography in Applications of Statistics," published in *Metron*, Vol. VIII, 1930, Pp. 95-99.

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